

Checkpoints Chapter 2 FORCES**Question 1**

Once the ball has left the bat, there can be only two forces acting on it, the force due to gravity and the air resistance.

If the air resistance is defined as 'very little', then you can assume that this means zero.

$\therefore$ the only force acting is the weight force, which will act directly down.

$\therefore$ **B (ANS)**

Question 2

Because the air resistance must oppose the motion, so it must be acting to the left. Now there are two forces acting.

$\therefore$ **C (ANS)**

Question 3

The instant that the ball is in contact with the ground, the centre of mass of the ball is still moving forward, but the bottom of the ball (the part in contact with the ground) has a frictional force acting on it trying to slow it down. This force will act to the left, and since it is not acting at the CoM, it will produce a torque on the ball, giving rise to spin.

$\therefore$ **C (ANS)**

Question 4

When a car is moving to the right, then to stop it a force needs to act to the left. The only force that stops cars (without deformation) is the friction between the tyre and the road. This friction must act to the left.

To accelerate a car, there needs to be a net force acting in the direction of the acceleration.

$\therefore$ this frictional force must act to the right.

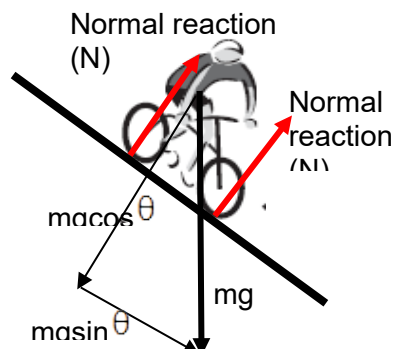
Consider the 'hoon' doing burnouts in Lygon Street. They put oil on the road to minimise friction between the tyre and the road, the put their foot down on the accelerator and the wheels spin around, but the car does not go forward. When the oil is all burnt off, then the car shoots forward, because of the frictional force of the road on the tyre.

$\therefore$ **A (ANS)**

Question 5

The car behind them accelerates them forwards. The seat exerts the force on John and Betty.

$\therefore$ **C (ANS)**

Question 6

The weight force can be resolved into 2 components

$$\therefore mg \cos \theta = N$$

because the bike is not accelerating in this direction

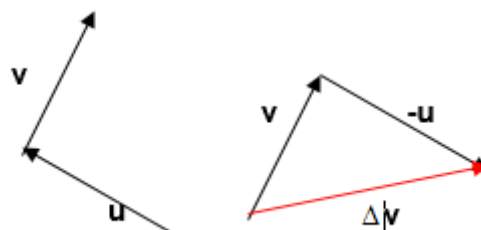
$\therefore$ the unbalanced force causing the

$$\begin{aligned} \text{acceleration} &= mg \sin \theta \\ &= mg \sin 30^\circ \\ &= 0.5mg \end{aligned}$$

$\therefore$ **C (ANS)**

Question 7

The direction of the change in velocity is given by the vector subtraction of $\mathbf{v} - \mathbf{u}$.



$\therefore$ **C (ANS)**

Question 8 (2012 Q3, 2m, 70%)

Force is a vector, so the magnitude of the force and the direction of the force need to be taken into consideration.

A, C and D will all have a net force in the vertical direction. B is the only option that would allow the vectors to sum to zero.

$\therefore$ **B (ANS)**

Question 9

Since the ball bounces up, the change in velocity (given by final – initial) must be up. This is the direction of the acceleration, hence the direction of the net force acting. Therefore the normal reaction must be greater than the weight.

∴ **C (ANS)**

Question 10 (2017 Q7, 1m)

Use $f = ma$

$$\therefore 4 = 2 \times a$$

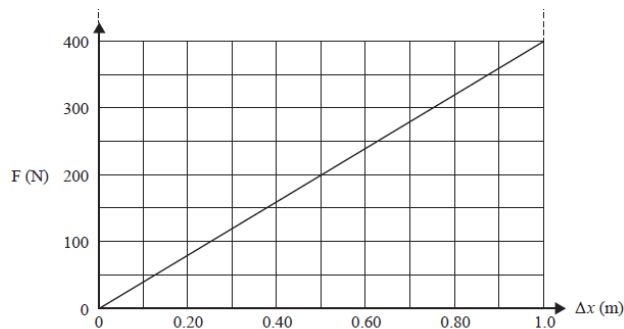
$$\therefore a = 2 \text{ m s}^{-2}$$

∴ **C (ANS)**

Question 11 (2017 Q12, 1m)

Use $F = k \Delta x$

∴ k is the gradient of the F vs Δx graph.



