

**FURTHER MATHEMATICS
TRIAL EXAMINATION 2
SOLUTIONS
2007**

SECTION A — solutions

Core

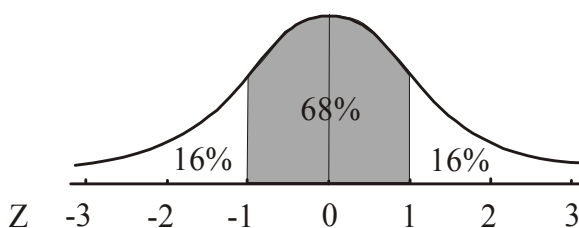
Question 1

- a. Standard deviation for 5B = 6.5 (correct to one decimal place) (1 mark)

- b. The distribution of results of 5A and 5B both have
- a shape that is approximately symmetric (1 mark)
- similar centres. (1 mark)

- c.
$$z = \frac{x - \bar{x}}{s}$$
$$= \frac{28 - 19.9}{9.3}$$
$$= 0.9 \text{ (correct to 1 decimal place)}$$
 (1 mark)

- d.

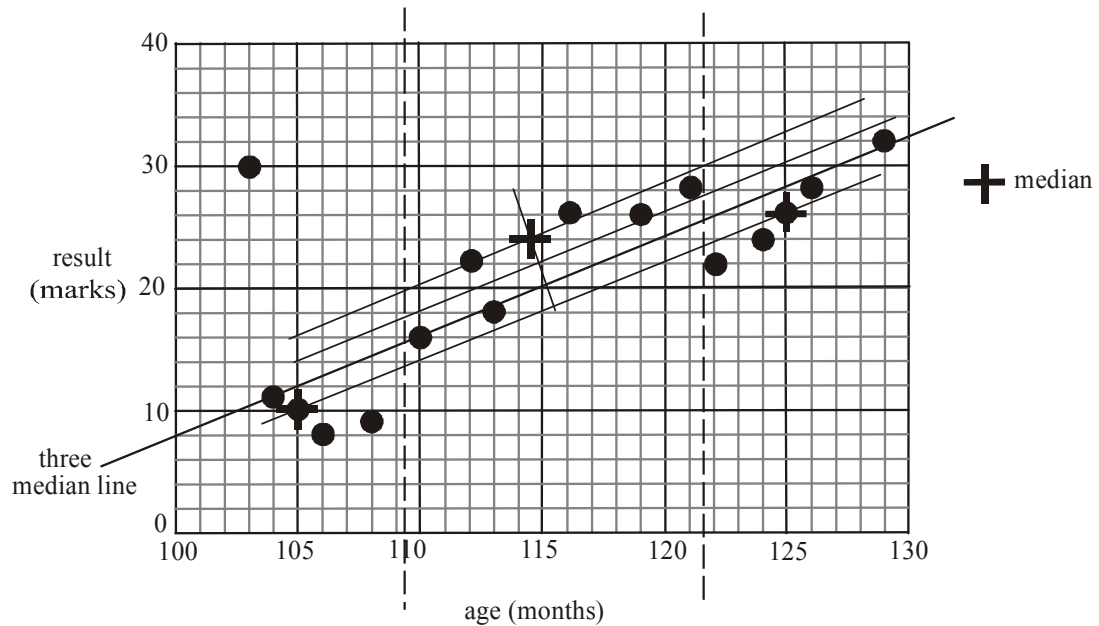


Since Lucy's z-score was -1 , we see from the diagram that 16% of students scored less than Lucy so 84% scored a higher result than Lucy.

(1 mark)

Question 2

a.



Divide the 16 points into 3 groups so that there are 5 in each of the outer groups and 6 in the middle group. The dotted lines indicate this grouping. Find the median in each of the 3 groups. The medians are located at (105, 10), (114.5, 24) and (125, 26). Place a ruler over the outer 2 medians and move it one third of the way towards the median in the centre group. This is the 3-median line.

(1 mark) correct medians

(1 mark) correct line shown

b. Choose a section of any of the lines shown (since they are parallel) and find the rise and the run.

For example between the two outside medians (105,10) and (125,26) which lie on the line, the rise is 16 and the run is 20. The gradient is $\frac{16}{20} = 0.8$.

(1 mark)

c. For every 1 month increase in age there is an increase of 0.8 in the result. (This is governed by the gradient of the line.)

(1 mark)

Question 3

- a.** It is appropriate to fit a least squares regression line to this data because the relationship between the variables age and result appears to be linear. **(1 mark)**
Secondly, there are no outliers in the data. **(1 mark)**

- b.** Using a calculator, we have

$$\text{result} = -191 \cdot 3 + 1 \cdot 6 \times \text{age}$$

where the coefficients are correct to one decimal place.

(1 mark) for - 191.3

(1 mark) for 1.6

- c. i.** Again from the calculator $r^2 = 0 \cdot 7830$ (correct to 4 decimal places) **(1 mark)**

- ii.** The coefficient of determinations tells us that 78.30% of the variation in the result can be accounted for by the variation in age. **(1 mark)**
(Clearly the remaining 21.7% has to be explained by factors other than age.)

