Website: contoureducation.com.au | **Phone:** 1800 888 300
Email: hello@contoureducation.com.au

VCE Specialist Mathematics ½

Graph Theory I [5.3]

Test

20 Marks. 1 Minute Reading. 16 Minutes Writing.

Results:

Test Questions	_____ / 20

Section A: Test Questions (20 Marks)

Question 1 (4 marks)

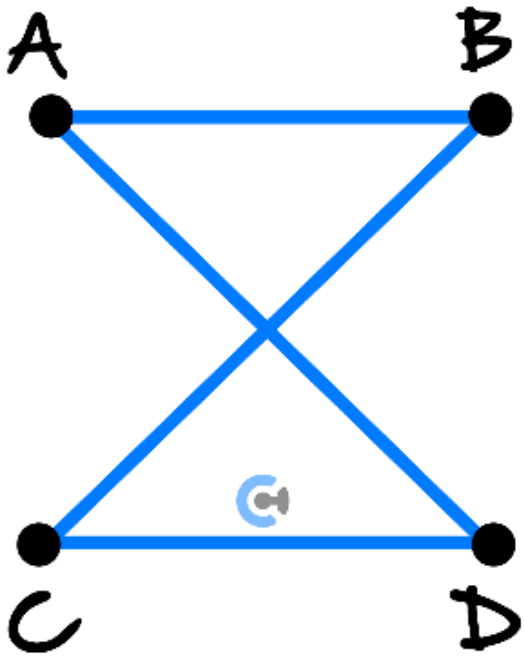
Tick whether the following statements are **true** or **false**.

Statement	True	False
a. A graph consists of a set of objects called **vertices** together with a set of unordered pairs of vertices, called **edges**.		
b. The number of edges that are directly connected to a particular vertex is the "degree" of the vertex and is generally denoted as $\deg(V)$, where V is the vertex.		
c. A **simple graph** is one in which pairs of vertices are always connected by one edge.		
d. A **connected** graph is a graph where it is possible to reach all vertices by moving along edges.		
e. A **complete** graph is a simple graph in which each vertex is connected to every other vertex.		
f. The number of edges in a complete graph K_n is given by the formula: $\frac{n(n+1)}{2}$.		
g. In graph theory, an isomorphism is where the corresponding vertices in both graphs are connected by the same edges.		
h. A subgraph is a graph whose vertices and edges are all contained within the original graph.		

Space for Personal Notes

Question 2 (2 marks)

Write the vertex sets and edge sets for the graph below.



