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VCE Specialist Mathematics ½ Logic & Algorithms I [2.4]

Workbook

Outline:



Pg 19-30

Algorithms

Pg 02-09

Pg 10-18

- Introduction to Algorithm
- Assigning Variables
- Flowchart
- Table of Values

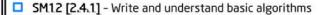
Selections and Loops

- Selections
- Loops

Pseudocode

- Introduction to Pseudocodes
- Pseudocode for Selection
- Pseudocode for Loops
- Functions
- Lists

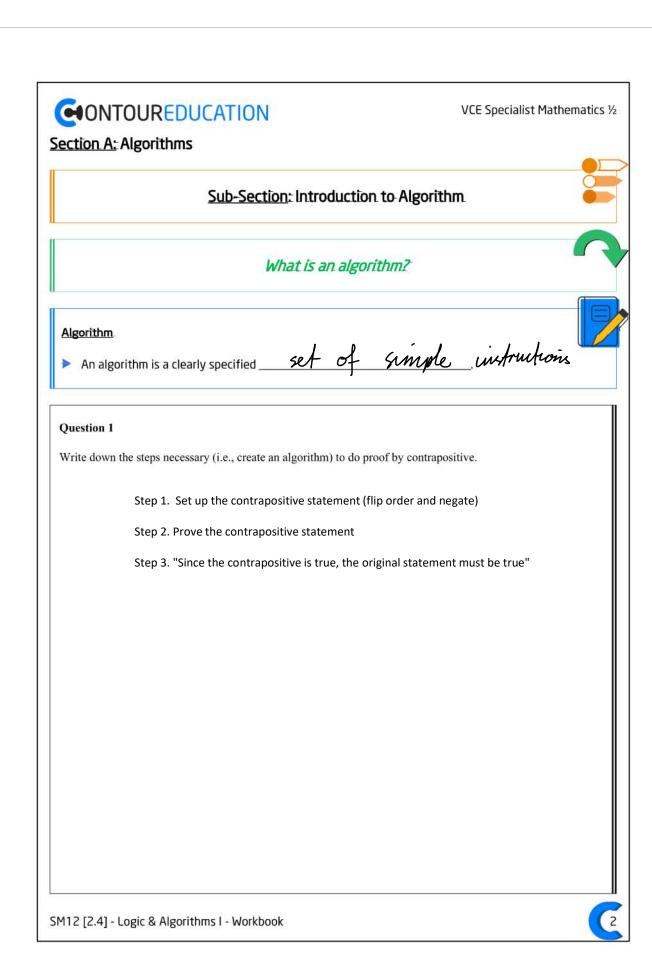
Learning Objectives:





- SM12 [2.4.2] Understand and evaluate algorithms that have conditional statements and represent hybrid functions as algorithms
- SM12 [2.4.3] Understand and evaluate algorithms with loops
- SM12 [2.4.4] Write and evaluate functions using pseudocode









Sub-Section: Assigning Variables

Assigning Variables



- To construct algorithms for more mathematical/complex problems, _ variables will be useful.
 - **G** E.g., $A \leftarrow 3$ assigns the **value 3** to the **variable** A.
- ➤ We can also <u>wpdate</u> our variables using the arrow.
 - E.g., $A \leftarrow A + 3$ assigns the value A + 3 to the variable A.
 - Since the value of A was already 3, its new value will be 6.

Question 2 Walkthrough.

For the following algorithm, evaluate the final output of the algorithm.

Step 1.
$$A \leftarrow 3$$

Step 3.
$$A \leftarrow 2A - 1$$

Step 1.
$$A \leftarrow 3$$

Step 2. $A \leftarrow A + 2$

Step 3. $A \leftarrow 2A - 1$

Step 4: Print A .

Step 3. $A \leftarrow 2A - 1$

Step 4: Print A .