Use points as far apart as possible,

$$\therefore k = \frac{400}{1}$$

$$\therefore k = 400 \text{ N m}^{-1}$$

∴ **C (ANS)**

Question 12

In a car accident, the car needs to come to rest from its initial speed. This means that it needs to lose momentum. This loss of momentum is given by Impulse = $F \Delta t = m \Delta v$. (Newton's second law).

For a car of fixed mass, and a set speed, then the larger 't' is then the smaller 'F' is.

The crash barrier 'crumples slowly' so that the time of the collision is increased, and hence the average force 'F' is smaller. This smaller 'F' means that the average force exerted is less and so the damage done is less.

Question 13a

The frictional force between the tyres and the road is the force that actually accelerates the car.

$$F = ma$$

$$\therefore F = 1200 \times 9$$

$$\therefore F = 10800 \text{ N}$$

$$\therefore \mathbf{F = 1.1 \times 10^4 \text{ N (ANS)}}$$

Question 13b

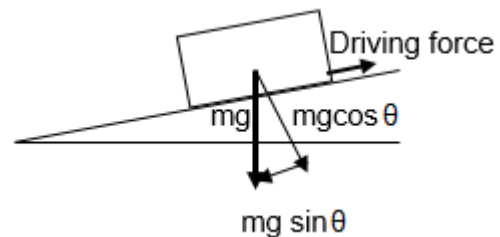
The Normal reaction force = mg , because the car is not accelerating in the vertical direction.

$$\frac{1200 \times 9.0}{1200 \times 9.8}$$

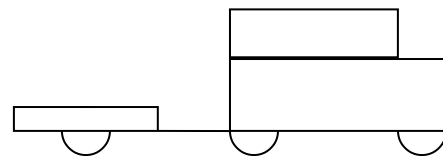
$$= 0.92 \quad \text{(ANS)}$$

Question 14

If the train is travelling at a constant speed, then its acceleration is zero, which means that the sum of the forces acting on it is zero. The driving force are overcoming the component of the train's weight force that is acting down the slope.



$$\begin{aligned} \therefore mg \sin \theta &= \text{Driving force} \\ &= 600 \times 9.8 \times \sin 5^\circ \\ &= \mathbf{512 \text{ N (ANS)}} \end{aligned}$$

Question 15a

This is a simplified version of the diagram. Use your imagination to work out which is the car and which is the trailer.

If the tension in the 'coupling' (which is another word for the connecting rod between the car and the trailer) is 1000 N, then this means that the net force acting on the trailer is 1000 N. This is the force that is available to accelerate the trailer.

Since $F = ma$

$$\therefore 1000 = m \times 1$$

$$\therefore \mathbf{m = 1000 \text{ kg. (ANS)}}$$

Question 15b

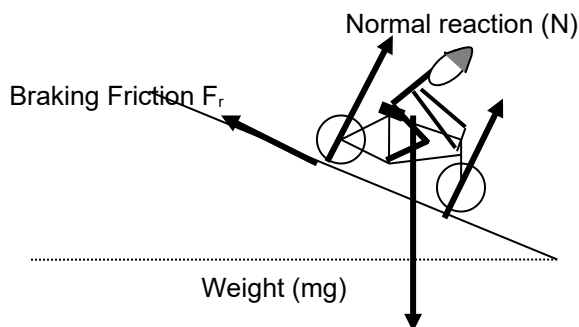
If the mass of the car is 1500 kg, the driving force from the car needs to accelerate 1500 + 1000 kg, using $F = ma$

$$\therefore F = 2500 \times 1 \\ = 2500 \text{ N (ANS)}$$

Question 15c

The frictional force that the road is exerting on the driving wheels, is the only force acting (ignoring air resistance) and so it must be 2500 N, because that is the size of the force that is causing the car/trailer combination to accelerate.

$$\therefore 2500 \text{ N (ANS)}$$

Question 16a

The weight force should always come from the centre of mass of the system (Theo + bike). In reality there are two normal reactions, they come from the bottom of the tyre, where it is in contact with the road. Often the idealised diagram only has one drawn on it.