vertices = {A, B, C, D}

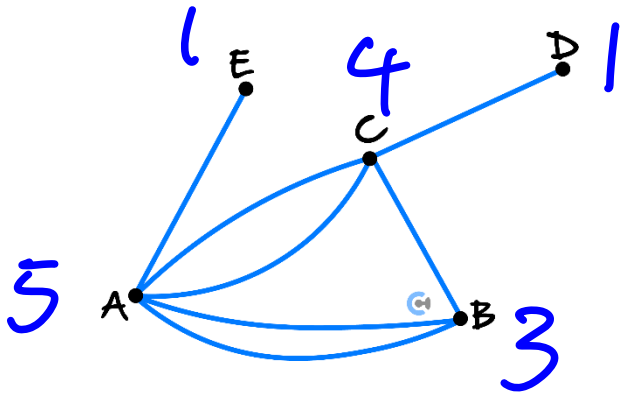
edges = {AB, AD, BC, CD}

Space for Personal Notes

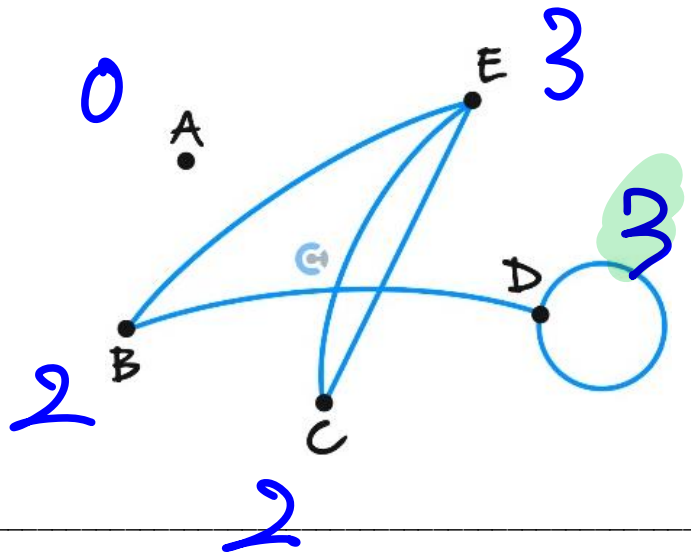
Question 3 (4 marks)

Identify the degree of each vertex in the following graphs.

a. (2 marks)

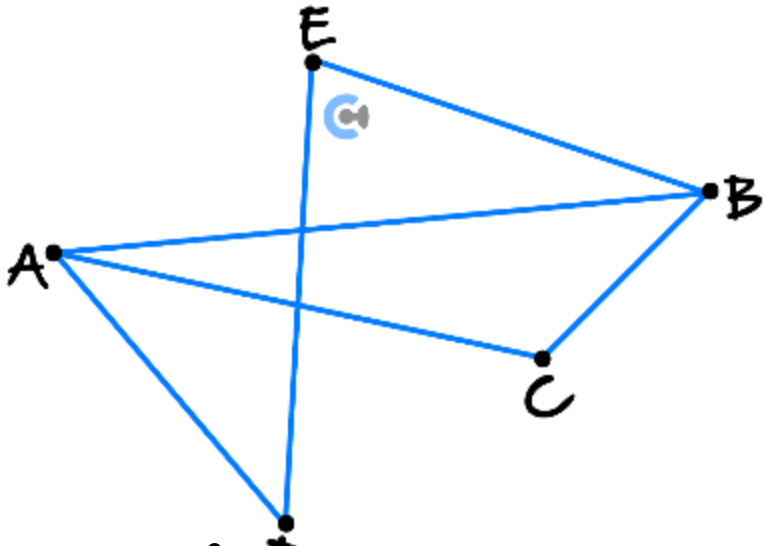


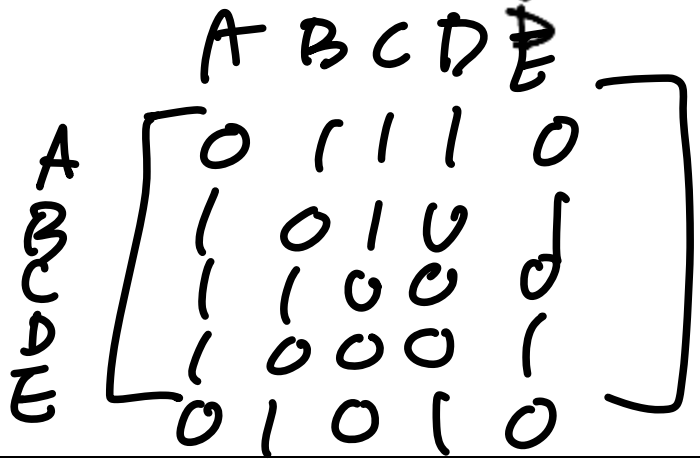
b. (2 marks)



Question 4 (2 marks)

Construct the adjacency matrix for the given graph.



