

Victorian Certificate of Education
2020

SUPERVISOR TO ATTACH PROCESSING LABEL HERE

STUDENT NUMBER

Letter

MATHEMATICAL METHODS

Written examination 2

Wednesday 18 November 2020

Reading time: 3.00 pm to 3.15 pm (15 minutes)

Writing time: 3.15 pm to 5.15 pm (2 hours)

QUESTION AND ANSWER BOOK

Structure of book

Section	Number of questions	Number of questions to be answered	Number of marks
A	20	20	20
B	5	5	60
			Total 80

- Students are permitted to bring into the examination room: pens, pencils, highlighters, erasers, sharpeners, rulers, a protractor, set squares, aids for curve sketching, one bound reference, one approved technology (calculator or software) and, if desired, one scientific calculator. Calculator memory DOES NOT need to be cleared. For approved computer-based CAS, full functionality may be used.
- Students are NOT permitted to bring into the examination room: blank sheets of paper and/or correction fluid/tape.

Materials supplied

- Question and answer book of 27 pages
- Formula sheet
- Answer sheet for multiple-choice questions

Instructions

- Write your **student number** in the space provided above on this page.
- Check that your **name** and **student number** as printed on your answer sheet for multiple-choice questions are correct, **and** sign your name in the space provided to verify this.
- Unless otherwise indicated, the diagrams in this book are **not** drawn to scale.
- All written responses must be in English.

At the end of the examination

- Place the answer sheet for multiple-choice questions inside the front cover of this book.
- You may keep the formula sheet.

Students are NOT permitted to bring mobile phones and/or any other unauthorised electronic devices into the examination room.

SECTION A – Multiple-choice questions**Instructions for Section A**

Answer **all** questions in pencil on the answer sheet provided for multiple-choice questions.

Choose the response that is **correct** for the question.

A correct answer scores 1; an incorrect answer scores 0.

Marks will **not** be deducted for incorrect answers.

No marks will be given if more than one answer is completed for any question.

Unless otherwise indicated, the diagrams in this book are **not** drawn to scale.

Question 1

Let f and g be functions such that $f(-1) = 4$, $f(2) = 5$, $g(-1) = 2$, $g(2) = 7$ and $g(4) = 6$.

The value of $g(f(-1))$ is

- A. 2
- B. 4
- C. 5
- D. 6
- E. 7

Question 2

Let $p(x) = x^3 - 2ax^2 + x - 1$, where $a \in R$. When p is divided by $x + 2$, the remainder is 5.

The value of a is

- A. 2
- B. $-\frac{7}{4}$
- C. $\frac{1}{2}$
- D. $-\frac{3}{2}$
- E. -2

Question 3

Let $f'(x) = \frac{2}{\sqrt{2x-3}}$.

If $f(6) = 4$, then

- A. $f(x) = 2\sqrt{2x-3}$
- B. $f(x) = \sqrt{2x-3} - 2$
- C. $f(x) = 2\sqrt{2x-3} - 2$
- D. $f(x) = \sqrt{2x-3} + 2$
- E. $f(x) = \sqrt{2x-3}$

Question 4

The solutions of the equation $2\cos\left(2x - \frac{\pi}{3}\right) + 1 = 0$ are

- A. $x = \frac{\pi(6k-2)}{6}$ or $x = \frac{\pi(6k-3)}{6}$, for $k \in \mathbb{Z}$
- B. $x = \frac{\pi(6k-2)}{6}$ or $x = \frac{\pi(6k+5)}{6}$, for $k \in \mathbb{Z}$
- C. $x = \frac{\pi(6k-1)}{6}$ or $x = \frac{\pi(6k+2)}{6}$, for $k \in \mathbb{Z}$
- D. $x = \frac{\pi(6k-1)}{6}$ or $x = \frac{\pi(6k+3)}{6}$, for $k \in \mathbb{Z}$
- E. $x = \pi$ or $x = \frac{\pi(6k+2)}{6}$, for $k \in \mathbb{Z}$

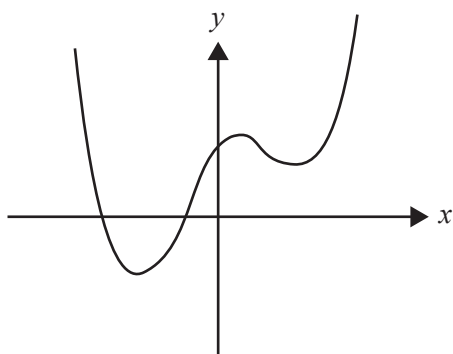
Question 5

The graph of the function $f: D \rightarrow \mathbb{R}$, $f(x) = \frac{3x+2}{5-x}$, where D is the maximal domain, has asymptotes