The braking force is the friction between the tyres and the road. In this diagram Theo only has the back brakes on. Note that Theo is wearing an approved helmet.

Question 16b

The sum of the forces must be zero, because Theo does not accelerate down the hill.

$$\text{This means that } \Sigma F = ma \\ = 0 \quad (\text{ANS})$$

Question 16c

Theo feels the force that the ground pushes up on him, usually when he is vertical, this is the same as his weight force. (This is the force that he pushes down on the ground)

When he is accelerating down he is going to 'feel' the normal reaction force pushing on him.

In this case the reaction force is given by $mg \cos \theta$.

This must always be less than mg , so Theo will feel 'lighter'.

Question 16d

This will only happen if we consider the effects of wind resistance. It is known that air resistance increases with speed, in fact air resistance $\propto v^3$. An Olympic class cyclist uses 90% of their energy overcoming air resistance when they are riding at 40 km h^{-1} . This is the reason why physicists spend a lot of effort in trying to streamline the bike/rider combination. (This is yet another useless bit of trivia, but it continues to demonstrate the importance of physics in everyday life).

So, back to the question, the acceleration will decrease because the component of the weight force that is acting down the slope will stay constant, but the air resistance will increase.

Question 17

At time $t = 2.5 \text{ s}$, there is a net force of 200 N acting on her.

$$\text{This means that since } f = ma \therefore 200 = 80 \times a \\ \therefore a = 2.5 \text{ ms}^{-2} \quad (\text{ANS})$$

You need to be a little careful with this question because you must understand that even though the gradient of the line is zero, there is still a force acting, because this is a force v time graph, not a velocity v time graph.

Question 18a

The change in velocity is always given by $v(\text{final}) - v(\text{initial})$. This is a vector equation, and it turned out to be a $1:1:\sqrt{2}$ triangle.

$$\therefore 14.1 \text{ m s}^{-1} \quad (\text{ANS})$$

Question 18b

$$\text{The impulse } I = m \Delta v \\ = 0.250 \times 14.14 \\ = 3.5 \text{ N s} \quad (\text{ANS})$$

Question 18c

The impulse on the bat has to be the equal and opposite of the impulse on the ball.

$$\therefore 3.5 \text{ N s} \quad (\text{ANS})$$

Question 19a

She is travelling at a steady speed of 15 m/s.
So she is not accelerating
 $\therefore$ the sum of the forces is zero.

$$\therefore 0 \text{ N} \quad (\text{ANS})$$

Question 19b

For the sum of the forces to be zero, then the ground must be exerting a force equal to in size, but opposite in direction, to the frictional forces acting.

So the ground must be exerting a force of $(55 + 5) = 60 \text{ N}$ (ANS)

Question 20a

$u = 0$, $x = 16$, $t = 4$, $a = ??$

$$x = ut + \frac{1}{2} a t^2$$

$$16 = 0 + \frac{1}{2} \times a \times 4^2$$

$$16 = 8a$$

$$\therefore a = 2 \text{ m s}^{-2} \quad (\text{ANS})$$

Question 20b

$F = ma$

$$\therefore F = 90 \times 2 = 180 \text{ N} \quad (\text{ANS})$$

Question 20c

This is the force that is causing the bike to accelerate.

$$\therefore 180 \text{ N} \quad (\text{ANS})$$

Question 21a (2012 Q4a, 2m, 75%)

Cable A is supporting both masses.
The net force on the 2.0 kg sphere is zero.
Therefore the tension in cable A is equal and opposite to the weight of both spheres.

$$\therefore T = (1.0 + 2.0) \times 10$$

$$\therefore T = 30 \text{ N} \quad (\text{ANS})$$

The direction of this force is **UP**.

