

The Mathematical Association of Victoria

Trial Exam 2017

SPECIALIST MATHEMATICS

Written Examination 1

STUDENT NAME _____

Reading time: 15 minutes

Writing time: 1 hour

QUESTION AND ANSWER BOOK

Structure of Book

<i>Number of questions</i>	<i>Number of questions to be answered</i>	<i>Number of marks</i>
10	10	40

- Students are permitted to bring into the examination room: pens, pencils, highlighters, erasers, sharpeners, rulers.
- Students are NOT permitted to bring into the examination room: any technology (calculators or software), notes of any kind, blank sheets of paper and/or correction fluid/tape.

Materials supplied

- Question and answer book of 14 pages.
- Formula sheet.
- Working space is provided throughout the book.

Instructions

- Write your **name** in the space provided above on this page.
- Unless otherwise indicated, the diagrams in this book are **not** drawn to scale.
- All written responses must be in English.

Students are NOT permitted to bring mobile phones and/or any other unauthorised electronic devices into the examination room.

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Question 2 (4 marks)

The number of minutes it takes for an LG V10 phone to fully charge from 0% is normally distributed with a mean of 65 minutes and a standard deviation of 3 minutes. The number of minutes it takes for an LG G5 phone to fully charge from 0% is normally distributed with a mean of 76 minutes and a standard deviation of 5 minutes.

Let the random variable X represent the charging time of the LG V10 phone and let the random variable Y represent the charging time of the LG G5.

- a. The probability that the LG G5 phone fully charges from 0% in less time than the LG V10 phone is equal to $\Pr(Z \leq a)$ where Z has the standard normal distribution. Find the value of a . 2 marks

A phone seller decides to test the claim that the LG V10 phone takes an average time of 65 minutes to fully charge from 0% using the following hypothesis:

$$H_0 : \mu = 65 \text{ minutes.}$$

$$H_1 : \mu \neq 65 \text{ minutes.}$$

The seller collected a sample of 50 LG V10 phones and found that the average time to fully charge from 0% was 68 minutes.

- b. The p -value for this test is given by the expression $2\Pr(Z \leq b)$, where Z has the standard normal distribution. Find the value of b . 2 marks

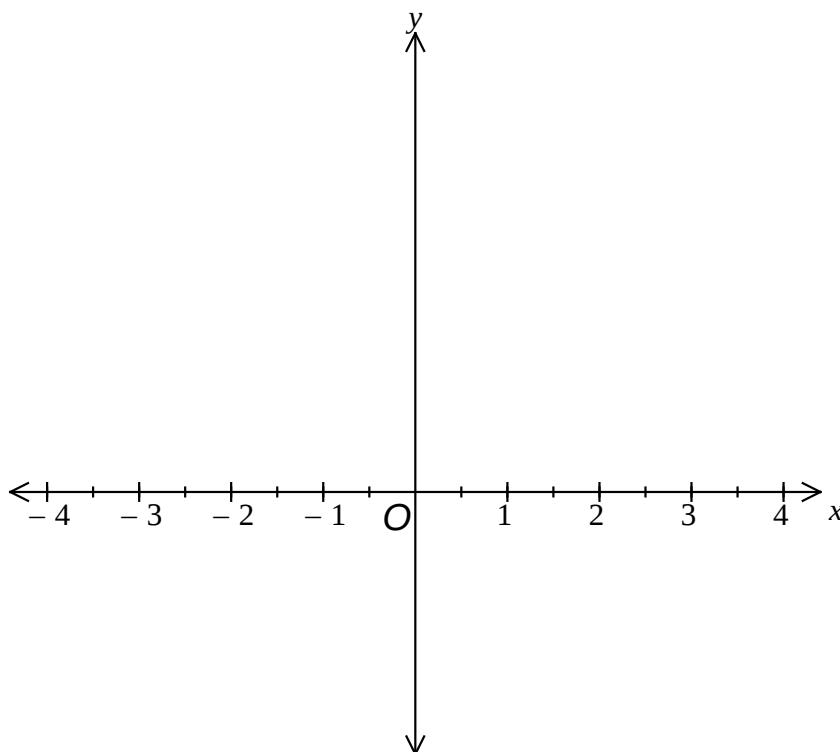
Question 3 (5 marks)

- a. Find the equation of all asymptotes of $f(x) = \frac{x^3 - 3x + 2}{x - 2}$.

2 marks

- b. Draw a graph of $y = f(x)$ over its maximal domain. Label all axes intercepts with their coordinates and all asymptotes with their equations.

3 marks

**TURN OVER**

Find in polar form all solutions of $z^4 = \sqrt{3}z^2 - 1$, $z \in \mathbb{C}$.

[illegible]

Question 5 (7 marks)

A lift begins moving vertically upwards from rest with an acceleration given by $\frac{1}{3}\sqrt{25-v^2} \text{ ms}^{-2}$

where $v \text{ ms}^{-1}$ is its speed t seconds after it starts moving. This acceleration is maintained until the lift reaches its maximum speed.

- a.** The lift moves a distance of b metres before reaching its maximum speed. Find the value of b . 3 marks

[illegible]

TURN OVER

- b.** The speed of the lift is increasing for $t \in [0, t_1)$. Find the largest value of t_1 .

2 marks

Once the lift reaches its maximum speed the acceleration changes to $-\frac{1}{3}\sqrt{10v - v^2} \text{ ms}^{-2}$ and the lift slows down.

- c. There is a 20 kg parcel sitting on a set of bathroom scales inside the lift.
Find the reading of the scales when the lift is slowing down and has a speed of 2 ms^{-1} .
Give your answer in units of **kg wt**.

2 marks

TURN OVER

Question 6 (3 marks)

Let C be a curve defined by the equation $y = f(x)$. The arc length of C from the points (a, b) to

$(2, -3)$, where $a < 2$, is given by $\int_a^2 \frac{\sqrt{x^2 - 6x + 13}}{3 - x} dx$.

Find the two rules for the function $f(x)$.

[illegible]

