



Website: contoureducation.com.au | Phone: 1800 888 300
Email: hello@contoureducation.com.au

VCE Mathematical Methods $\frac{3}{4}$
Differentiation II [2.2]
Test Solutions

20.5 Marks. 10 Minutes Writing.

Results:

Test Questions	_____ / 13.5
Extension Test Questions	_____ / 7



Section A: Test Questions (13.5 Marks)

Question 1 (3.5 marks)

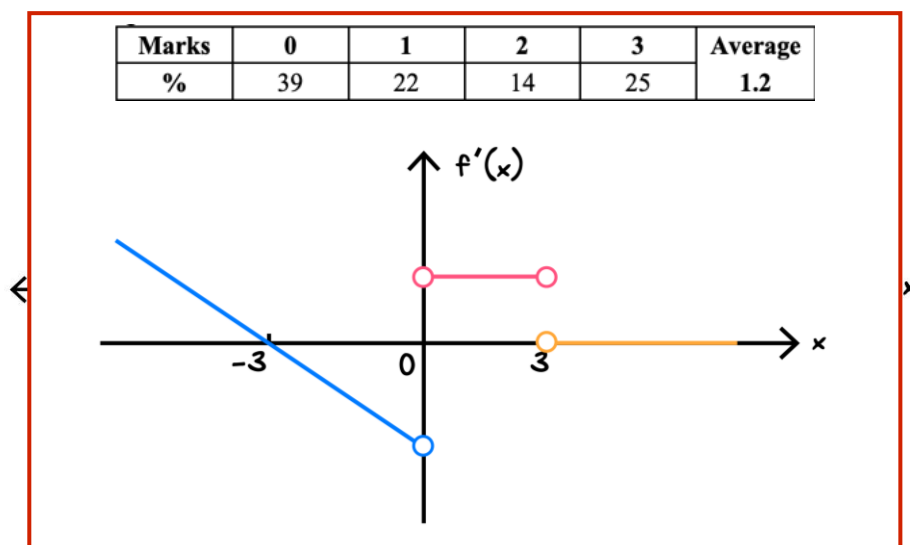
Tick whether the following statements are **true** or **false**.

	True	False
a. If the function is undefined at $x = a$, the limit is also always undefined at $x = a$.		<input checked="" type="checkbox"/>
b. A function is continuous if the limit is defined.		<input checked="" type="checkbox"/>
c. For a function to be differentiable, it must be continuous and the gradient from the left and right must be the same.	<input checked="" type="checkbox"/>	
d. When joined smoothly, the function is NOT differentiable.		<input checked="" type="checkbox"/>
e. When the function's positive gradient is getting steeper, then it is concave down.		<input checked="" type="checkbox"/>
f. Points of inflection occur when the concavity of the function changes.	<input checked="" type="checkbox"/>	
g. Not all points of inflection are stationary points of inflection. However, all stationary points of inflection are points of inflection.	<input checked="" type="checkbox"/>	

Space for Personal Notes

Question 2 (4 marks)

The diagram below shows the graph of a function with domain R .



a. For the graph shown above, sketch, on the same set of axes, the graph of the derivative function. (3 marks)

b. Hence, state the domain of the derivative function. (1 mark)

Marks	0	1	Average
%	55	45	0.5

$R \setminus \{0, 3\}$

Space for Personal Notes

Question 3 (3 marks)

Consider the function:

$$f(x) = \begin{cases} ax^2 + 4 & -5 \leq x \leq 1 \\ \sin(x - 1) + b & 1 < x \leq 3 \end{cases}$$

- a. Find the value of a and b such that the graph joins smoothly at $x = 1$. (2 marks)

```
[1]:= f[x_] := a * x^2 + 4
[2]:= g[x_] := Sin[x - 1] + b
[3]:= Solve[f[1] == g[1] && f'[1] == g'[1], {a, b}]
t[3]= {{a -> 1/2, b -> 9/2}}
```