Question 3

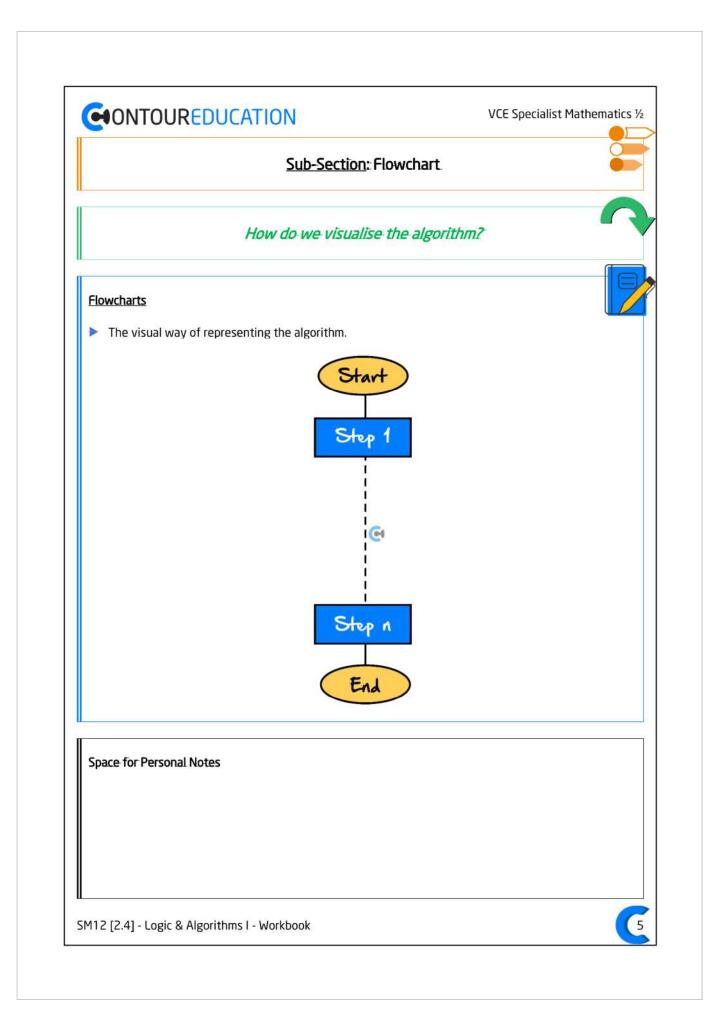
Construct an algorithm that doubles any input given.