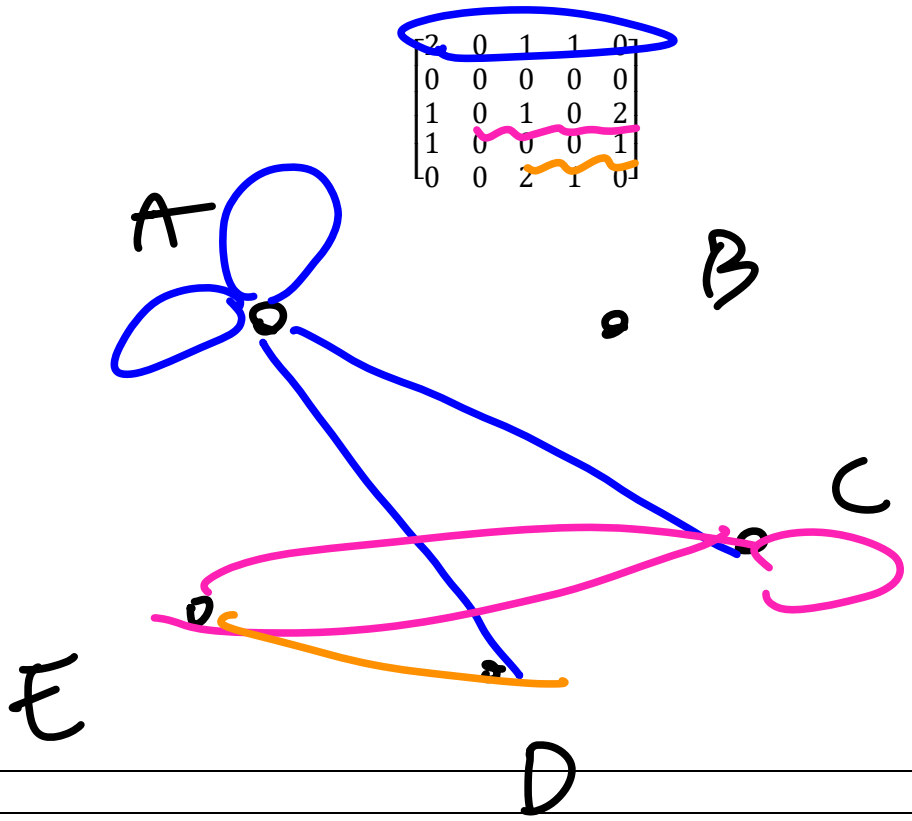


Space for Personal Notes

Question 5 (3 marks)

Draw graphs to represent the following adjacency matrices.

$$\begin{bmatrix} 2 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 2 \\ 1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 2 & 1 & 0 \end{bmatrix}$$



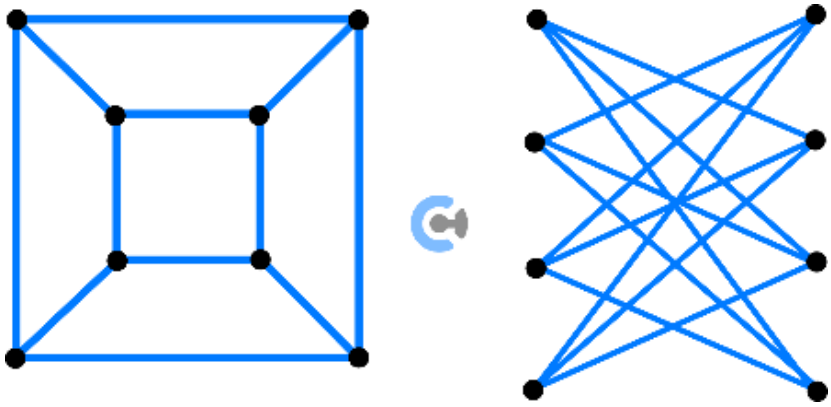
Space for Personal Notes

Question 6 (2 marks)

For each of the following pairs of graphs, determine whether the graphs are isomorphic.

a. (1 mark)

