

# Test 3

Section A: Technology free. 41 marks  
Section B: CAS technology assumed. 39 marks  
Suggested time: 90 minutes

## Section A: Short answer and extended response questions. Technology free.

### Specific instructions to students

- Answer **all** questions in the spaces provided.
- A decimal approximation will not be accepted if an **exact** answer is required to a question.
- In questions where more than one mark is available, appropriate working **must** be shown.

### QUESTION 1

3 marks

Find matrix  $A$ , given

$$2A - 3 \begin{bmatrix} 1 & 4 \\ -2 & 3 \end{bmatrix} = \begin{bmatrix} 5 & 1 \\ 1 & 5 \end{bmatrix}.$$

Matrix  $A$  has a  $2 \times 2$  degree.

$$2A - \begin{bmatrix} 3 & 12 \\ -6 & 9 \end{bmatrix} = \begin{bmatrix} 5 & 1 \\ 1 & 5 \end{bmatrix}$$

$$2A = \begin{bmatrix} 5 & 1 \\ 1 & 5 \end{bmatrix} + \begin{bmatrix} 3 & 12 \\ -6 & 9 \end{bmatrix}$$

$$= \begin{bmatrix} 8 & 13 \\ -5 & 14 \end{bmatrix}$$

$$A = \frac{1}{2} \begin{bmatrix} 8 & 13 \\ -5 & 14 \end{bmatrix}$$

$$= \begin{bmatrix} 4 & \frac{13}{2} \\ -\frac{5}{2} & 7 \end{bmatrix}$$

### QUESTION 2

3 marks

Let  $A = \begin{bmatrix} a & 1 \\ b & 3 \end{bmatrix}$ ,  $B = \begin{bmatrix} a^2 + 1 & b \\ 2a + b & -3 \end{bmatrix}$  and  $C = \begin{bmatrix} 3 & 2 \\ h & k \end{bmatrix}$ .

If  $A + B = C$ , find  $a$ ,  $b$ ,  $h$  and  $k$ .

$$\text{LHS: } A + B = \begin{bmatrix} a^2 + a + 1 & b + 1 \\ 2a + 2b & 0 \end{bmatrix}$$

Equate components

$$a^2 + a + 1 = 3$$

$$a^2 + a - 2 = 0$$

$$(a + 2)(a - 1) = 0$$

$$a = -2, 1$$

$$b + 1 = 2$$

$$b = 1$$

$$2a + 2b = h$$

$$\text{when } a = -2 \text{ and } b = 1, h = -2$$

$$\text{when } a = 1 \text{ and } b = 1, h = 4$$

$$k = 0$$

Two sets of solutions:  $a = -2, b = 1, h = -2, k = 0$   
and  $a = 1, b = 1, h = 4, k = 0$

### QUESTION 3

2 marks

If  $A = \begin{bmatrix} \frac{\sqrt{3}}{2} & -\frac{1}{2} \\ \frac{1}{2} & \frac{\sqrt{3}}{2} \end{bmatrix}$  and  $B = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$ , find  $AB$ . Write the

answer in the form  $a \begin{bmatrix} b & c \\ d & e \end{bmatrix}$ .

$$\begin{aligned} AB &= \begin{bmatrix} \frac{\sqrt{3}}{2} \times 0 + -\frac{1}{2} \times 1 & \frac{\sqrt{3}}{2} \times -1 + -\frac{1}{2} \times 0 \\ \frac{1}{2} \times 0 + \frac{\sqrt{3}}{2} \times 1 & \frac{1}{2} \times -1 + \frac{\sqrt{3}}{2} \times 0 \end{bmatrix} \\ &= \begin{bmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{bmatrix} \\ &= \frac{1}{2} \begin{bmatrix} 1 & -\sqrt{3} \\ \sqrt{3} & -1 \end{bmatrix} \end{aligned}$$

### QUESTION 4

Total 4 marks

a Find the determinant of  $A = \begin{bmatrix} 3 & 5 \\ 4 & 2 \end{bmatrix}$ .