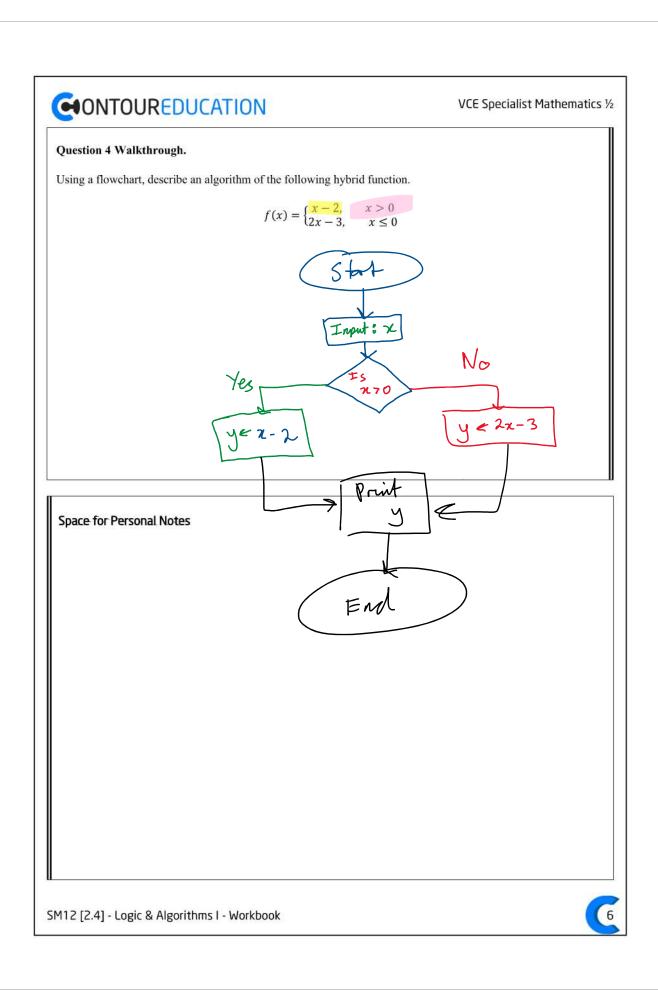
Step 1: Imput A

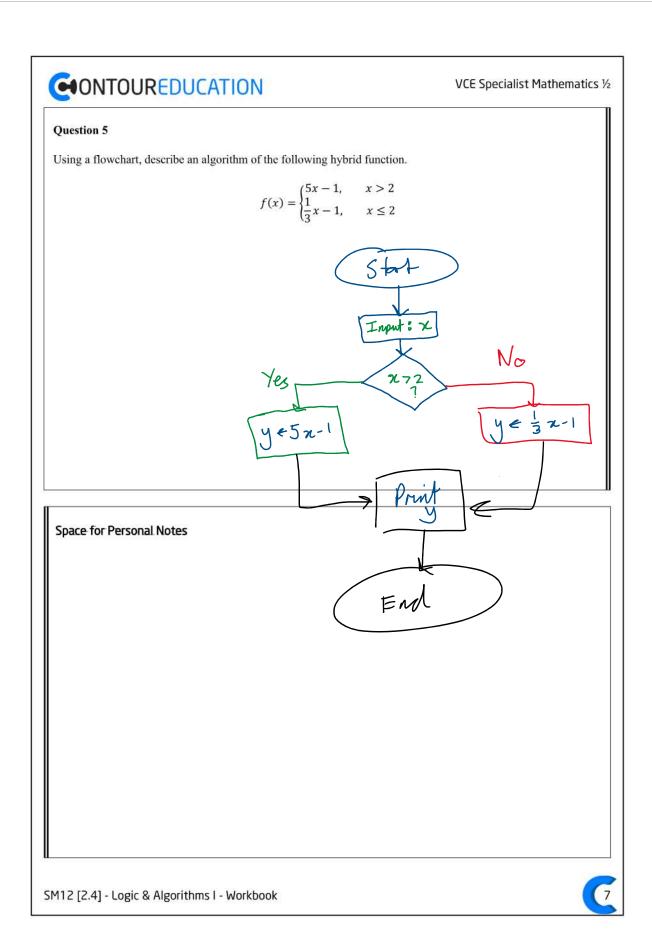
Step 2: A = 2A

Step 3: Print A

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How do we track the value of the variables?



Table of Values

Used to check if the algorithm works by following the steps one by one.

	Variable (s)	
Step 1	Value 1	
	¥	
•		
Step n	Value n	

Question 6 Walkthrough.

Consider the following algorithm.

Step 1:
$$A \leftarrow 2$$
 and $B \leftarrow 3$

Step 2:
$$A \leftarrow 2A + 4$$
 and $B \leftarrow 2B - 1$

Step 3:
$$A \leftarrow B$$

Perform a desk check (construct the table of values) for the values of A and B.

Step	A	B
1	2	3
2	8	5
3	5	5





Question 7

The following algorithm was intended to swap the values of two variables, A and B.

Step 1: Input A, B

Step 2: $A \leftarrow B$

Step 3: $B \leftarrow A$

Step 4: Print A, B

a. Perform a desk check (construct the table of values) for the values of A and B as 2,4 for the above algorithm.