Total 15 marks

SECTION B**Module 1: Number patterns****Question 1**

- a. $84 - 3 \times 14 = 42$ jars remained after 3 hours. (1 mark)
- b. $84 \div 14 = 6$ so Paula will run out of jam after 6 hours. (1 mark)
- c. The sequence is 84, 70, 56, 42,
This is an arithmetic sequence because the difference between each term is the same; that is, the difference is 14. (1 mark)
- d. $d = -14$ Note that the value is negative since each hour Paula has fewer jars left to sell. (1 mark)

Question 2

- a. $\frac{11}{10} = \frac{12 \cdot 1}{11} = 1 \cdot 1$ so the common ratio is $1 \cdot 1$. (1 mark)
- b. Using a calculator, the amount of chutney Paula makes for the ninth market is $10 \times 1.1^8 = 21.44$ kg (correct to 2 decimal places). (1 mark)
- c. $A_n = 10 \times (1 \cdot 1)^{n-1}$ (1 mark)
- d. Again using a calculator start by multiplying 10 by $1 \cdot 1$.
At the 13th market the amount of chutney produced first exceeded 30kg. (1 mark)
- e. The amount of chutney Paula makes in the first year in total is given by

$$S_{12} = \frac{10(1 \cdot 1^{12} - 1)}{1 \cdot 1 - 1}$$

$$= 213 \cdot 8428$$
The amount of chutney Paula makes in the first two years in total is given by

$$S_{24} = \frac{10(1 \cdot 1^{24} - 1)}{1 \cdot 1 - 1}$$

$$= 884 \cdot 9733$$
In the second year therefore Paula makes $884 \cdot 9732... - 213 \cdot 8428... = 671 \cdot 1304...$
So the difference between what she makes in the first year and what she makes in the second year is $671 \cdot 1304... - 213 \cdot 8428... = 457 \cdot 29$ kg (correct to 2 decimal places) . (1 mark)

Question 3

- a. Since Paula makes 15% more fudge than she had to sell at the previous market,
 $r = 1.15$. (1 mark)
 Since Paula keeps 200g of the fudge she makes for her family, $d = -200$. (1 mark)

- b. Using a calculator, generate the sequence. The first time the sequence exceeds 3kg;
 i.e. 3000g is for $n = 15$ where the amount made is 3220.2g.
 So at the 15th market that Paula attends, 3kg is exceeded. (1 mark)

- c. If Paula didn't keep 200g of the fudge for her family the difference equation would be

$$F_{n+1} = 1.15F_n \text{ where } F_1 = 1\,600 \text{ that is } d = 0.$$

This represents a geometric sequence.

(1 mark)

- d. The difference equation would be $F_{n+1} = F_n - 200$ where $F_1 = 1\,600$.
 This is an arithmetic sequence.
 The sequence is 1 600, 1 400, 1 200, 1 000, 800, 600, 400, 200, 0.
 So the ninth market would be the one where for the first time Paula had no fudge to sell.

(1 mark)

Total 15 marks

Module 2: Geometry and trigonometry

Question 1

- a. The lookout at L is on a contour at 1700m. The shelter at S is on a contour at 1550m. The difference in height is 150m.

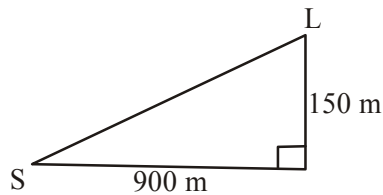
(1 mark)

- b. The contours to the north of the peak are the closest together and hence the land to the north of the peak is the steepest.

(1 mark)

- c. The average slope is given by

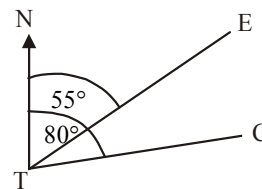
$$\frac{\text{rise}}{\text{run}} = \frac{150}{900} \\ = \frac{1}{6}$$



(1 mark)

Question 2

- a. The bearing of E from T is 055° .
The bearing of C from T is 080° ,
So the angle ETC equals $80^\circ - 55^\circ = 25^\circ$.



(1 mark)

- b. In $\triangle XET$,

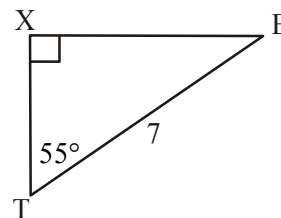
$$\cos(55^\circ) = \frac{TX}{ET}$$

$$\cos(55^\circ) = \frac{TX}{7}$$

$$TX = 7 \cos(55^\circ)$$

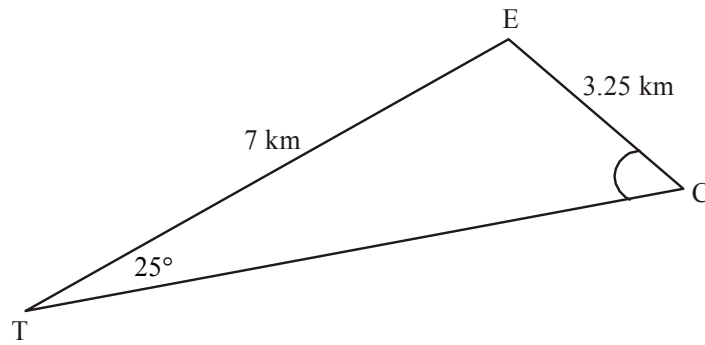
$$= 4.02 \text{ km}$$

(correct to 2 decimal places)