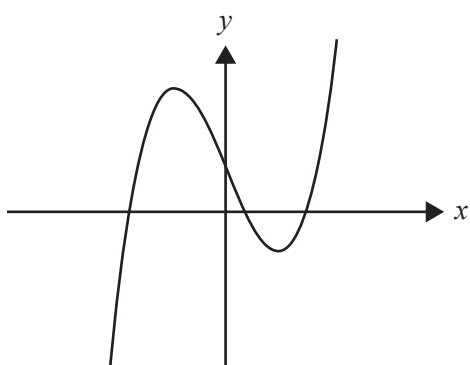
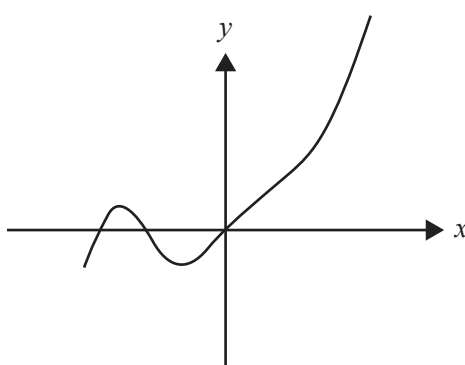
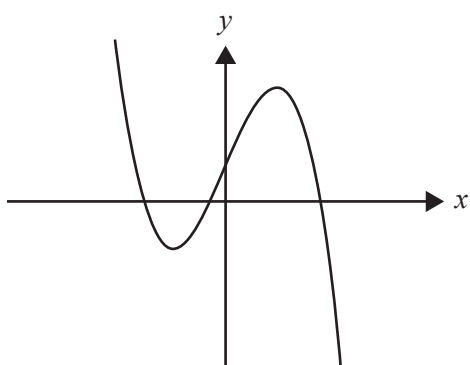
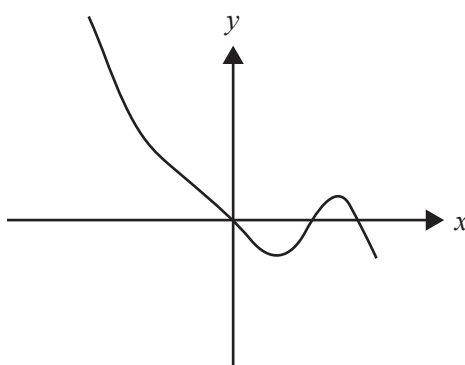
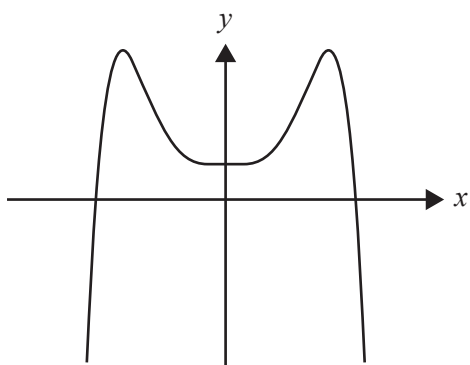
- A. $x = -5$, $y = \frac{3}{2}$
- B. $x = -3$, $y = 5$
- C. $x = \frac{2}{3}$, $y = -3$
- D. $x = 5$, $y = 3$
- E. $x = 5$, $y = -3$

Question 6

Part of the graph of $y = f'(x)$ is shown below.



The corresponding part of the graph of $y = f(x)$ is best represented by

A.**B.****C.****D.****E.**

Question 7

If $f(x) = e^{g(x^2)}$, where g is a differentiable function, then $f'(x)$ is equal to

- A. $2xe^{g(x^2)}$
- B. $2xg(x^2)e^{g(x^2)}$
- C. $2xg'(x^2)e^{g(x^2)}$
- D. $2xg'(2x)e^{g(x^2)}$
- E. $2xg'(x^2)e^{g(2x)}$

Question 8

Items are packed in boxes of 25 and the mean number of defective items per box is 1.4

Assuming that the probability of an item being defective is binomially distributed, the probability that a box contains more than three defective items, correct to three decimal places, is

- A. 0.037
- B. 0.048
- C. 0.056
- D. 0.114
- E. 0.162

Question 9

If $\int_4^8 f(x)dx = 5$, then $\int_0^2 f(2(x+2))dx$ is equal to

- A. 12
- B. 10
- C. 8
- D. $\frac{1}{2}$
- E. $\frac{5}{2}$

Question 10

Given that $\log_2(n+1) = x$, the values of n for which x is a positive integer are

- A. $n = 2^k, k \in \mathbb{Z}^+$
- B. $n = 2^k - 1, k \in \mathbb{Z}^+$
- C. $n = 2^{k-1}, k \in \mathbb{Z}^+$
- D. $n = 2k - 1, k \in \mathbb{Z}^+$
- E. $n = 2k, k \in \mathbb{Z}^+$

Question 11

The lengths of plastic pipes that are cut by a particular machine are a normally distributed random variable, X , with a mean of 250 mm.

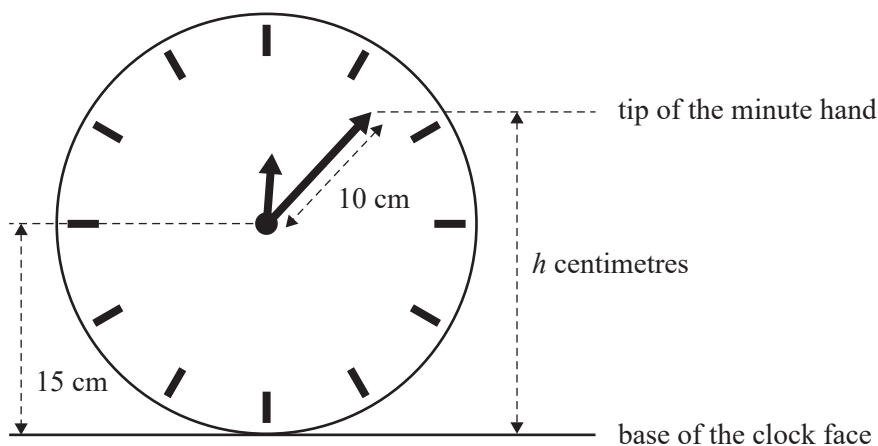
Z is the standard normal random variable.