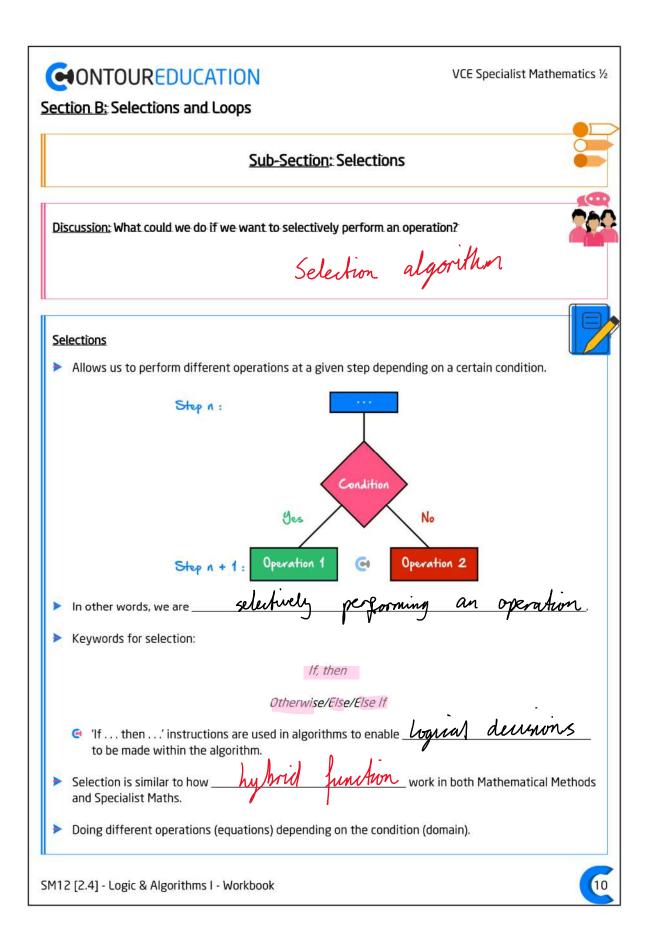
Step	A	B
l	2	4
2	4	4
3	4	9
4	4	4

b. Did the algorithm perform what it was designed for?



c. Construct a new algorithm that swaps the value of *A* and *B*, and performs a desk check.

Create temporary variable



Question 8 Walkthrough.

Construct a table of values for the following algorithm.

Step 1:
$$n \leftarrow 2$$

Step 2: If n is even, then
$$T \leftarrow 3n + 5$$

Otherwise $T \leftarrow n + 5$

Step 3:
$$n \leftarrow n + 3$$

Step 4: Print n, T.

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Question 9 Tech-Active.

Following is an algorithm for calculating the Australian tax.

Step 1: Input income

Step 2a: If $income \le 18200$, then $tax \leftarrow 0$

Step 2b: Else If $income \le 37000$, then $tax \leftarrow 0.19 \times income - 3458$

Step 2c: Else If $income \le 90000$, then $tax \leftarrow 0.325 \times income - 8453$

Step 2d: Else If $income \le 180000$, then $tax \leftarrow 0.37 \times income - 12503$

Step 2e: Else $tax \leftarrow 0.45 \times income - 26903$

Step 3: Print tax

Calculate the tax for \$75000.