1 mark

$$\begin{aligned} \text{The determinant is: } \Delta &= (3 \times 2 - 5 \times 4) \\ &= -14 \end{aligned}$$

b Find  $A^{-1}$ , the inverse of  $A$ .

1 mark

$$A^{-1} = -\frac{1}{14} \begin{bmatrix} 2 & -5 \\ -4 & 3 \end{bmatrix} \text{ or } \begin{bmatrix} -\frac{1}{7} & \frac{5}{14} \\ \frac{2}{7} & -\frac{3}{14} \end{bmatrix}$$

c Find  $X$  if  $AX = B$ , where  $B = \begin{bmatrix} -2 \\ 1 \end{bmatrix}$ .

2 marks

The degree of  $X$  is  $(2 \times 1)$ .

$$X = A^{-1} B$$

$$= -\frac{1}{14} \begin{bmatrix} 2 & -5 \\ -4 & 3 \end{bmatrix} \times \begin{bmatrix} -2 \\ 1 \end{bmatrix}$$

$$= -\frac{1}{14} \begin{bmatrix} 2 \times -2 + -5 \times 1 \\ -4 \times -2 + 3 \times 1 \end{bmatrix}$$

$$= -\frac{1}{14} \begin{bmatrix} -9 \\ 11 \end{bmatrix} \text{ or } \begin{bmatrix} \frac{9}{14} \\ -\frac{11}{14} \end{bmatrix}$$

**QUESTION 5**

Total 3 marks

- a** Set up a matrix equation to solve the pair of simultaneous equations  $2x - y = 7$  and  $3y - 5x = -19$ .

1 mark

$$\begin{bmatrix} 2 & -1 \\ -5 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 7 \\ -19 \end{bmatrix}$$

- b** Solve the matrix equation to find the solution set.

2 marks

The inverse of  $\begin{bmatrix} 2 & -1 \\ -5 & 3 \end{bmatrix}$  is  $\begin{bmatrix} 3 & 1 \\ 5 & 2 \end{bmatrix}$ .

Solution:  $\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 3 & 1 \\ 5 & 2 \end{bmatrix} \begin{bmatrix} 7 \\ -19 \end{bmatrix}$

$$= \begin{bmatrix} 2 \\ -3 \end{bmatrix}$$

**QUESTION 6**

Total 3 marks

- a** Write the following transformations in matrix form: A dilation of 3 from the  $x$  axis followed by a reflection in the line  $y = x$  followed by a translation of 4 in the  $x$  direction and  $-3$  in the  $y$  direction.

2 marks

$$\begin{bmatrix} 4 \\ -3 \end{bmatrix} + \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} \text{ or } \begin{bmatrix} 3y + 4 \\ x - 3 \end{bmatrix}$$

- b** Hence, find the image of the point  $(3, -2)$  under these transformations.

1 mark

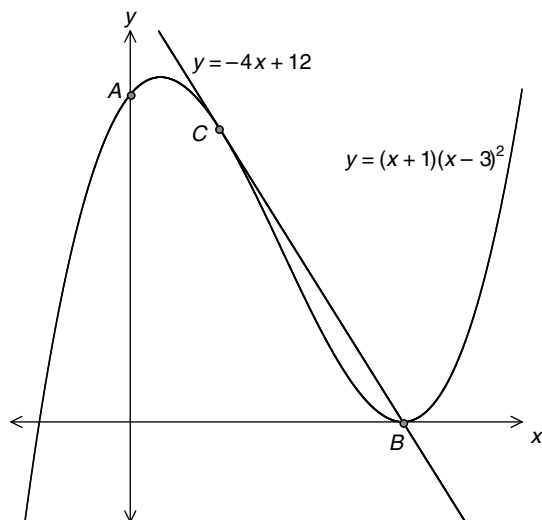
$$\begin{bmatrix} 4 \\ -3 \end{bmatrix} + \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 3 \end{bmatrix} \begin{bmatrix} 3 \\ -2 \end{bmatrix} \text{ or } \begin{bmatrix} 3 \times -2 + 4 \\ 3 - 3 \end{bmatrix}$$

$$= \begin{bmatrix} -2 \\ 0 \end{bmatrix} = \begin{bmatrix} -2 \\ 0 \end{bmatrix}$$

**QUESTION 7**

Total 7 marks

The graph of  $y = (x + 1)(x - 3)^2$  is shown.