If $\Pr(X < 259) = 1 - \Pr(Z > 1.5)$, then the standard deviation of the lengths of plastic pipes, in millimetres, is

- A. 1.5
- B. 3
- C. 6
- D. 9
- E. 12

Question 12

A clock has a minute hand that is 10 cm long and a clock face with a radius of 15 cm, as shown below.



At 12.00 noon, both hands of the clock point vertically upwards and the tip of the minute hand is at its maximum distance above the base of the clock face.

The height, h centimetres, of the tip of the minute hand above the base of the clock face t minutes after 12.00 noon is given by

- A. $h(t) = 15 + 10 \sin\left(\frac{\pi t}{30}\right)$
- B. $h(t) = 15 - 10 \sin\left(\frac{\pi t}{30}\right)$
- C. $h(t) = 15 + 10 \sin\left(\frac{\pi t}{60}\right)$
- D. $h(t) = 15 + 10 \cos\left(\frac{\pi t}{60}\right)$
- E. $h(t) = 15 + 10 \cos\left(\frac{\pi t}{30}\right)$

Question 13

The transformation $T: R^2 \rightarrow R^2$ that maps the graph of $y = \cos(x)$ onto the graph of $y = \cos(2x + 4)$ is

A. $T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} \frac{1}{2} & 0 \\ 0 & 1 \end{bmatrix} \left(\begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} -4 \\ 0 \end{bmatrix}\right)$

B. $T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} \frac{1}{2} & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} -4 \\ 0 \end{bmatrix}$

C. $T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} \frac{1}{2} & 0 \\ 0 & 1 \end{bmatrix} \left(\begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} -2 \\ 0 \end{bmatrix}\right)$

D. $T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} 2 & 0 \\ 0 & 1 \end{bmatrix} \left(\begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} 2 \\ 0 \end{bmatrix}\right)$

E. $T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} 2 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} 2 \\ 0 \end{bmatrix}$

Question 14

The random variable X is normally distributed.

The mean of X is twice the standard deviation of X .

If $\Pr(X > 5.2) = 0.9$, then the standard deviation of X is closest to

A. 7.238

B. 14.476

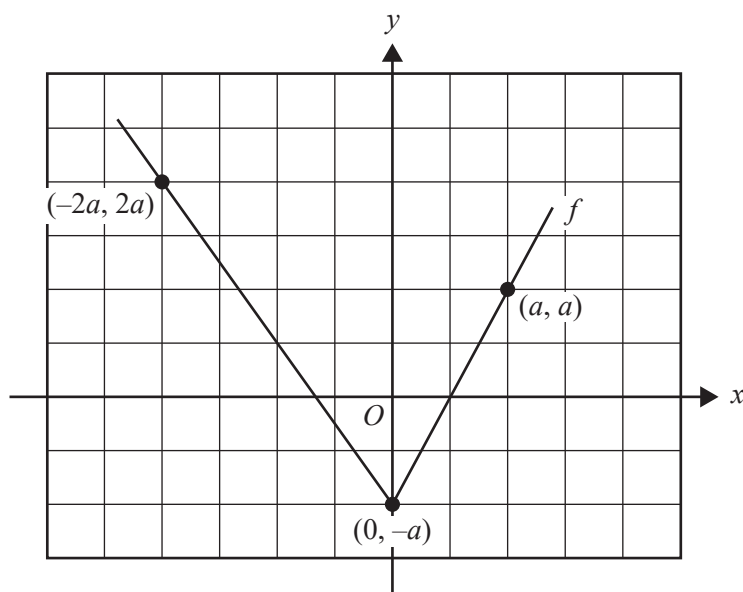
C. 3.327

D. 1.585

E. 3.169

Question 15

Part of the graph of a function f , where $a > 0$, is shown below.

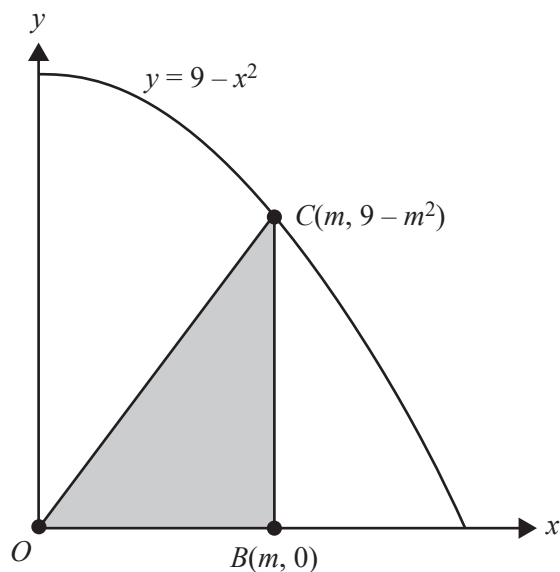


The average value of the function f over the interval $[-2a, a]$ is

- A. 0
- B. $\frac{a}{3}$
- C. $\frac{a}{2}$
- D. $\frac{3a}{4}$
- E. a

Question 16

A right-angled triangle, OBC , is formed using the horizontal axis and the point $C(m, 9 - m^2)$, where $m \in (0, 3)$, on the parabola $y = 9 - x^2$, as shown below.



The maximum area of the triangle OBC is

- A. $\frac{\sqrt{3}}{3}$
- B. $\frac{2\sqrt{3}}{3}$
- C. $\sqrt{3}$
- D. $3\sqrt{3}$
- E. $9\sqrt{3}$

Question 17

Let $f(x) = -\log_e(x + 2)$.