(1 mark)

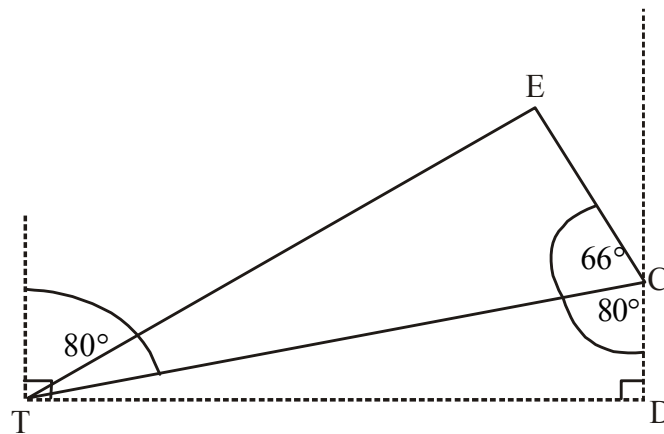
c.



$$\begin{aligned}\text{In } \triangle CET, \frac{\sin(\angle ECT)}{7} &= \frac{\sin(25^\circ)}{3.25} \text{ (sine rule)} \\ \sin(\angle ECT) &= \frac{7 \times \sin(25^\circ)}{3.25} \\ &= 0.91025... \\ \angle ECT &= 65.54...^\circ \\ &= 66^\circ \text{ (to the nearest degree)}\end{aligned}$$

(1 mark)

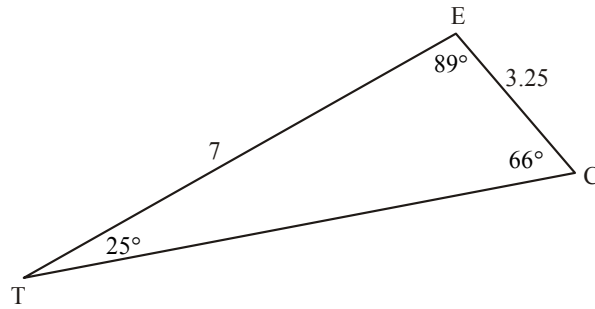
d.



$\angle DCT = 80^\circ$ (alternate angles in parallel lines are equal).
So the bearing of E from C is equal to $180^\circ + 80^\circ + 66^\circ = 326^\circ$.

(1 mark)

e.



In $\triangle CET$, $\angle CET = 180^\circ - 66^\circ - 25^\circ$
 $= 89^\circ$

(1 mark)

Method 1 - using the cosine rule

$$(CT)^2 = 7^2 + 3 \cdot 25^2 - 2 \times 7 \times 3 \cdot 25 \cos(89^\circ)$$

$$CT = 7 \cdot 66605\dots$$

$$= 7 \cdot 7 \text{ km (correct to 1 decimal place)}$$

Method 2 - using the sin rule

$$\frac{CT}{\sin(89^\circ)} = \frac{3 \cdot 25}{\sin(25^\circ)}$$

$$CT = 7 \cdot 7 \text{ km}$$

(correct to 1 decimal place)

(1 mark)

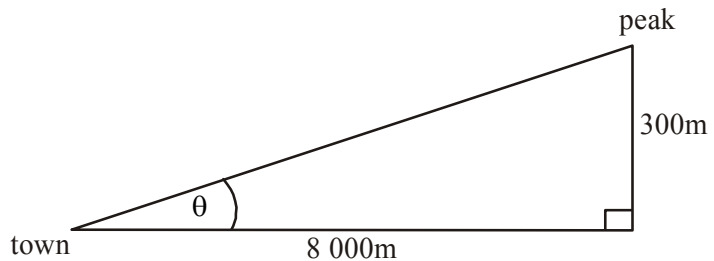
Question 3Let θ equal the angle of elevation.

$$\tan(\theta) = \frac{300}{8000}$$

$$\theta = 2 \cdot 1475\dots$$

$$= 2^\circ 9' \text{ (to the nearest minute)}$$

(1 mark)

**Question 4**

- a. surface area = $4 \times$ surface area of side of cube + $4 \times$ surface area of slant side of pyramid
 Now we can use Heron's formula to find the area of the slant side of a pyramid.