- a** State the coordinates of the points  $A$  and  $B$ . 2 marks

Point  $A$ :  $y$  intercept

$$(x = 0), y = 1 \times (-3)^2 = 9$$

Point  $B$ :  $x$  intercept

$$(y = 0), (x + 1)(x - 3)^2 = 0$$

$$x = -1, 3$$

Since  $B > 0$ ,  $B = 3$

- b** Hence, find the average rate of change of  $y$  with respect to  $x$  from  $A$  to  $B$ . 2 marks

Average rate of change:

$$\frac{0 - 9}{3 - 0} = \frac{-9}{3} = -3$$

The tangent to the curve at  $C$ , where  $x = 1$ , also passes through the point  $B$ .

- c** Show that the equation to the tangent at  $C$  is  $y = -4x + 12$ . 2 marks

Coordinates of  $C$ :

$$y = (1 + 1)(1 - 3)^2 = 8$$

Gradient of line joining  $B$  and  $C$ :

$$\frac{8 - 0}{1 - 3} = -4$$

Equation of line passing through  $B$  and  $C$ :

$$y = -4x + c$$

$$(3, 0): 0 = -4 \times 3 + c$$

$$c = 12$$

$$y = -4x + 12$$

- d** Hence, state the instantaneous rate of change of  $y$  with respect to  $x$  of the curve at  $C$ . 1 mark

The instantaneous rate of change of  $y$  with respect to  $x$  at  $C$  is the gradient of the tangent to the curve at  $C = -4$ .

**QUESTION 8**

Total 4 marks

The temperature ( $T^\circ\text{C}$ ) of a cup of coffee at time  $t$  minutes after the coffee is made is modelled by the formula:  $T(t) = \frac{1050}{4t + 15} + 20$ ,  $0 \leq t \leq 20$ .

- a** Find the temperature of the coffee when it is first made. 1 mark

$$\text{When it is first made } t = 0, T = \frac{1050}{15} + 20$$

$$= 90^\circ\text{C}$$

- b** Find the temperature of the coffee 5 minutes after it was made. 1 mark

$$t = 5, T = \frac{1050}{35} + 20$$

$$= 50^\circ\text{C}$$

- c Find the average rate of change of the temperature of the coffee from when it was first made until 5 minutes later. **2 marks**

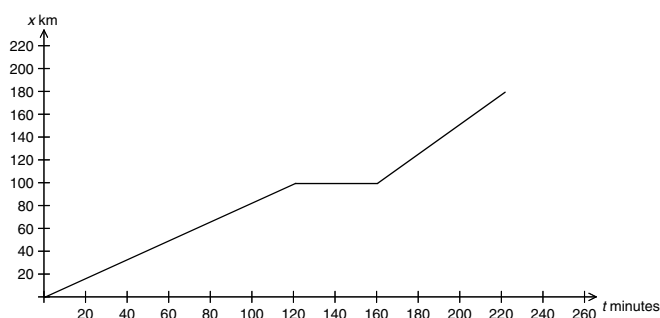
$$\begin{aligned}\text{Average rate of change: } \frac{50 - 90}{5 - 0} \\ &= \frac{-40}{5} \\ &= -8^\circ\text{C/minute.}\end{aligned}$$

### QUESTION 9

**Total 6 marks**

A family going on a holiday drives 100 km in 120 minutes. They stop for 40 minutes before resuming their journey, then travel a further 80 km in 60 minutes.