Question 21b (2012 Q4b, 2m, 15%)

Newton's third law can be written in the form;

$$\mathbf{F}_{A \text{ on } B} = -\mathbf{F}_{B \text{ on } A}$$

Then the weight of sphere is

$$\mathbf{F}_{\text{Earth on Sphere}}$$

In terms of Newton's action and reaction pairs, the 'reaction' will be

$$\mathbf{F}_{\text{Sphere on Earth}} \quad \text{UP} \quad (\text{ANS})$$

This question was done very poorly, 15%, so ensure that you understand the concepts underlying the answer.

Question 22a (2012 Q5a, 1m, 60%)

Constant speed implies that the net force is zero.

$$\therefore T_2 = 400 \text{ N and}$$

$$\therefore T_1 = 400 + T_2$$

$$\therefore T_1 = 800 \text{ N} \quad (\text{ANS})$$

Question 22b (2012 Q5b, 2m, 60%)

Isolate the second log.

$$\therefore \Sigma F = ma$$

$$\therefore T_2 - 400 = 600 \times 0.50$$

$$\therefore T_2 = 300 + 400$$

$$\therefore T_2 = 700 \text{ N} \quad (\text{ANS})$$

Question 22c (2012 Q5c, 2m, 80%)

$U = 4.0$, $a = 0.50$, $x = 20$, $v = ?$

Use $v^2 - u^2 = 2ax$

$$\therefore v^2 - 4^2 = 2 \times 0.5 \times 20$$

$$\therefore v^2 = 20 + 16$$

$$\therefore v^2 = 36$$

$$\therefore v = 6 \text{ m s}^{-1} \quad (\text{ANS})$$

Question 22d (2012 Q5d, 3m, 53%)

Rope 1 needs to provide the tension to accelerate both logs, so the tension in it will be greater than that of Rope 2.

$$\therefore \text{Rope 1} \quad (\text{ANS})$$

Use $\Sigma F = ma$

$$\therefore T_1 - T_2 - 400 = 600a$$

and

$$T_2 - 400 = 600a$$

$$\therefore T_2 = 600a + 400$$

$$\therefore T_1 - (600a + 400) - 400 = 600a$$

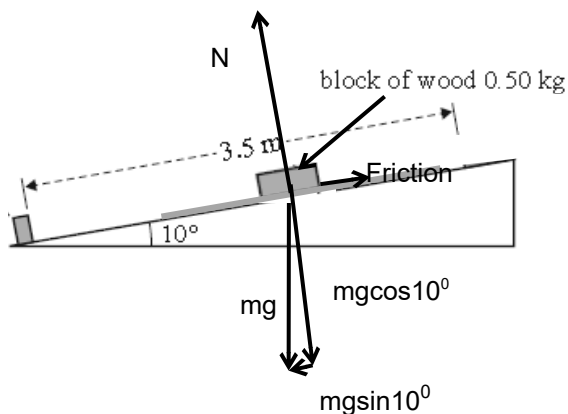
$$\therefore T_1 = 600a + (600a + 400) + 400$$

Use $T_1 = 2400 \text{ N}$ at its breaking point.

$$\therefore 2400 = 1200a + 800$$

$$\therefore 1600 = 1200 \times a$$

$$\therefore a = 1.33 \text{ m s}^{-2} \quad (\text{ANS})$$

Question 23 (2013 Q1b, 3m, 40%)

From the diagram we get

$$\Sigma F = ma$$

$$\therefore 0.5a = mg \sin 10^\circ - \text{Friction}$$

First we need to find 'a'.

Use $x = ut + \frac{1}{2}at^2$ to get

$$3.5 = \frac{1}{2} \times a \times 6^2$$

$$\therefore a = 0.1944$$

Substitute back into

$$\therefore 0.5a = mg \sin 10^\circ - \text{Friction}$$

$$\therefore 0.5 \times 0.1944 = 0.5 \times 9.8 \times \sin 10^\circ - \text{Friction}$$

$$\therefore 0.0972 = 0.8508 - \text{Friction}$$

$$\therefore \text{Friction} = 0.75 \text{ N (ANS)}$$

Note that the answer in the back of the book is incorrect.

Substitute into $T = m_2a$

$$\therefore T = 6 \times 2.5$$

$$= 15 \text{ N (ANS)}$$

Note that this question was done very poorly on the exam.