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

$$\text{where } s = \frac{1}{2}(a+b+c)$$

$$= \frac{1}{2}(3+3+2)$$

$$= 4$$

$$\text{So, } A = \sqrt{4(4-3)(4-3)(4-2)}$$

$$= \sqrt{8}$$

(1 mark)

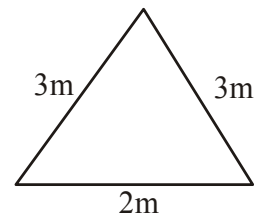
So total surface area

$$= 4 \times 2 \times 2 + 4 \times \sqrt{8}$$

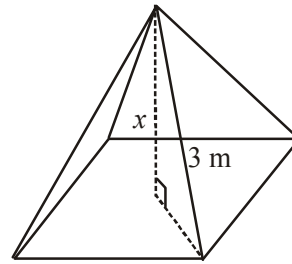
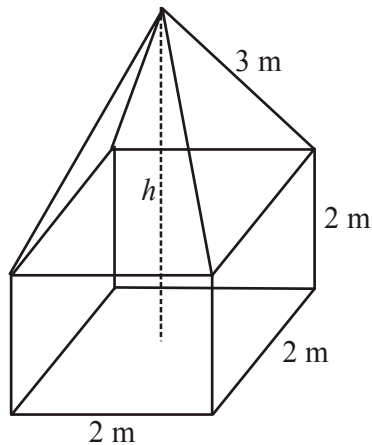
$$= 16 + 4\sqrt{8}$$

$$= 27 \cdot 3 \text{ m}^2 \text{ (correct to 2 decimal places)}$$

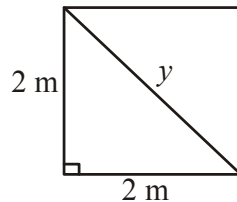
(1 mark)



- b. The height of the cube is 2m.



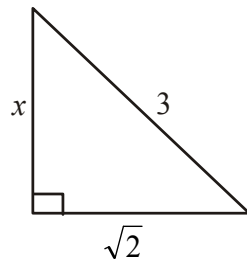
In the square pyramid, let the height be x . We know that the slant side is 3m. To find the length of the diagonal of the square base, use Pythagoras



$$\begin{aligned} y^2 &= 2^2 + 2^2 \\ y &= \sqrt{4 + 4} \\ &= \sqrt{8} \\ &= \sqrt{4 \times 2} \\ &= 2\sqrt{2} \end{aligned}$$

(1 mark)

So the length of half the diagonal of the square base is $\sqrt{2}$ m.



$$\begin{aligned} \text{So } x &= \sqrt{3^2 - (\sqrt{2})^2} \\ &= \sqrt{9 - 2} \\ &= \sqrt{7} \end{aligned}$$

The height of the pyramid is $\sqrt{7}$ m.

So the total height of the trig marker is $2 + \sqrt{7} = 4.65$ m (to 2 decimal places).

(1 mark)

- c. volume = volume of cube + volume of pyramid

$$= \text{length} \times \text{width} \times \text{height} + \frac{1}{3} \times \text{area of base} \times \text{height} \quad (\text{using formula sheet})$$

$$= 2 \times 2 \times 2 + \frac{1}{3} \times 2 \times 2 \times \sqrt{7} \quad (\text{from part b.})$$

$$= 8 + \frac{4\sqrt{7}}{3}$$

$$= 11.53 \text{ m}^3 \quad (\text{correct to 2 decimal places})$$

(1 mark)

Total 15 marks

Module 3: Graphs and relations.**Question 1**

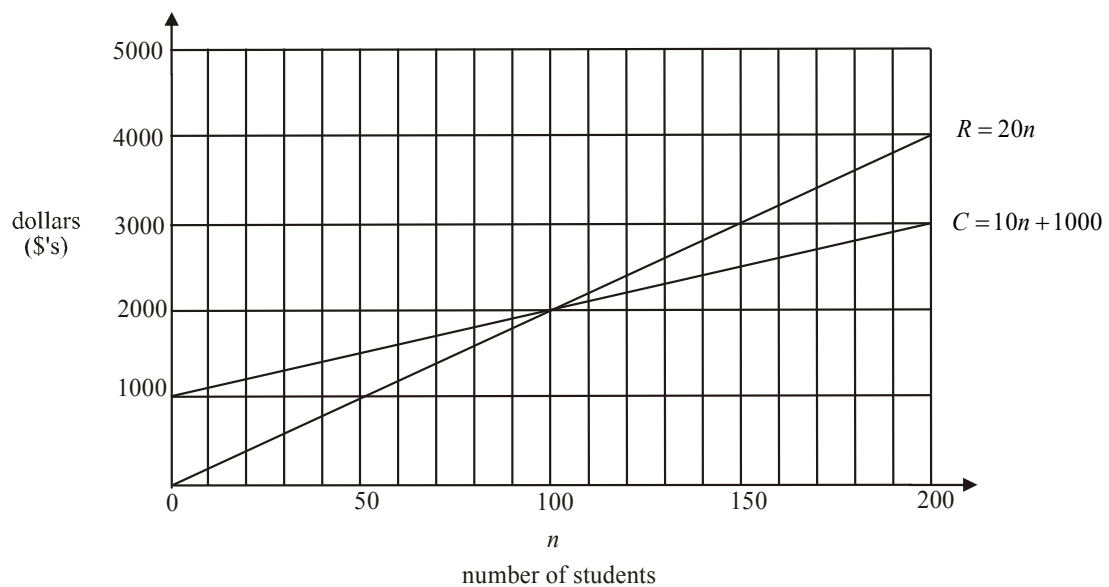
- a. The average weekly revenue received for each student who attends a class is given by the gradient of the revenue function.

$$\begin{aligned}\text{Now, gradient} &= \frac{\text{rise}}{\text{run}} \\ &= \frac{4\,000}{200} \\ &= 20\end{aligned}$$

The answer is \$20.