A tangent to the graph of f has a vertical axis intercept at $(0, c)$.

The maximum value of c is

- A. -1
- B. $-1 + \log_e(2)$
- C. $-\log_e(2)$
- D. $-1 - \log_e(2)$
- E. $\log_e(2)$

Question 18

Let $a \in (0, \infty)$ and $b \in \mathbb{R}$.

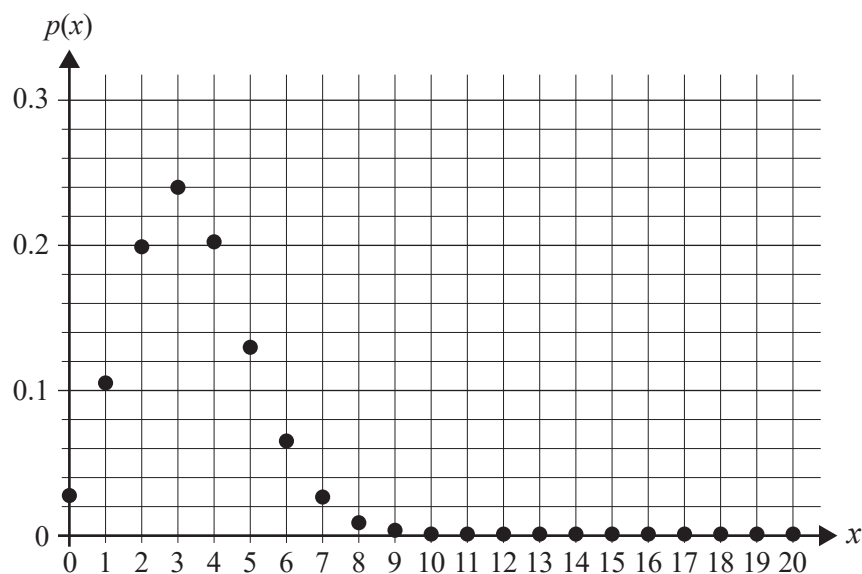
Consider the function $h: [-a, 0) \cup (0, a] \rightarrow \mathbb{R}$, $h(x) = \frac{a}{x} + b$.

The range of h is

- A. $[b - 1, b + 1]$
- B. $(b - 1, b + 1)$
- C. $(-\infty, b - 1) \cup (b + 1, \infty)$
- D. $(-\infty, b - 1] \cup [b + 1, \infty)$
- E. $[b - 1, \infty)$

Question 19

Shown below is the graph of p , which is the probability function for the number of times, x , that a '6' is rolled on a fair six-sided die in 20 trials.



Let q be the probability function for the number of times, w , that a '6' is **not** rolled on a fair six-sided die in 20 trials. $q(w)$ is given by

- A. $p(20 - w)$
- B. $p\left(1 - \frac{w}{20}\right)$
- C. $p\left(\frac{w}{20}\right)$
- D. $p(w - 20)$
- E. $1 - p(w)$

Question 20

Let $f: R \rightarrow R$, $f(x) = \cos(ax)$, where $a \in R \setminus \{0\}$, be a function with the property

$$f(x) = f(x + h), \text{ for all } h \in Z$$

Let $g: D \rightarrow R$, $g(x) = \log_2(f(x))$ be a function where the range of g is $[-1, 0]$.

A possible interval for D is

- A. $\left[\frac{1}{4}, \frac{5}{12}\right]$
- B. $\left[1, \frac{7}{6}\right]$
- C. $\left[\frac{5}{3}, 2\right]$
- D. $\left[-\frac{1}{3}, 0\right]$
- E. $\left[-\frac{1}{12}, \frac{1}{4}\right]$

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**END OF SECTION A
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SECTION B

Instructions for Section B

Answer **all** questions in the spaces provided.

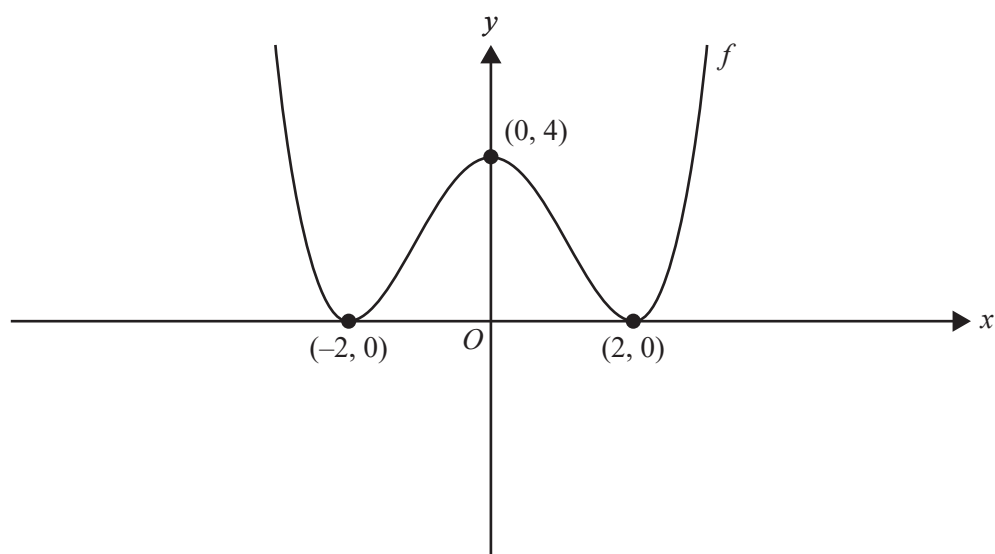
In all questions where a numerical answer is required, an exact value must be given unless otherwise specified.