- a On the axes provided, draw a displacement-time graph representing their journey. Label the axes appropriately. **3 marks**



- b Find the average speed for the journey in km/minute, to the nearest whole number. **2 marks**

$$\begin{aligned}\text{Average speed: } \frac{\text{distance travelled}}{\text{time taken}} \\ &= \frac{100 + 80}{120 + 40 + 60} \\ &= \frac{180}{220} \\ &= \frac{9}{11} \text{ km/minute}\end{aligned}$$

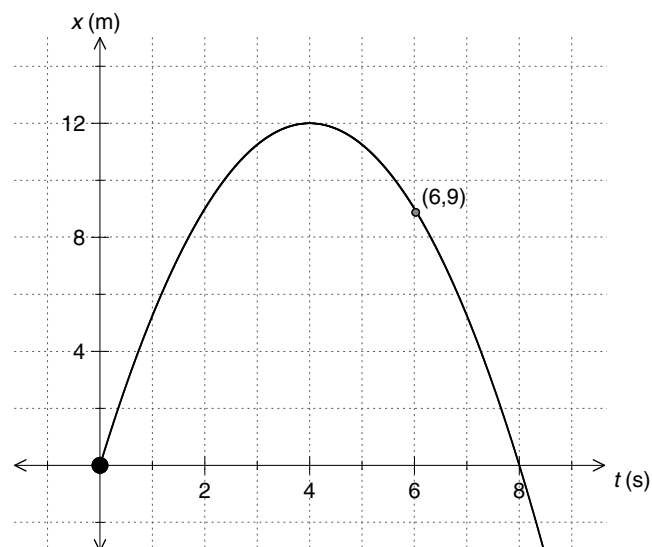
- c If the return journey took 3 hours and there were no stops, what was the average speed for the return journey, in km/hour? **1 mark**

$$\begin{aligned}\text{Average speed: } \frac{180}{3} \\ &= 90 \text{ km/hr}\end{aligned}$$

### QUESTION 10

**Total 6 marks**

The diagram shows the displacement-time graph of a particle moving along a horizontal straight line. The equation of the graph is  $x(t) = ax(x - 8)$ .



- a Show that the value of  $a$  is  $-\frac{3}{4}$ . **1 mark**

$$\begin{aligned}(6, 9): 9 &= 6a(6 - 8) \\ a &= \frac{9}{6} \times -\frac{1}{2} \\ &= -\frac{3}{4}\end{aligned}$$

- b At what time is the velocity zero? What is the displacement at this time? **2 marks**

From the graph, velocity is zero when  $t = 4$  s; displacement is 12 m.

- c What is the maximum displacement of the particle for  $0 \leq t \leq 8$ ? **1 mark**

Maximum displacement is 12 m.

- d Over which values of  $t$  is the velocity positive? **2 marks**

The velocity is positive when  $0 < t < 4$ .

## Section B: Multiple-choice questions. CAS technology assumed.

### Specific instructions to students

- A correct answer scores 1, and an incorrect answer scores 0.
- Marks are not deducted for incorrect answers.
- No marks are given if more than one answer is given.
- Choose the alternative which most correctly answers the question and mark your choice on the multiple-choice answer section at the bottom of each page, as shown in the example below.

1 ☐ A ☐ B ☐ C ☒ D ☐ E



- Use pencil only.

### QUESTION 11

If  $P = \begin{bmatrix} -2 & 1 & 3 \end{bmatrix}$  and  $Q = \begin{bmatrix} -1 \\ 0 \\ 4 \end{bmatrix}$ , then the product,  $PQ$  is:

**A**  $\begin{bmatrix} 2 & 0 & 12 \end{bmatrix}$

**B**  $\begin{bmatrix} 2 \\ 0 \\ 12 \end{bmatrix}$

**C**  $\begin{bmatrix} 2 & -1 & -3 \\ 0 & 0 & 0 \\ -8 & 4 & 12 \end{bmatrix}$

**D**  $[14]$

**E** not defined

### QUESTION 12

Let  $A = \begin{bmatrix} 4 & -3 \\ 5 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ . The dimension of  $AB$  is:

**A**  $2 \times 2$

**B**  $2 \times 3$

**C**  $3 \times 2$

**D**  $2 \times 1$

**E** not defined

### QUESTION 13

The matrix equation to solve the simultaneous equations

$$x + 2y + z = 1$$

$$2x - 3y + z = -1$$

$$-x + y = 3$$

is:

**A**  $\begin{bmatrix} 1 & 2 & 1 \\ 2 & -3 & 1 \\ -1 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \\ 3 \end{bmatrix}$