(1 mark)

- b.



(1 mark)

- c. Method 1 - graphically

From the graph, the revenue function and the cost function intersect at (100, 2 000) so the number of students required to achieve 'break even' is 100.

(1 mark)

Method 2 - algebraically

$$R = 20n$$

$$C = 10n + 1000$$

At break even point,

$$R = C$$

$$20n = 10n + 1\,000$$

$$10n = 1\,000$$

$$n = 100$$

So the number of students required is 100.

(1 mark)

d. i.

$$\begin{aligned}
 P &= R - C \\
 &= 20n - (10n + 1\,000) \\
 &= 20n - 10n - 1\,000 \\
 &= 10n - 1\,000
 \end{aligned}$$

(1 mark)

ii. Profit only occurs when revenue is greater than costs. This occurs when $n > 100$ since at $n = 100$, there is break even point and for $n < 100$, the dance school is losing money.

The required inequation is $n > 100$.

(1 mark)

e. The maximum number of students that the school can teach in a week is 200.

When $n = 200$,

$$P = 10n - 1\,000$$

becomes $P = 10 \times 200 - 1\,000$

$$= 2\,000 - 1\,000$$

$$= 1\,000$$

The maximum weekly profit is \$1 000.

(1 mark)

Question 2a. If you attend 4 classes per week you pay $4 \times \$20 = \80 each week.

(1 mark)

b. For 1 class you pay \$30 in total per week,

for 2 the total is \$50,

for 3 the total is \$75,

for 4 the total is \$80,

for 5 the total is \$100,

for 6 the total is \$90,

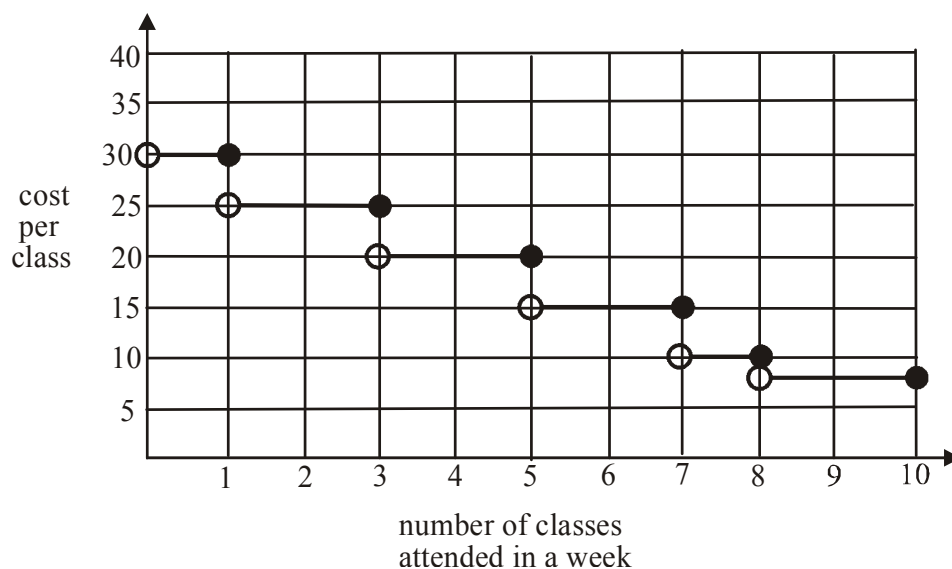
for 7 the total is \$105,

for 8 the total is \$80.

The maximum amount possible per week is \$105. This is how much you pay in total in a week if you are attending 7 classes.

(1 mark)