In questions where more than one mark is available, appropriate working **must** be shown.

Unless otherwise indicated, the diagrams in this book are **not** drawn to scale.

Question 1 (11 marks)

Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = a(x+2)^2(x-2)^2$, where $a \in \mathbb{R}$. Part of the graph of f is shown below.



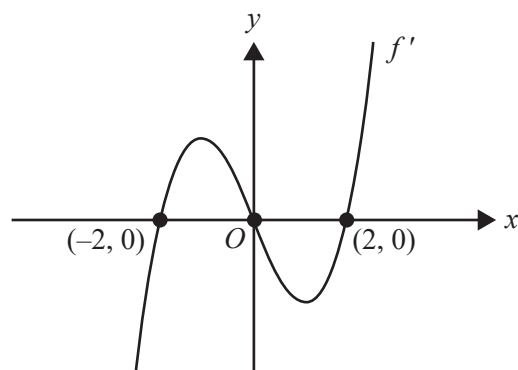
- a. Show that $a = \frac{1}{4}$.

1 mark

- b. Express $f(x) = \frac{1}{4}(x+2)^2(x-2)^2$ in the form $f(x) = \frac{1}{4}x^4 + bx^2 + c$, where b and c are integers.

1 mark

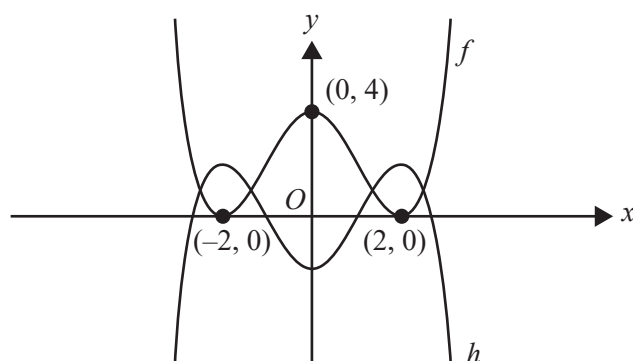
Part of the graph of the derivative function f' is shown below.



- c. i. Write the rule for f' in terms of x . 1 mark

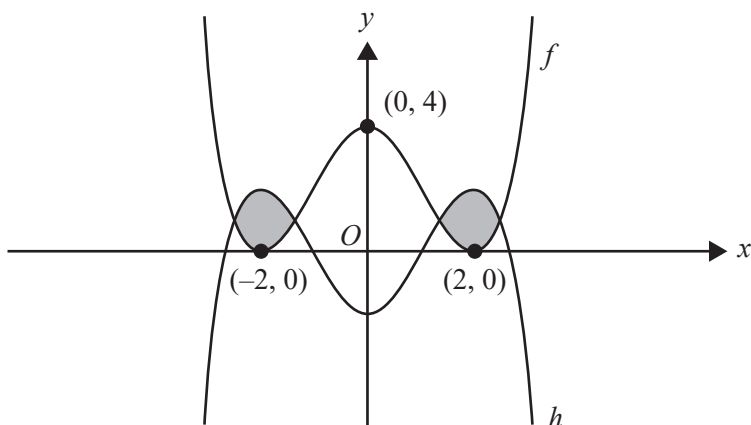
- ii. Find the minimum value of the graph of f' on the interval $x \in (0, 2)$. 2 marks

Let $h: \mathbb{R} \rightarrow \mathbb{R}$, $h(x) = -\frac{1}{4}(x+2)^2(x-2)^2 + 2$. Parts of the graphs of f and h are shown below.



- d. Write a sequence of two transformations that map the graph of f onto the graph of h . 1 mark

- ---
- ---



- e. i. State the values of x for which the graphs of f and h intersect. 1 mark

- ii. Write down a definite integral that will give the total area of the shaded regions in the graph above. 1 mark

- iii. Find the total area of the shaded regions in the graph above. Give your answer correct to two decimal places. 1 mark

- f. Let D be the vertical distance between the graphs of f and h .
Find all values of x for which D is at most 2 units. Give your answers correct to two decimal places. 2 marks

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SECTION B – continued
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Question 2 (11 marks)

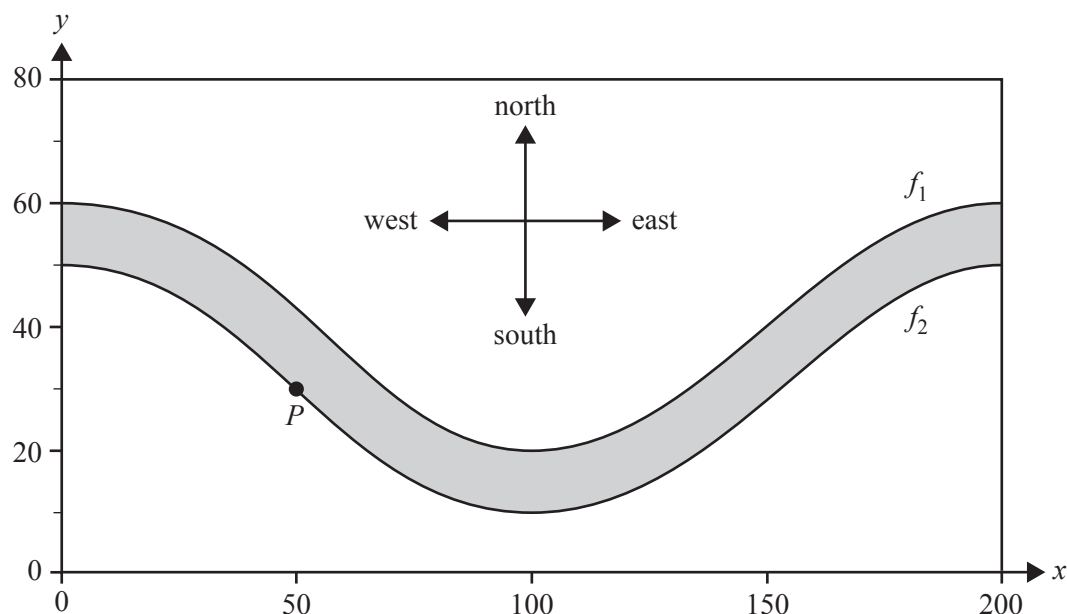
An area of parkland has a river running through it, as shown below. The river is shown shaded.