**B**  $\begin{bmatrix} 1 & 2 & 1 \\ 2 & -3 & 1 \\ -1 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \\ 3 \end{bmatrix}$

**C**  $\begin{bmatrix} x & y & z \end{bmatrix} \begin{bmatrix} 1 & 2 & 1 \\ 2 & -3 & 1 \\ -1 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & -1 & 3 \end{bmatrix}$

**D**  $\begin{bmatrix} x & y & z \end{bmatrix} \begin{bmatrix} 1 & 2 & 1 \\ 2 & -3 & 1 \\ -1 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \\ 3 \end{bmatrix}$

**E**  $\begin{bmatrix} 1 & 2 & -1 \\ 2 & -3 & 1 \\ 1 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 & -1 & 3 \end{bmatrix}$

### QUESTION 14

The average rate of change of  $y$  with respect to  $x$  for  $y = f(x)$  from  $x = 3$  to  $x = 3 + h$  can be found by evaluating:

**A**  $\frac{f(3)}{3}$

**B**  $\frac{f(x+h) - f(x)}{h}$

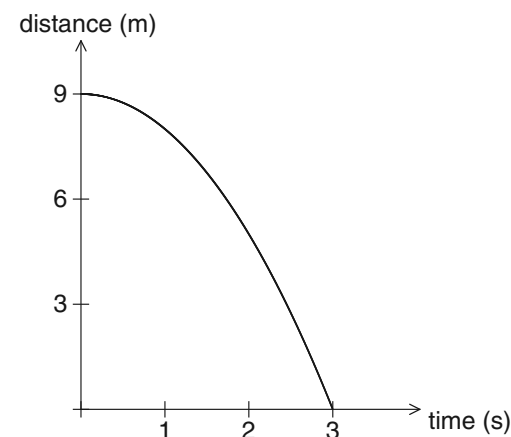
**C**  $\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$

**D**  $\lim_{h \rightarrow 0} \frac{f(3+h) - f(3)}{h}$

**E**  $\frac{f(3+h) - f(3)}{h}$

### QUESTION 15

The average speed from  $t = 0$  to  $t = 3$  for the displacement-time graph shown is:



**A**  $\frac{1}{3}$  m/s

**B**  $-\frac{1}{3}$  m/s

**C**  $-6$  m/s

**D**  $-3$  m/s

**E**  $3$  m/s

ONE ANSWER PER LINE

USE PENCIL ONLY

11 ☐ A ☐ B ☐ C ☒ D ☐ E

12 ☐ A ☒ B ☐ C ☐ D ☐ E

13 ☐ A ☒ B ☐ C ☐ D ☐ E

14 ☐ A ☐ B ☐ C ☐ D ☒ E

15 ☐ A ☐ B ☐ C ☒ D ☐ E

## Section B: Extended response questions. CAS technology assumed.

### Specific instructions to students

- Answer **all** questions in the spaces provided.
- In questions where more than one mark is available, appropriate working **must** be shown.

### QUESTION 16

Total 8 marks

The hyperbola  $y = 1 + \frac{1}{k+x}$  crosses the  $x$  axis at the point  $A$  and the  $y$  axis at the point  $B$ .

- a Express the coordinates of  $A$  and of  $B$  in terms of  $k$ . 2 marks

$$y \text{ intercept } (x = 0) \quad y = 1 + \frac{1}{k}$$

$$\text{Using CAS: } x \text{ intercept: solve } 1 + \frac{1}{k+x} = 0 \text{ for } x$$

$$x = -k - 1$$

$$\text{Coordinates are: } A = (-k - 1, 0) \text{ and } B = \left(0, 1 + \frac{1}{k}\right).$$