tax < 0.325 × 75000 - 8453

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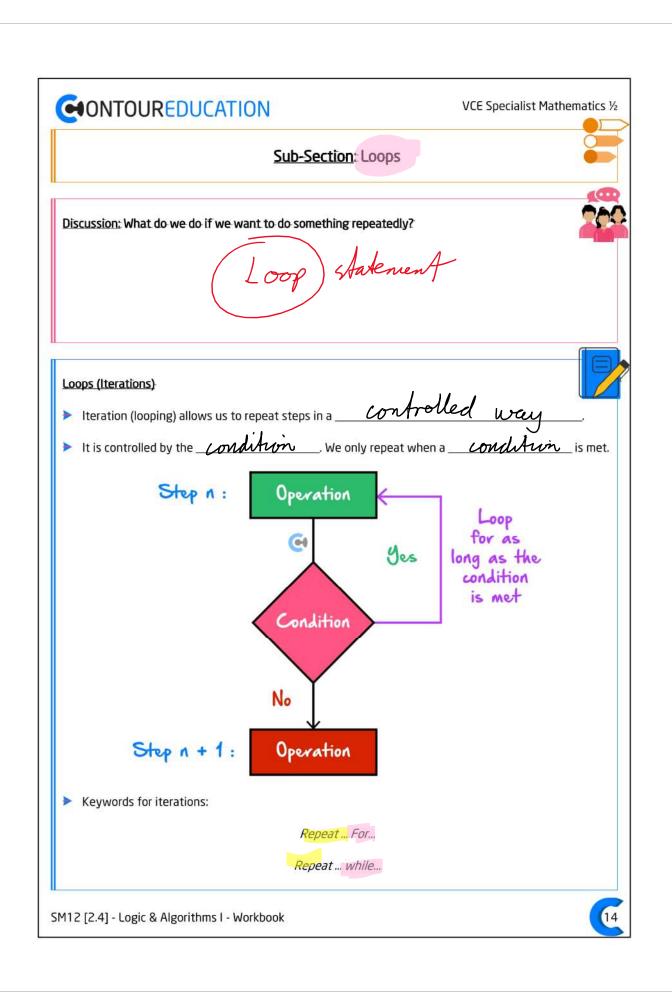
Question 10

Turn the following hybrid function into an algorithm.

$$f(n) = \begin{cases} 1 - 2n, & \text{if } n \text{ is even} \\ 4, & \text{if } n = 5 \\ 2n + 1, & \text{otherwise} \end{cases}$$

Step 1'. Input nStep 2: If n is even, y = 1-2nelse if n = 5, y = 4else y = 2n+1Step 3: Print y

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Discussion: What are the differences between for and while loops?



For: We know how many times to repeat While: We don't know.

Analogy: Your parents taking care of you.



- Consider the two parents below.
 - Parent 1:

I'll take care of you for the next 10 years!

@ Parent 2:

I'll take care of you while you are not married!

- For which parent do we exactly know how many years they will take care of us?
- Hence, which parent is a for loop and which parent is a while loop?



P1 = for P2 = white

For v/s While Loop



- For Loop
 - We know how many iterations will happen.
- While Loop
 - We don't know how many loops will happen.

Question 11 Walkthrough.

Create a table of values for the following algorithm.

Step 1.
$$A \leftarrow 10$$
 and $n \leftarrow 0$

Step 2.
$$A \leftarrow 2A$$
 and $n \leftarrow n + 2$

Step 3. Repeat from step 2 while n < 5

Step	A	n
1	10	0
2	20	2
	40	4
	80	6

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Question 12

Construct an algorithm that outputs the largest multiple of 3 that is less than 1000.

5tep 1:
$$X \leftarrow 0$$

5tep 2: $X \leftarrow X + 3$

NOTE: We use a while loop here as we do not know straight away how many loops this will take.



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Question 13

Consider the following algorithm:

Step 1.
$$A \leftarrow 87$$

Step 2.
$$A \leftarrow 2A - 1$$

Step 3. Repeat from step 2 while A > 50

What is the problem with this algorithm?

Algorithm goes on forever, because condition is ALWAYS met

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Section C: Pseudocode

Sub-Section: Introduction to Pseudocodes



Pseudocode



operation 1

else
operation 2

end if

- "Pseudo" = fake, so pseudocode = fake code.
- Concise way of representing algorithms.

Pseudocodes: Indentation (Spacing)



- For pseudocodes, the placement of codes is important.
- For every rabbit hole of codes, we fall into, we write out codes more towards the right direction.
 - For every rabbit hole of codes, we come out of, we write out codes back towards the <u>left</u> <u>direction</u>.
 - A rabbit hole of codes can be loops, selections, etc.

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Sub-Section: Pseudocode for Selection.