The north bank of the river is modelled by the function $f_1 : [0, 200] \rightarrow \mathbb{R}$, $f_1(x) = 20 \cos\left(\frac{\pi x}{100}\right) + 40$.

The south bank of the river is modelled by the function $f_2 : [0, 200] \rightarrow \mathbb{R}$, $f_2(x) = 20 \cos\left(\frac{\pi x}{100}\right) + 30$.

The horizontal axis points east and the vertical axis points north.

All distances are measured in metres.



A swimmer always starts at point P , which has coordinates $(50, 30)$.

Assume that no movement of water in the river affects the motion or path of the swimmer, which is always a straight line.

- a.** The swimmer swims north from point P .

Find the distance, in metres, that the swimmer needs to swim to get to the north bank of the river.

1 mark

- b. The swimmer swims east from point P .

Find the distance, in metres, that the swimmer needs to swim to get to the north bank of the river.

2 marks

- c. On another occasion, the swimmer swims the minimum distance from point P to the north bank of the river.

Find this minimum distance. Give your answer in metres, correct to one decimal place.

2 marks

- d. Calculate the surface area of the section of the river shown on the graph on page 16, in square metres.

1 mark

- e. A horizontal line is drawn through point P . The section of the river that is south of the line is declared a 'no swimming' zone.

Find the area of the 'no swimming' zone, correct to the nearest square metre.

3 marks

- f. Scientists observe that the north bank of the river is changing over time. It is moving further north from its current position. They model its predicted new location using the function with rule $y = k f_1(x)$, where $k \geq 1$.

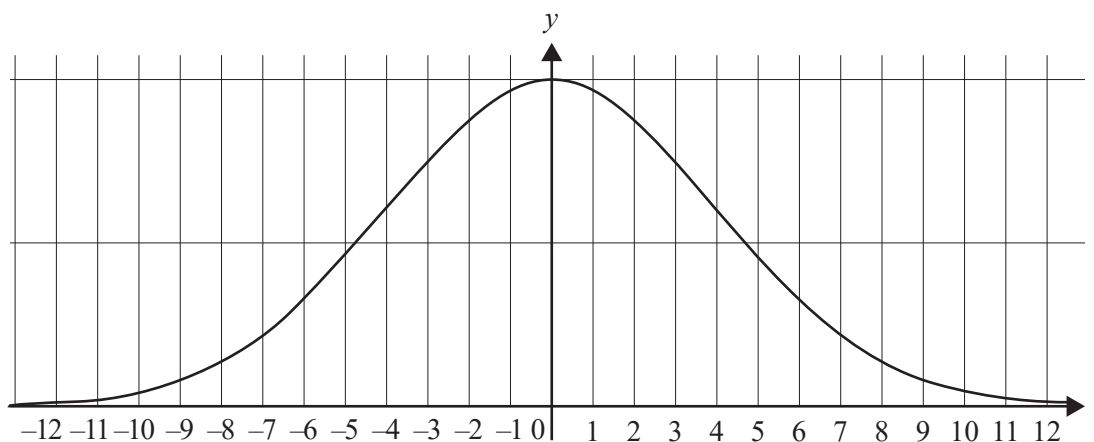
Find the values of k for which the distance **north** across the river, for all parts of the river, is strictly less than 20 m.

2 marks

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Question 3 (12 marks)

A transport company has detailed records of all its deliveries. The number of minutes a delivery is made before or after its scheduled delivery time can be modelled as a normally distributed random variable, T , with a mean of zero and a standard deviation of four minutes. A graph of the probability distribution of T is shown below.



- a. If $\Pr(T \leq a) = 0.6$, find a to the nearest minute.

1 mark

- b. Find the probability, correct to three decimal places, of a delivery being no later than three minutes after its scheduled delivery time, given that it arrives after its scheduled delivery time.

2 marks

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- c. Using the model described on page 19, the transport company can make 46.48% of its deliveries over the interval $-3 \leq t \leq 2$.

It has an improved delivery model with a mean of k and a standard deviation of four minutes.

Find the values of k , correct to one decimal place, so that 46.48% of the transport company's deliveries can be made over the interval $-4.5 \leq t \leq 0.5$

3 marks

A rival transport company claims that there is a 0.85 probability that each delivery it makes will arrive on time or earlier.

Assume that whether each delivery is on time or earlier is independent of other deliveries.