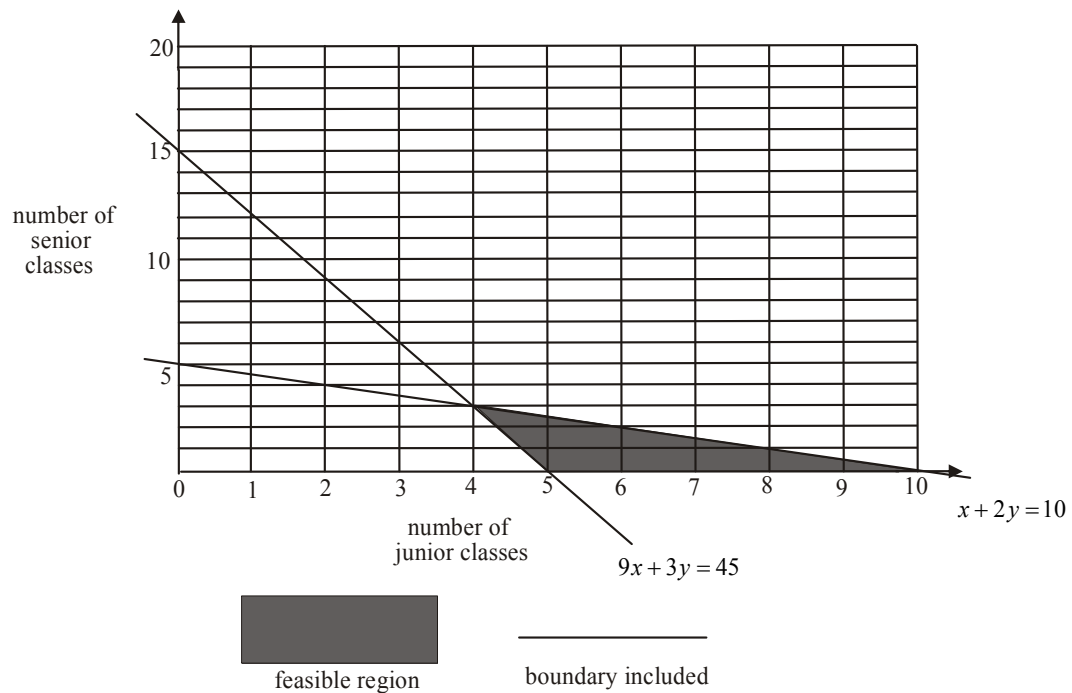
c.



(1 mark)

Question 3

a.

(1 mark) correctly showing boundary of $x + 2y \leq 10$

(1 mark) correctly showing feasible region

(1 mark) correctly indicating boundaries

- b. From the graph, the possible points, given that the coordinates have to be whole numbers, that is, they must represent the number of classes, are $(5,0)$ $(6,0)$ $(7,0)$ $(8,0)$ $(9,0)$ $(10,0)$ $(5,1)$ $(6,1)$ $(7,1)$ $(8,1)$ $(5,2)$ $(6,2)$ and $(4,3)$.

So there are 13 points.

(1 mark)

- c. $P = 12x + 8y$.

(1 mark)

- d. Maximum profit will occur at one of the corner points of the feasible region. From the graph, those corner points are located at $(5,0)$, $(10,0)$ and $(4,3)$.

$$\text{At } (5,0), \quad P = 12 \times 5 + 8 \times 0 = 60$$

$$\text{At } (10,0), \quad P = 12 \times 10 + 8 \times 0 = 120$$

$$\text{At } (4,3), \quad P = 12 \times 4 + 8 \times 3 = 72$$

The maximum profit that could be made is \$120.

(1 mark)

Total 15 marks

Question 2

a.
$$I = \frac{PrT}{100} \text{ (simple interest formula)}$$

$$= \frac{5\,000 \times 5.75 \times 4}{100}$$

$$= 1150 \quad (1 \text{ mark})$$

Total investment is worth $\$5\,000 + \$1150 = \$6\,150$.

(1 mark)

b.
$$A = PR^n$$

$$= 18\,000 \times (1.0045)^{72}$$

$$= 24\,869.57$$

$$R = 1 + \frac{r}{100} \text{ (compound interest formula)}$$

$$= 1 + \frac{0.45}{100}$$

$$= 1.0045$$

Note that annual interest of 5.4% represents monthly interest of $5.4\% \div 12 = 0.45\%$.

Note also that over 6 years, with monthly calculations of interest, there are $6 \times 12 = 72$ calculations of interest.

The investment is worth \$24 869.57.

(1 mark)

c. Since there are regular payments made, use *TVM* solver

$$N = 36$$

$$I\% = 6.4$$

$$PV = -3\,000 \text{ (money you give to the bank)}$$

$$PMT = -800 \text{ (money you give to the bank)}$$

$$FV = ?$$

$$P/Y = 4$$

$$C/Y = 4$$

The future value i.e. after nine years will be \$43 853.26.

So Juan's investment after 9 years has a total value of \$43 853.26.

(1 mark)

d. Again, since there are regular payments; this time in the context of a loan, we can use *TVM* solver.

$$N = 48$$

$$I = 7.2$$

$$PV = 140\,000 \text{ (money the bank gives you)}$$

$$PMT = ?$$

$$FV = -90\,000 \text{ (money you still need to give the bank)}$$

$$P/Y = 12$$

$$C/Y = 12$$

(1 mark)

They need to pay \$1 741.96 each month.

- e. Again using *TVM* solver,
 $N = ?$

$$I = 7 \cdot 2$$

$$PV = 90\,000$$

$$PMT = -900$$

$$FV = 0$$

$$P/Y = 12$$

$$C/Y = 12$$

It will take 153.17 periods of 1 month. That is, it will take $153.17 \div 12 = 12.8$ years (to one decimal place).

(1 mark)

Question 3

- a. The equipment is to be depreciated by $\$35\,000 - \$11\,000 = \$24\,000$. **(1 mark)**
 Over 6 years, this represents an annual depreciation rate of $\$24\,000 \div 6 = \$4\,000$ per year.