Question 25 (2014 Q1b, 2m, 50%)

Use $T = \Sigma ma$

$$= 2 \times 10 \times 10^3 \times 0.2$$

$$= 4 \times 10^3 \text{ N (ANS)}$$

Question 26 (2014 Q2a, 2m, 60%)

Use the equation $F = k \times \Delta x$

$F = mg$, so

$$0.05 \times 10 = k \times 0.1$$

$$\therefore 0.5 / 0.1 = k$$

$$\therefore k = 5 \text{ N m}^{-1}$$

$$0.1 \times 10 = k \times 0.2$$

$$\therefore 0.1 / 0.2 = k$$

$$\therefore k = 5 \text{ N m}^{-1}$$

$$0.15 \times 10 = k \times 0.3$$

$$\therefore 0.15 / 0.3 = k$$

$$\therefore k = 5 \text{ N m}^{-1}$$

$$\therefore k = 5 \text{ N m}^{-1} \text{ (ANS)}$$

Question 24a (2013 Q2a, 1m, 70%)

$$W = mg$$

$$\therefore W = 2 \times 10$$

$$= 20 \text{ N (ANS)}$$

Make sure you answer the question, by including the unit.

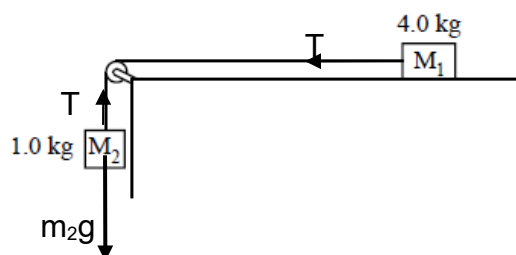
Question 24b (2013 Q2b, 3m, 27%)

Use the equations $m_1a = m_1g - T$
and $T = m_2a$

$$\therefore 2a = 20 - 6a$$

$$\therefore 8a = 20$$

$$\therefore a = 2.5 \text{ ms}^{-2}$$

Question 27a (2015 Q2a, 2m, 52%)

For M_2 , use $\Sigma F = ma$

$$\therefore m_2g - T = m_2a$$

$$\therefore 1 \times 10 - T = 1 \times a$$

For M_1 , use $\Sigma F = ma$

$$\therefore T = m_1a$$

$$\therefore T = 4 \times a$$

Combine the two equations to get

$$10 - 4a = a$$

$$\therefore 10 = 5a$$

$$\therefore a = 2 \text{ m s}^{-2} \text{ (ANS)}$$

Question 27b (2015 Q2b, 2m, 54%)Consider M_1 ,

$$T = 4 \times a$$

$$\therefore T = 4 \times 2$$

$$\therefore T = 8 \text{ N (ANS)}$$

Question 28 (2016 Q3a, 2m, 60%)Use $F = k \Delta x$ With 1 mass, $F = 0.050 \times 9.8$

$$\therefore F = 0.49 \text{ N.}$$

$$\therefore 0.49 = k \times 0.25$$

$$\therefore k = 1.96$$

$$\therefore k = 2 \text{ N m}^{-1} \text{ (ANS)}$$

Question 29 (2016 Q4d, 3m, 57%)

Use the work done is the change in KE.

$$\therefore F \times d = \Delta KE$$

$$KE_i = \frac{1}{2}mv^2$$

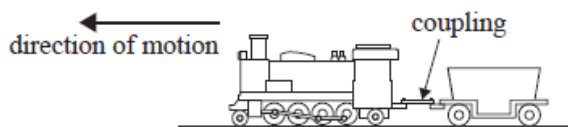
$$= \frac{1}{2} \times 4 \times 2^2$$

$$= 8 \text{ J}$$

$$\therefore F \times d = 8$$

$$\therefore 2.0 \times d = 8$$

$$\therefore d = 4 \text{ m (ANS)}$$

Question 30 (~2016 Q1)

For the wagon to accelerate at 0.10 m s^{-1} , use $F = ma$, where F is the tension in the coupling.

$$\therefore F = 10\,000 \times 0.10$$

$$\therefore F = 1000 \text{ N (ANS)}$$