- b Write an expression to find the gradient of the line joining  $A$  and  $B$ . Write the expression for the gradient in simplest form. 2 marks

$$m = \frac{\left(1 + \frac{1}{k}\right) - 0}{0 - (-k - 1)}$$

$$\text{Using CAS: } m = \frac{1}{k}$$

- c Write the equation of the line joining  $A$  and  $B$ . 1 mark

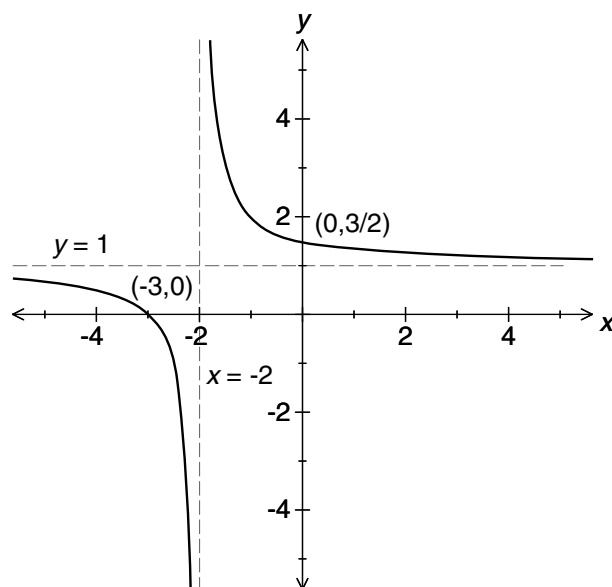
$$y = \frac{1}{k}x + 1 + \frac{1}{k}$$

- d On the axes provided, sketch the graph of the hyperbola when  $k = 2$ . Label any asymptotes and  $x$  and  $y$  intercepts. 3 marks

$k = 2$ :  $y = 1 + \frac{1}{x+2}$ . This hyperbola has a vertical asymptote at  $x = -2$  and a horizontal asymptote at  $y = 1$ .

$$y \text{ intercept is } 1 + \frac{1}{2} = \frac{3}{2}$$

$$x \text{ intercept is } -2 - 1 = -3$$



### QUESTION 17

Total 9 marks

The general equation of a quartic polynomial that passes through the origin is given by  $y = ax^4 + bx^3 + cx^2 + dx$ . A particular quartic polynomial that passes through the origin also passes through the points  $(-2, 15)$ ,  $(-1, 2)$ ,  $(1, -3)$  and  $(2, -7)$ .

- a Write four simultaneous equations using  $a, b, c$  and  $d$ . 2 marks

$$16a - 8b + 4c - 2d = 15$$

$$a - b + c - d = 2$$

$$a + b + c + d = -3$$

$$16a + 8b + 4c + 2d = -7$$

- b Rewrite these equations as a matrix equation. 1 mark

$$\begin{bmatrix} 16 & -8 & 4 & -2 \\ 1 & -1 & 1 & -1 \\ 1 & 1 & 1 & 1 \\ 16 & 8 & 4 & 2 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} 15 \\ 2 \\ -3 \\ -7 \end{bmatrix}$$

- c Find the values of  $a, b, c$  and  $d$ . Hence, write the equation of the particular quartic polynomial. 2 marks

CAS: Either use SOLVE with equations or solve the matrix equation.

$$a = \frac{1}{2}, b = -1, c = -1, d = -\frac{3}{2}$$

$$\text{Quartic equation: } y = \frac{1}{2}x^4 - x^3 - x^2 - \frac{3}{2}x$$

- d Find the coordinates of the minimum point to two decimal places. 2 marks

From the graph:  $(2.13, -7.10)$ .

- e State the range of  $f: [0, 3] \rightarrow \mathbb{R}$ ,  $f(x) = \frac{1}{2}x^4 - x^3 - x^2 - \frac{3}{2}x$  to two decimal places. 2 marks

From the graph, the range is  $[-7.10, 0]$ .

**QUESTION 18****Total 10 marks**

The combined water storage levels of all dams for a certain Australian city for 2007 can be modelled by the function

$$P(t) = \begin{cases} 40.527 - 2.0743t & 0 \leq t \leq 6 \\ -0.0194t^3 + 0.0369t^2 + 6.0897t - 5.2976 & 6 < t < 13, \end{cases}$$

where  $P(t)$  is the percentage of total capacity of water stored in all dams  $t$  months after 1 January 2007. ( $t = 0$  is 1 January 2007,  $t = 1$  is 1 February 2007.)