(1 mark)

- b. Using reducing balance depreciation, the value of the equipment V , is given by

$$V = P \times \left(1 - \frac{r}{100}\right)^t$$

$$11\,000 = 35\,000 \left(1 - \frac{r}{100}\right)^6$$

(1 mark)

Method 1 – using equation solver on a graphics calculator.

The equation to be solved is

$$0 = P \times \left(1 - \frac{r}{100}\right)^t - V$$

where $P = 35\,000$

$$t = 6$$

$$V = 11\,000$$

The value of r is given by 17.5442... So $r = 17.5\%$ (to one decimal place).

(1 mark)

Method 2 – by hand

$$11\,000 = 35\,000 \left(1 - \frac{r}{100}\right)^6$$

$$\frac{11\,000}{35\,000} = \left(1 - \frac{r}{100}\right)^6$$

$$(0.3142\dots)^{\frac{1}{6}} = 1 - \frac{r}{100}$$

$$0.8246 = 1 - \frac{r}{100}$$

$$\frac{r}{100} = 1 - 0.8245\dots$$

$$r = 100(1 - 0.8245\dots)$$

$$= 17.5\% \text{ (to one decimal place)}$$

(1 mark)

- c.** Using part **a.**, after 1 year the equipment had a book value of
 $\$35\,000 - \$4\,000 = \$31\,000$ (flat rate depreciation).
 Using part **b.**, after 1 year the equipment had a book value of
 $35\,000 \times \left(1 - \frac{17.5}{100}\right)^1 = \$28\,875$ (reducing balance depreciation).

The difference is x where

$$x = \$31\,000 - \$28\,875$$

$$= \$2\,125$$

(1 mark)

(If answers to either **a.** or **b.** were incorrect, but used correctly in **c.** then the mark should be awarded.)

Total 15 marks

Module 5: Networks and decision mathematics**Question 1**

a. i. $x = 1$ because Pat defeated Kate. (1 mark)

ii. $y = 0$ because Lou loses to Kate. (1 mark)

b. The one-step dominance score for Ricki is given by $1 + 1 + 0 + 0 = 2$. (1 mark)

c. Looking at the dominance matrix we see that Pat defeated Kate and Kate defeated Lou. This represents a two-step dominance of Pat over Lou. There are no other two-step dominances of Pat over Lou so $a = 1$. (1 mark)

d. Lou defeats Ricki and Ricki defeats Kate. This represents a two-step dominance of Lou over Kate. Also, Lou defeats Pat and Pat defeats Kate. This represents a second two-step dominance.
In total there are two two-step dominances of Lou over Kate so $b = 2$. (1 mark)

e. The dominances are given by

	one-step dominance score	two-step dominance score	one and two-step dominance score
Pat	1	1	2
Kate	1	2	3
Ricki	2	2	4
Lou	2	3	5

(1 mark)

From the one and two-step dominance scores we see that Lou is ranked first and Ricki is ranked second in this fitness competition.

(1 mark)

Question 2

	Wing Attack	Centre	Wing Defence	Goal Attack
Claire	3	2	2	5
Michelle	2	1	3	1
Sue	1	3	2	4
Kylie	5	4	3	1

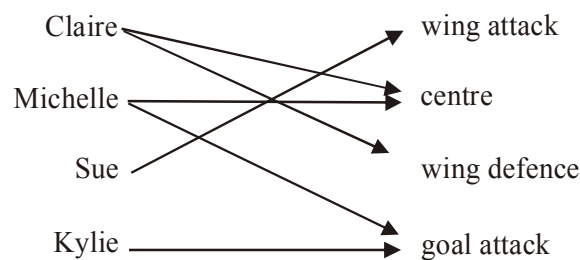
Subtract the minimum entry in each row from each of the entries in that row.

1	0	0	3
1	0	2	0
0	2	1	3
4	3	2	0

(1 mark)

The zero elements are covered and the minimum number of lines required to do this is four so we have an optimal allocation straight off.

Using a bipartite graph gives us the possibilities

**(1 mark)**

The optimal allocation is:

Claire plays wing defence.

Michelle plays centre.

Sue plays wing attack.

Kylie plays goal attack.

(1 mark)

Note that Kylie can only play goal attack and Sue can only play wing attack according to the bipartite graph. This then determines where Claire and Michelle can play.