- d. Assuming that the rival company's claim is true, find the probability that on a day in which the rival company makes eight deliveries, fewer than half of them arrive on time or earlier. Give your answer correct to three decimal places.

2 marks

- e. Assuming that the rival company's claim is true, consider a day in which it makes n deliveries.

- i. Express, in terms of n , the probability that one or more deliveries will **not** arrive on time or earlier.

1 mark

- ii. Hence, or otherwise, find the minimum value of n such that there is at least a 0.95 probability that one or more deliveries will **not** arrive on time or earlier.

1 mark

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- f. An analyst from a government department believes the rival transport company's claim is only true for deliveries made before 4 pm. For deliveries made after 4 pm, the analyst believes the probability of a delivery arriving on time or earlier is x , where $0.3 \leq x \leq 0.7$

After observing a large number of the rival transport company's deliveries, the analyst believes that the overall probability that a delivery arrives on time or earlier is actually 0.75

Let the probability that a delivery is made after 4 pm be y .

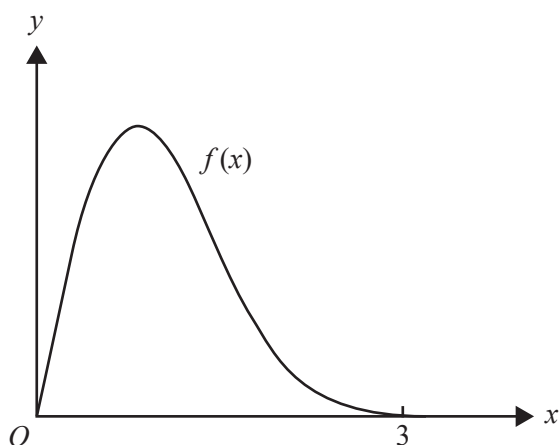
Assuming that the analyst's beliefs are true, find the minimum and maximum values of y .

2 marks

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Question 4 (13 marks)

The graph of the function $f(x) = 2xe^{(1-x^2)}$, where $0 \leq x \leq 3$, is shown below.



- a. Find the slope of the tangent to f at $x = 1$. 1 mark

- b. Find the obtuse angle that the tangent to f at $x = 1$ makes with the positive direction of the horizontal axis. Give your answer correct to the nearest degree. 1 mark

- c. Find the slope of the tangent to f at a point $x = p$. Give your answer in terms of p . 1 mark

- d. i. Find the value of p for which the tangent to f at $x = 1$ and the tangent to f at $x = p$ are perpendicular to each other. Give your answer correct to three decimal places.

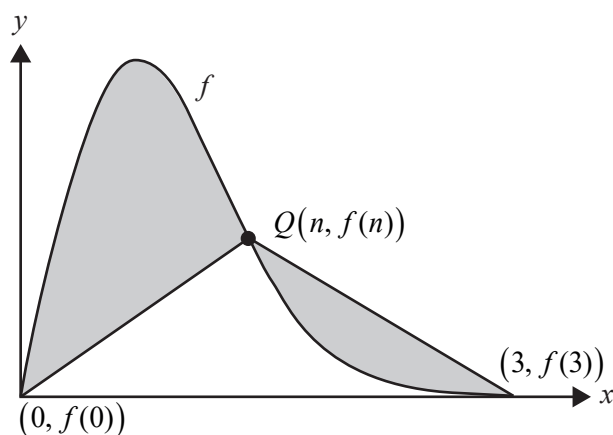
2 marks

- ii. Hence, find the coordinates of the point where the tangents to the graph of f at $x = 1$ and $x = p$ intersect when they are perpendicular. Give your answer correct to two decimal places.

3 marks

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Two line segments connect the points $(0, f(0))$ and $(3, f(3))$ to a single point $Q(n, f(n))$, where $1 < n < 3$, as shown in the graph below.



- e. i. The first line segment connects the point $(0, f(0))$ and the point $Q(n, f(n))$, where $1 < n < 3$.

Find the equation of this line segment in terms of n .

1 mark

- ii. The second line segment connects the point $Q(n, f(n))$ and the point $(3, f(3))$, where $1 < n < 3$.

Find the equation of this line segment in terms of n .

1 mark

- iii. Find the value of n , where $1 < n < 3$, if there are equal areas between the function f and each line segment. Give your answer correct to three decimal places.

3 marks

Question 5 (13 marks)

Let $f: R \rightarrow R$, $f(x) = x^3 - x$.

Let $g_a: R \rightarrow R$ be the function representing the tangent to the graph of f at $x = a$, where $a \in R$.

Let $(b, 0)$ be the x -intercept of the graph of g_a .