Pseudocode: Selections (If, Else, Else if, Then)



"If-then" allows us to perform operations when a certain condition is met.

if condition then
operation
end if

> "Else" provides an opportunity to perform a different operation when a condition is NOT met.

if condition then
operation 1
else
operation 2
end if

"Else if" provides an opportunity to add multiple pathways each with different conditions.

if condition 1 then
operation 1
else if condition 2 then
operation 2
else
operation 3
end if

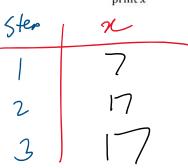


Question 14 Walkthrough.

Evaluate the final output from each of the following:

$$x \leftarrow 7$$
if $x < 15$

$$x \leftarrow x + 10$$
else
$$x \leftarrow x - 10$$
print x



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Question 15

Evaluate the final output from each of the following:

Step	a	b	$a \leftarrow 4v$ $b \leftarrow 2$
	١	2	if $a + b < 5$ $b \leftarrow b + 5$
2	0	7	$a \leftarrow a - 1$ end if $a \leftarrow b$
Ster	a	5	, ,
	4	2	_
2	4	2	-

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Variable moved from

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pper bound



Sub-Section: Pseudocode for Loops

Pseudocode: Iterations (For Loops, While Loops, and Nested Loops)



For Loops: It is a loop that increases the variable by 1 each time it loops.

of coops. It is a loop that increases the variable by I each time it loops.

lower

for variable from lower bound to upper bound

condition

operation

end for

- While Loops: It is a loop that does NOT change the value of a variable by default.
 - To change the value of the variable, it needs to be described in the <u>operaturn</u> section

while condition
operation
end while

- Nested Loop: We can have a loop happening within another loop.
 - The first pass of the outer loop starts the inner loop, which executes to completion. Then the second pass of the outer loop starts the inner loop again. This repeats until the outer loop finishes.

for var1 from lower1 to upper1

for var2 from lower2 to upper2

operation2

end for

operation 1

end for

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Example of a Nested Loop: Minutes and seconds.

Declare integer seconds, minutes

For minutes = 0 to 59

For seconds = 0 to 59

Output "", seconds

Next For

Next For

Question 16 Walkthrough.

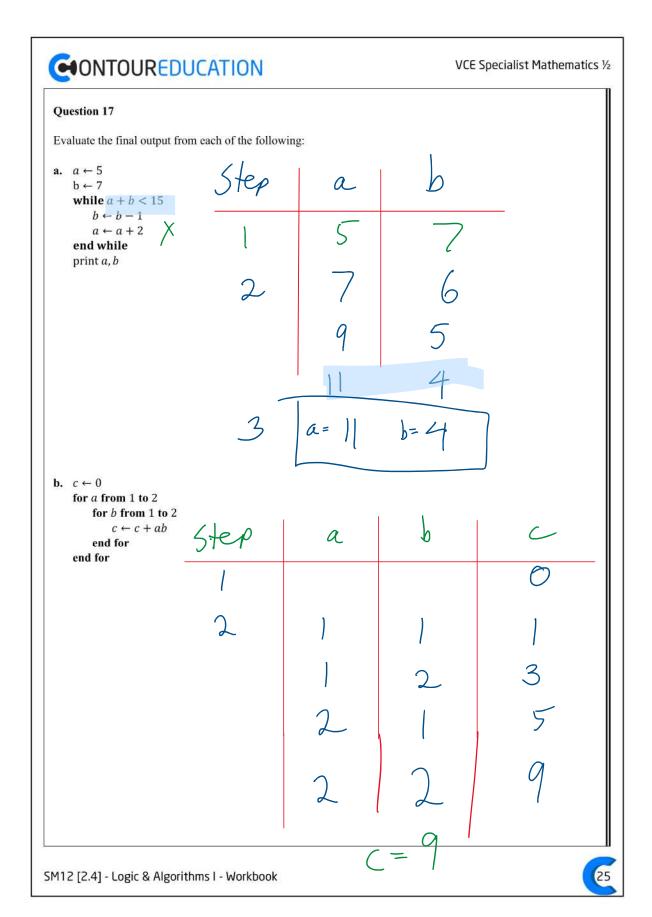
Evaluate the final output from each of the following:

$$total \leftarrow 0$$

for i **from** 1 **to** 3
 $total \leftarrow total + i$
end for
print $total$

Step	total	i
1	0	
2	1)
	3	2
	6	3
3	16	7

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Function

Think of a function as a bag of algorithms.