Question 3

- a.** If the minimum time for the project to be completed is 12 weeks, then the length of the critical path is 12 weeks. Also since the earliest start time and the latest start time are the same for activity *H* and also for activity *J*, then they both lie on the critical path. So the length of activity *J* is $12 - 10 = 2$ weeks.
(1 mark)
- b.** From part **a.** the critical path lies along activities *A*, *D*, *H*, *J*. The earliest start time and latest start time for activity *H* is 7. That means that activities *H* and *J* have a combined duration of 5 weeks. Since *G* and *I* don't lie on the critical path, their combined duration must be less than 5 weeks so their maximum duration combined is 4 weeks.
(1 mark)
- c.** If Activities *A*, *C* and *I* are of equal duration, and given that their combined duration is less than 12 weeks (because they don't form a critical path) and also given that the duration for each activity is in whole weeks, then they could each have a duration of 3 weeks (total duration of 9 weeks) or 2 weeks (total duration of 6 weeks) or 1 week (total duration of 3 weeks). Any of these three answers is acceptable. So activity *A* could have a duration of 1, 2 or 3 weeks.
(1 mark)
- d. i.** Activity *E* takes 3 weeks and activities *H* and *J* lie on the critical path and have a combined duration of 5 weeks. Therefore Activity *E* would have a latest starting time of $12 - 5 - 3 = 4$ weeks .
(1 mark)
- ii.** Activity *E* has a latest starting time of 4 weeks and activity *F* has a latest starting time of $10 - 3 = 7$ weeks. Neither activities *B*, *E* or *F* lie on the critical path. Therefore the duration of *B* can be 1, 2 or 3 weeks (assuming that it is not 0 weeks). Note that if activity *B* had a duration of 4 weeks then activities *B* and *E* would then be on the critical path.
(1 mark)

Total 15 marks

Module 6: Matrices**Question 1**

a. $P = \begin{bmatrix} 80 \\ 100 \\ 90 \\ 120 \end{bmatrix}$

The order of matrix P is 4×1 ; that is 4 rows $\times$ 1 column .

(1 mark)

- b. The matrix product RP gives the total profit since R is a 1×4 matrix and P is a 4×1 matrix. The matrix product RP is a 1×1 matrix. The matrix product PR multiplies a 4×1 matrix by a 1×4 matrix and gives a 4×4 matrix.

(1 mark)

c.

$$\begin{aligned}
 RP &= \begin{bmatrix} 7 & 6 & 2 & 4 \end{bmatrix} \begin{bmatrix} 80 \\ 100 \\ 90 \\ 120 \end{bmatrix} \\
 &= [7 \times 80 + 6 \times 100 + 2 \times 90 + 4 \times 120] \\
 &= [1820]
 \end{aligned}$$

The profit is \$1 820.

(1 mark)

Question 2

a.
$$T = \begin{matrix} & \begin{matrix} \text{this year} \\ A & B & C \end{matrix} \\ \begin{matrix} \text{following year} \\ A \\ B \\ C \end{matrix} & \begin{bmatrix} 0.82 & 0.12 & 0.05 \\ 0.08 & 0.78 & 0.07 \\ 0.10 & 0.10 & 0.88 \end{bmatrix} \end{matrix}$$

(2 marks)

b.
$$H_0 = \begin{bmatrix} 45\,000 \\ 62\,000 \\ 56\,000 \end{bmatrix} \begin{matrix} A \\ B \\ C \end{matrix}$$

(1 mark)

c. i. The matrix product is TH_0 .

(1 mark)

ii.

$$TH_0 = \begin{bmatrix} 0.82 & 0.12 & 0.05 \\ 0.08 & 0.78 & 0.07 \\ 0.10 & 0.10 & 0.88 \end{bmatrix} \begin{bmatrix} 45\,000 \\ 62\,000 \\ 56\,000 \end{bmatrix}$$

$$= \begin{bmatrix} 47\,140 \\ 55\,880 \\ 59\,980 \end{bmatrix}$$

(1 mark)

d.
$$T^{10}H_0 = \begin{bmatrix} 48\,702 \\ 41\,715 \\ 72\,583 \end{bmatrix}$$

$$T^{30}H_0 = \begin{bmatrix} 47\,921 \\ 40\,999 \\ 74\,080 \end{bmatrix}$$

(1 mark)

$$T^{50}H_0 = \begin{bmatrix} 47\,912 \\ 40\,997 \\ 74\,091 \end{bmatrix}$$

$$T^{60}H_0 = \begin{bmatrix} 47\,912 \\ 40\,997 \\ 74\,091 \end{bmatrix}$$

The last two matrices indicate that a steady state has been reached.

(1 mark)

(Note that two state matrices where the steady state has been reached – correct to the nearest whole number must be shown.)

Question 3

a. $AX = B$

$$\begin{bmatrix} 1 & 1 & -1 \\ -1 & 0 & 1 \\ 2 & 1 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 580 \\ 800 \\ 9620 \end{bmatrix}$$

(1 mark)

b. i. $\det A = 1$ (using a calculator).

(1 mark)

ii. Matrix B does not have a determinant because it is not a square matrix.

(1 mark)

c. Now,

$$A^{-1} = \begin{bmatrix} -1 & 0 & 1 \\ 1 & 1 & 0 \\ -1 & 1 & 1 \end{bmatrix}$$

Also,

(1 mark)

$$AX = B$$

$$A^{-1}AX = A^{-1}B$$

$$X = A^{-1}B$$

$$\begin{aligned} &= \begin{bmatrix} -1 & 0 & 1 \\ 1 & 1 & 0 \\ -1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 580 \\ 800 \\ 9620 \end{bmatrix} \\ &= \begin{bmatrix} 9040 \\ 1380 \\ 9840 \end{bmatrix} \end{aligned}$$

So 9 040 guests come for the scuba diving, 1 380 come for the golf and 9 840 come for the swimming.

(1 mark)**Total 15 marks**