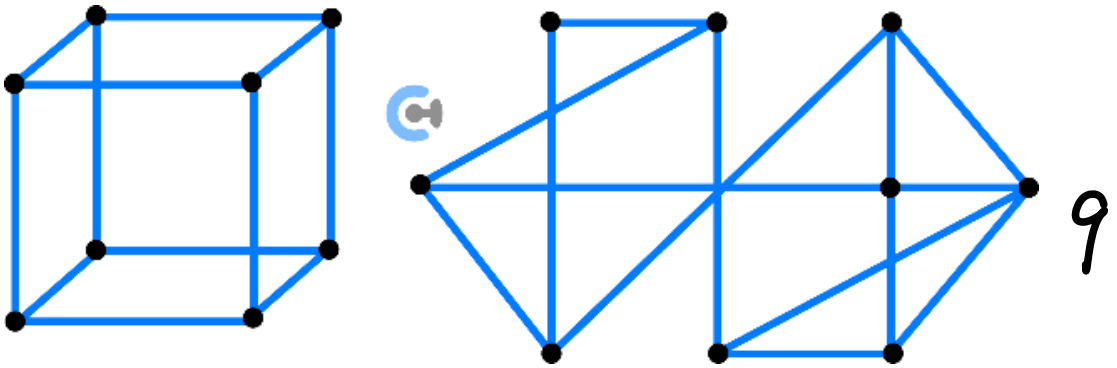
3-regular



Yes

b. (1 mark)