Instead of saying "an algorithm for picking the largest prime number smaller than n^* , we can save this algorithm as f(n).

- Using functions allows us to easily change the input of the algorithm.
- - 6 By simply mentioning the function within the pseudocode, we can incorporate another algorithm.

define function(input):

follow these instructions

return output

Question 18 Walkthrough.

Construct a pseudocode for a function named "dist" which calculates the distance between two points.

Define dist (x_1, x_2, y_1, y_2) inputs $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ return d

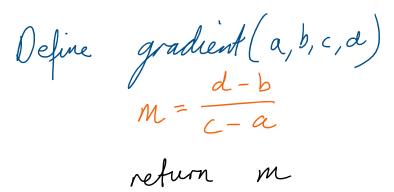
NOTE: Within the function, the two points can be defined as any arbitrary value.



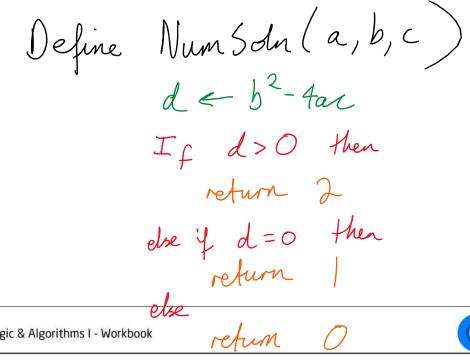
Question 19

Using pseudocode, define a function for finding each of the following:

a. The gradient of the line through two points (a, b) and (c, d).



b. Number of solutions for a quadratic equation $ax^2 + bx + c = 0$.







Sub-Section: Lists

Lists



Lists are merely a collection of values. More formally, it is defined as a finite sequence of values.

 $A \leftarrow [1,3,5,7,9]$: Defines A as a list of odd numbers up to 10.

- The notation A[n] spits out the " n^{th} " value in the list. E.g., A[3] = 5.
- To add more values to the list we can _append

Append 11 to A (From above)

Result: A = [1, 3, 5, 7, 9, 11].

- Index:
 - The position of an entry in a list is called its index. In this book, we use 1 as the index of the first entry. However, most programming languages use 0 as the index of the first entry.

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Question 20 Walkthrough.

Consider the algorithm below and evaluate the output.

$$A \leftarrow []$$

for i from 1 to 10
if $i < 8$ then
append i to A
end if
end for
return A

Step	i	A
1		[]
2	1	$[\Gamma]$
	2	[1,2]

$$A = [1,2,3,4,5,6,7]$$

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Question 21

Consider the algorithm below and evaluate the output.

$A \leftarrow [\]$ for i from 1 to 8	5tep	7	
if $i < 4$ then append $2i$ to A	ľ		
else append $i - 2$ to A		l .	[2]
end if end for		2	[2,4]
return A		3	[2,4,6]
		4	[2,4,6,2]
		5	,
	ر (6	;
A = [2,4,6,3]	14,5,6	7	[2,4,6, 2,3,4,5,6

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Contour Checklist

Learning Objective: [2.4.1] – Write and Understand Basic Algorithms

Key Takeaways

Algorithm.

An algorithm is a clearly specified ______ set of simple instructions.

Assigning Variables

assigning

- To construct algorithms for more mathematical/complex problems, _ variables will be useful.
 - E.g., $A \leftarrow 3$ assigns the value 3 to the variable A.
- We can also <u>update</u> our variables using the arrow.
 - \bigcirc E.g., $A \leftarrow A + 3$ assigns the value A + 3 to the variable A.