- a. Show that $b = \frac{2a^3}{3a^2 - 1}$. 3 marks

- b. State the values of a for which b does not exist. 1 mark

- c. State the nature of the graph of g_a when b does not exist. 1 mark

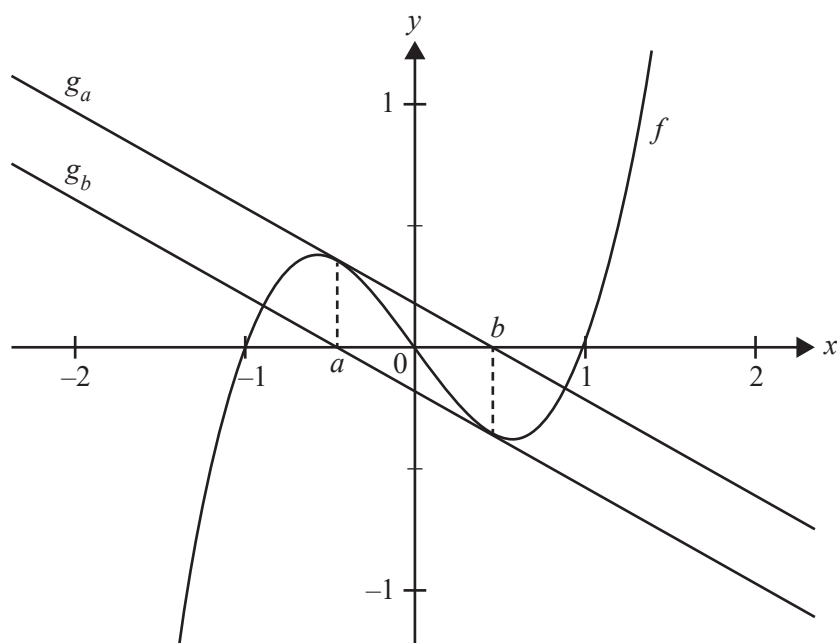
- d. i. State all values of a for which $b = 1.1$. Give your answers correct to four decimal places. 1 mark

- ii. The graph of f has an x -intercept at $(1, 0)$.

State the values of a for which $1 \leq b < 1.1$. Give your answers correct to three decimal places. 1 mark

The coordinate $(b, 0)$ is the horizontal axis intercept of g_a .

Let g_b be the function representing the tangent to the graph of f at $x = b$, as shown in the graph below.



- e. Find the values of a for which the graphs of g_a and g_b , where b exists, are parallel and where $b \neq a$. 3 marks

Let $p : \mathbb{R} \rightarrow \mathbb{R}, p(x) = x^3 + wx$, where $w \in \mathbb{R}$.

- f. Show that $p(-x) = -p(x)$ for all $w \in \mathbb{R}$. 1 mark

A property of the graphs of p is that two distinct parallel tangents will always occur at $(t, p(t))$ and $(-t, p(-t))$ for all $t \neq 0$.

- g. Find all values of w such that a tangent to the graph of p at $(t, p(t))$, for some $t > 0$, will have an x -intercept at $(-t, 0)$.

1 mark

- h. Let $T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$, $T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} m & 0 \\ 0 & n \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} h \\ k \end{bmatrix}$, where $m, n \in \mathbb{R} \setminus \{0\}$ and $h, k \in \mathbb{R}$.

State any restrictions on the values of m, n, h and k , given that the image of p under the transformation T always has the property that parallel tangents occur at $x = -t$ and $x = t$ for **all** $t \neq 0$.

1 mark

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MATHEMATICAL METHODS

Written examination 2

FORMULA SHEET

Instructions

This formula sheet is provided for your reference.
A question and answer book is provided with this formula sheet.

Students are NOT permitted to bring mobile phones and/or any other unauthorised electronic devices into the examination room.

Mathematical Methods formulas

Mensuration

area of a trapezium	$\frac{1}{2}(a+b)h$	volume of a pyramid	$\frac{1}{3}Ah$
curved surface area of a cylinder	$2\pi rh$	volume of a sphere	$\frac{4}{3}\pi r^3$
volume of a cylinder	$\pi r^2 h$	area of a triangle	$\frac{1}{2}bc \sin(A)$
volume of a cone	$\frac{1}{3}\pi r^2 h$		

Calculus

$\frac{d}{dx}(x^n) = nx^{n-1}$	$\int x^n dx = \frac{1}{n+1} x^{n+1} + c, n \neq -1$		
$\frac{d}{dx}((ax+b)^n) = an(ax+b)^{n-1}$	$\int (ax+b)^n dx = \frac{1}{a(n+1)}(ax+b)^{n+1} + c, n \neq -1$		
$\frac{d}{dx}(e^{ax}) = ae^{ax}$	$\int e^{ax} dx = \frac{1}{a} e^{ax} + c$		
$\frac{d}{dx}(\log_e(x)) = \frac{1}{x}$	$\int \frac{1}{x} dx = \log_e(x) + c, x > 0$		
$\frac{d}{dx}(\sin(ax)) = a \cos(ax)$	$\int \sin(ax) dx = -\frac{1}{a} \cos(ax) + c$		
$\frac{d}{dx}(\cos(ax)) = -a \sin(ax)$	$\int \cos(ax) dx = \frac{1}{a} \sin(ax) + c$		
$\frac{d}{dx}(\tan(ax)) = \frac{a}{\cos^2(ax)} = a \sec^2(ax)$			
product rule	$\frac{d}{dx}(uv) = u \frac{dv}{dx} + v \frac{du}{dx}$	quotient rule	$\frac{d}{dx}\left(\frac{u}{v}\right) = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$
chain rule	$\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}$		

Probability

$\Pr(A) = 1 - \Pr(A')$	$\Pr(A \cup B) = \Pr(A) + \Pr(B) - \Pr(A \cap B)$
$\Pr(A B) = \frac{\Pr(A \cap B)}{\Pr(B)}$	

Probability distribution		Mean	Variance
Bernoulli	$\Pr(X = x) = \begin{cases} p & x = 1 \\ 1 - p & x = 0 \end{cases}$	$\mu = p$	$\sigma^2 = p(1 - p)$
binomial	$\Pr(X = x) = \binom{n}{x} p^x (1 - p)^{n-x}$	$\mu = np$	$\sigma^2 = np(1 - p)$
normal	$\Pr(X \leq a) = \int_{-\infty}^a \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2} dx$	μ	σ^2