8



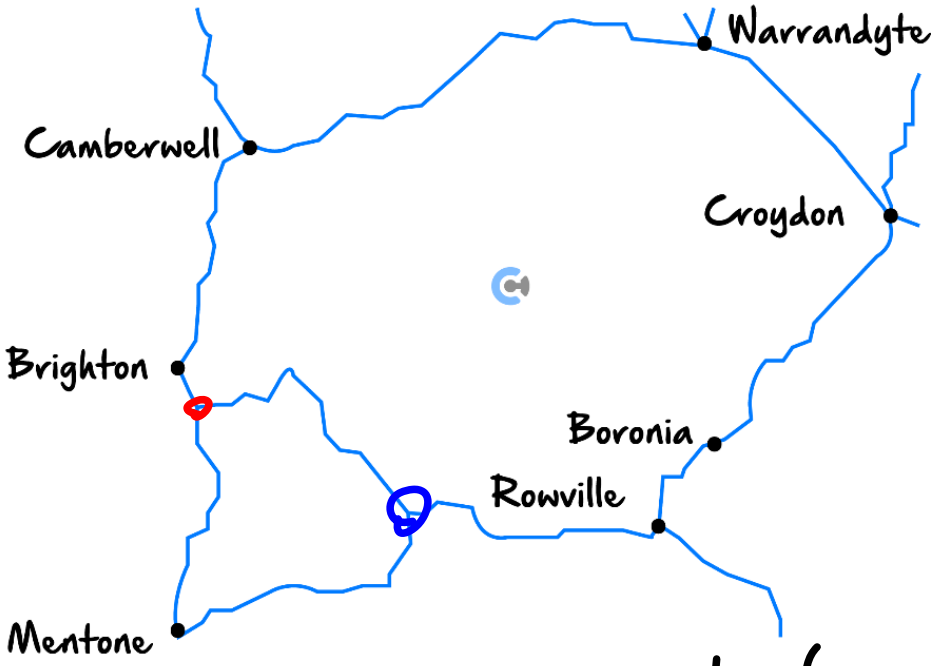
9

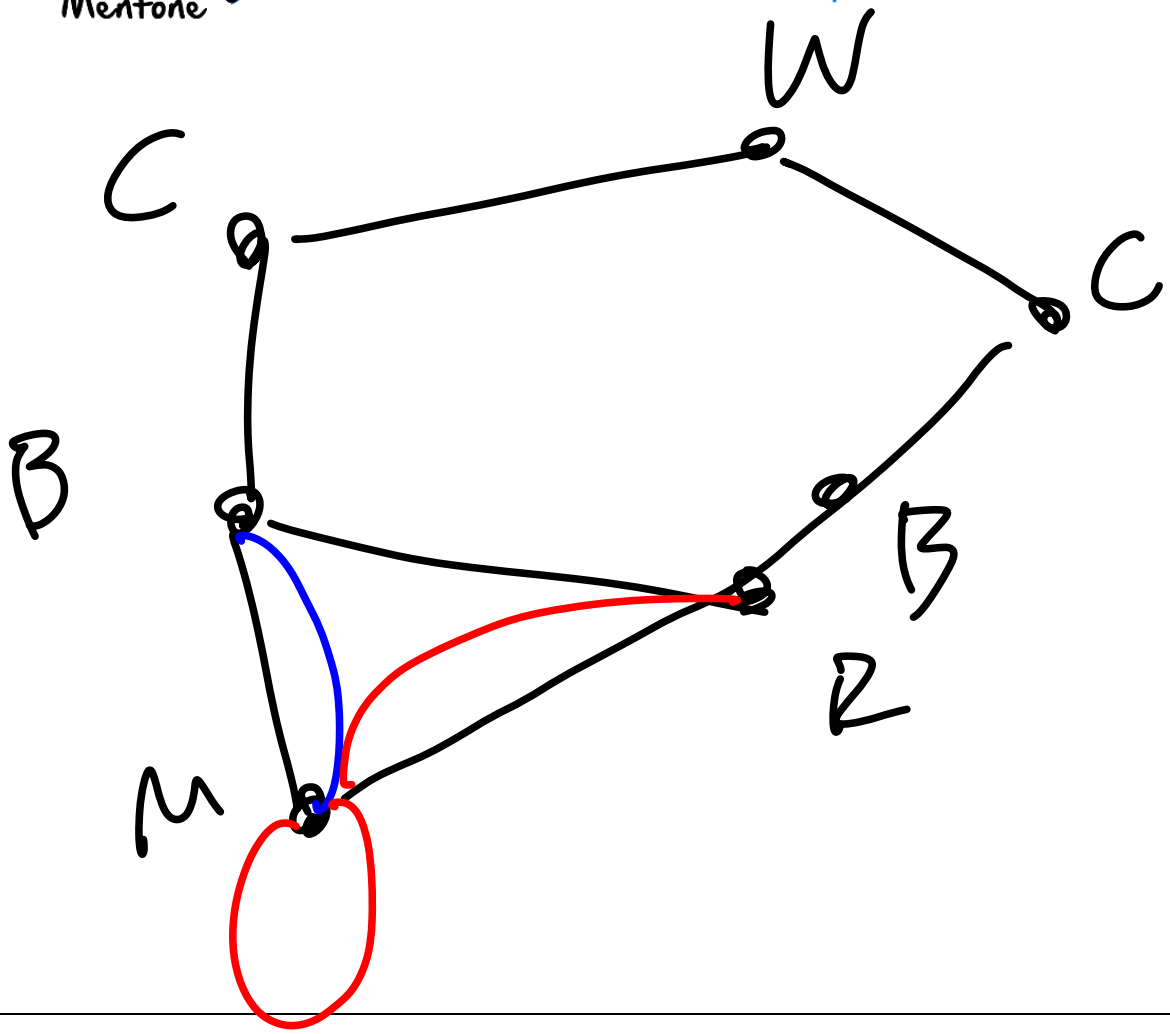
Not

Space for Personal Notes

Question 7 (3 marks)

Using the map below, represent the paths between the towns as a graph.





CONTOUREDUCATION

Website: contoureducation.com.au | **Phone:** 1800 888 300 | **Email:** hello@contoureducation.com.au

VCE Specialist Mathematics ½

Free 1-on-1 Consults

What are 1-on-1 Consults?

- **Who Runs Them?** Experienced Contour tutors (45 + raw scores and 99 + ATARs).
- **Who Can Join?** Fully enrolled Contour students.
- **When Are They?** 30-minute 1-on-1 help sessions, after-school weekdays, and all-day weekends.
- **What To Do?** Join on time, ask questions, re-learn concepts, or extend yourself!
- **Price?** Completely free!
- **One Active Booking Per Subject:** Must attend your current consultation before scheduling the next :)

SAVE THE LINK, AND MAKE THE MOST OF THIS (FREE) SERVICE!

Booking Link

bit.ly/contour-specialist-consult-2025