- a** What percentage of water is stored in all dams when  $t = 0$  and  $t = 9$ ? Give answers correct to one decimal place. **2 marks**

$t = 0$ :

$$P(0) = 40.527 - 2.0743 \times 0 \\ = 40.5\%$$

$t = 9$ :

$$P(9) = -0.0194 \times 9^3 + 0.0369 \times 9^2 \\ + 6.0897 \times 9 - 5.2976 \\ = 38.4\%$$

- b** Find the average rate of change of the percentage of stored water from  $t = 0$  to  $t = 6$ , and from  $t = 7$  to  $t = 12$ . Give a brief description of the significance of these results. **5 marks**

Average rate of change:

$t = 0$  to  $t = 6$ :

Over the domain  $0 \leq t \leq 6$  the gradient of the linear function gives the average rate of change, which is a constant value of  $-2.0743$ . To one decimal place:  $-2.1\%$  per month.

$t = 7$  to  $t = 12$ :

$$\frac{P(12) - P(7)}{12 - 7} = \frac{39.569 - 32.484}{5} \\ = 1.4\% \text{ per month}$$

Over the first 6 months the storage level dropped at a constant rate of  $2.1\%$  of full capacity per month. During the 5 months from the start of July to December, the storage level rose by an average of  $1.4\%$  of full capacity per month.

- c** The following table gives the percentage storage levels for several months of the second half of 2007.

$t$	7	10	12
$P$	31.9	39.9	39.7

It was thought that a quadratic polynomial of the form  $P(t) = at^2 + bt + c$  could give a more accurate model over these months.

- i** Find the values of  $a$ ,  $b$  and  $c$ , correct to three decimal places. **2 marks**

Use CAS to solve the simultaneous equations:

$$49a + 7b + c = 31.9$$

$$100a + 10b + c = 39.9$$

$$144a + 12b + c = 39.7$$

Or solve  $f(7) = 31.9$  and  $f(10) = 39.9$  and  $f(12) = 39.7$  for  $a$ ,  $b$  and  $c$ .

$$a = -0.553, b = 12.073, c = -25.5$$

The quadratic function is:

$$P(t) = -0.553t^2 + 12.073t - 25.5$$

- ii** Using this quadratic function, find the value for  $t$ , to the nearest whole number, when the water storage was a maximum. **1 mark**

CAS: Find the maximum value from the table of values or the graph.  $\therefore t = 11$

**QUESTION 19****Total 7 marks**

$$P = \begin{bmatrix} a & 0 \\ b & 1 \end{bmatrix} \text{ and } P^{-1} = \begin{bmatrix} u & 0 \\ v & 1 \end{bmatrix}$$

- a** By equating  $P \times P^{-1} = I$ , find  $u$  and  $v$  in terms of  $a$  and  $b$ . **4 marks**

$$P \times P^{-1} = \begin{bmatrix} a & 0 \\ b & 1 \end{bmatrix} \times \begin{bmatrix} u & 0 \\ v & 1 \end{bmatrix}$$

$$\text{LHS} = \begin{bmatrix} a \times u + 0 \times v & a \times 0 + 0 \times 1 \\ b \times u + 1 \times v & b \times 0 + 1 \times 1 \end{bmatrix} \\ = \begin{bmatrix} au & 0 \\ bu + v & 1 \end{bmatrix}$$

Equate components:

$$au = 1 \Rightarrow u = \frac{1}{a}$$

$$bu + v = 0$$

$$v = -bu$$

$$v = -\frac{b}{a}$$

- b** If  $a = 3$  and  $b = 4$ , write  $P^{-1}$  in the form  $\frac{1}{3} \begin{bmatrix} m & n \\ q & r \end{bmatrix}$ . State the values of  $m$ ,  $n$ ,  $q$  and  $r$ . **3 marks**

$$P^{-1} = \begin{bmatrix} \frac{1}{3} & 0 \\ -\frac{4}{3} & 1 \end{bmatrix} \\ = \frac{1}{3} \begin{bmatrix} 1 & 0 \\ -4 & 3 \end{bmatrix}$$

Thus  $m = 1$ ,  $n = 0$ ,  $q = -4$  and  $r = 3$ .