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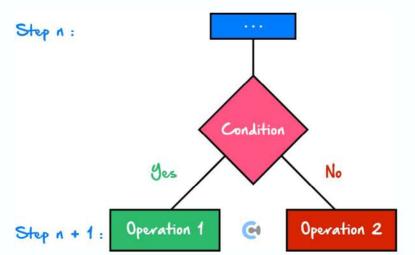
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 <u>Learning Objective</u>: [2.4.2] – Understanding and Evaluate Algorithms that have Conditional Statements and Represent Hybrid Functions as Algorithms

Key Takeaways

Selections

Allows us to perform different operations at a given step depending on a certain condition.



- ☐ In other words, we are _____ selectively performing an operation
- Keywords for selection:

If, then

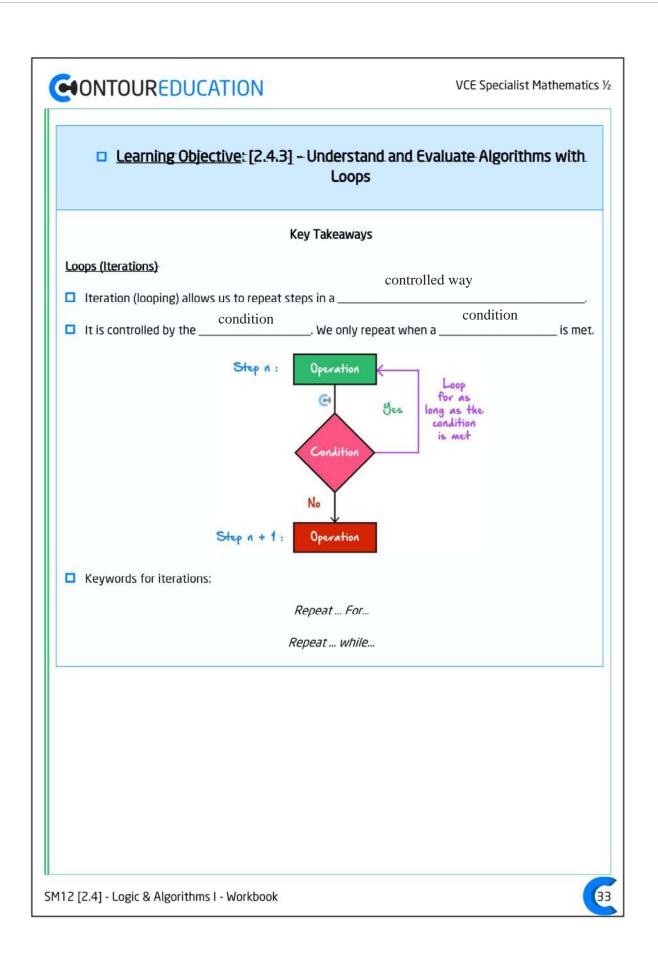
Otherwise/Else/Else If

'If ... then ...' instructions are used in algorithms to enable _______
 to be made within the algorithm.

hybrid functions

- Selection is similar to how ______ work in both Mathematical Methods and Specialist Maths.
- Doing different operations (equations) depending on the condition (domain).

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 Learning Objective: [2.4.4] – Write and Evaluate Functions Using Pseudocode

Key Takeaways

Pseudocode

if condition then
operation 1
else
operation 2
end if

- "Pseudo" = fake, so pseudocode = fake code.
- Concise way of representing algorithms.

Function

Think of a function as a bag of algorithms.

Instead of saying "an algorithm for picking the largest prime number smaller than n^* , we can save this algorithm as f(n).

- Using functions allows us to easily change the input of the algorithm.
- By incorporating functions within another algorithm, it allows us to have an ___

algorithm within algorithms

 By simply mentioning the function within the pseudocode, we can incorporate another algorithm.

define function(input):
 follow these instructions
 return output

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