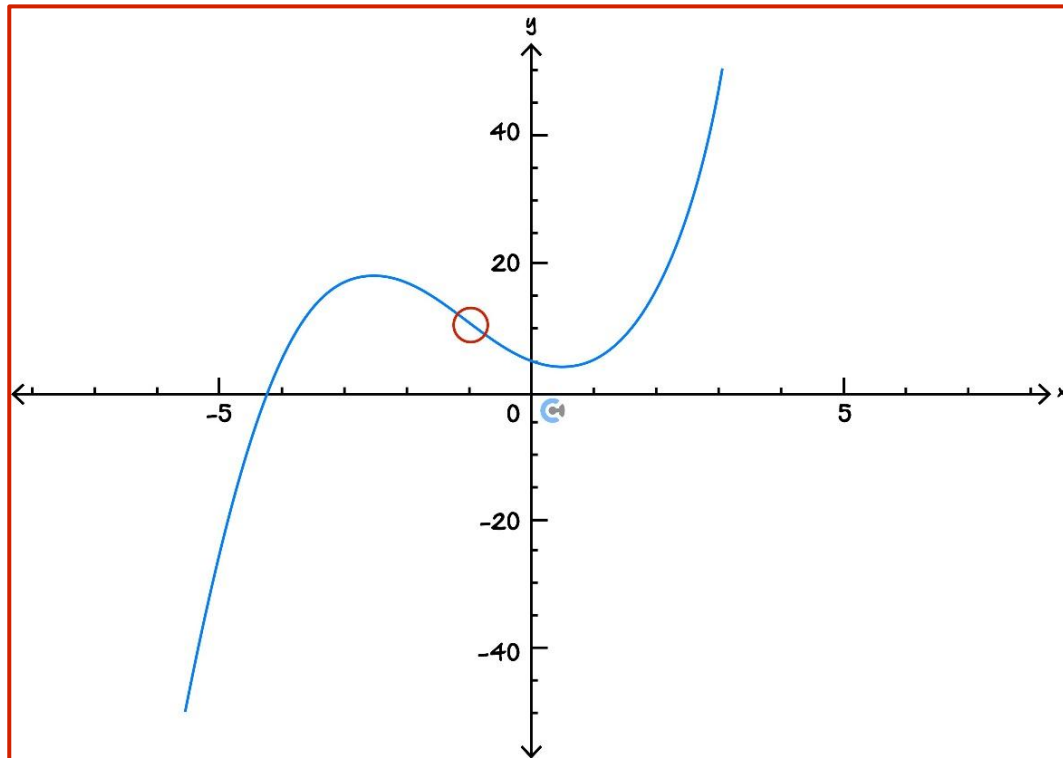
- b. Hence, state the domain of the derivative function. (1 mark)

$$-5 < x < 3$$

Space for Personal Notes

Question 4 (3 marks)

a. Circle the point of inflection on the graph below. (1 mark)



b. State whether at $x = -3$ the gradient is increasing or decreasing. Hence, state the concavity at $x = -3$. (2 marks)

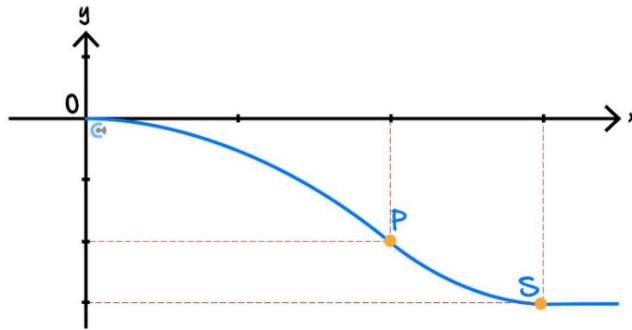
Gradient is decreasing as it is concave down.

Space for Personal Notes

Section B: Extension Test Questions (7 Marks)

Question 5 (7 marks) Tech-Active.

Engineers are designing a track for a new railway station to be built underground.

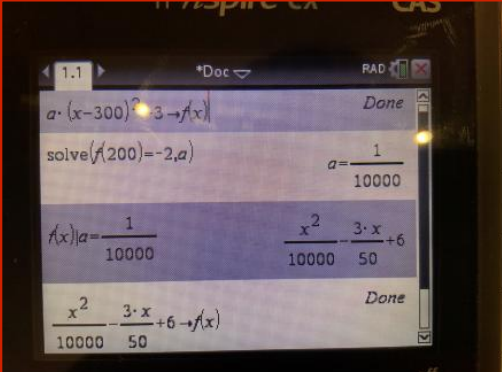


The coordinates of the station, to be positioned at S , are $(300, -3)$. The floor at S is **parallel** to the ground.

Two separate pieces of track OP and PS are to be built, that join smoothly at P : $(200, -2)$.

The rule that defines the track PS is given by $f_2(x) = a(x - h)^2 + k$, where $a, h, k \in \mathbb{R}$.

- a. Solve for the values of a , h and k . (2 marks)

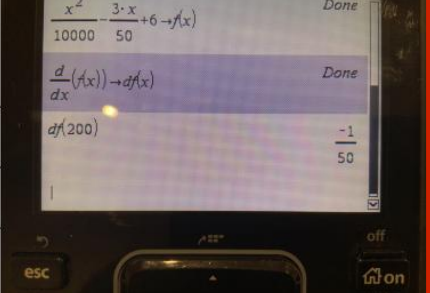


$h = 300$
 $k = -3$
 $a = \frac{1}{10000}$

- b. Find the gradient of the track at point P . (1 mark)

Find the gradient of the track at point P (1 mark)

$f_2'(200) = -\frac{1}{50}$



The rule defining track OP is given by $f_1(x) = mx^2 + nx + k$, where $m, n, k \in \mathbb{R}$.

c. Construct three equations involving m , n and k . (2 marks)

- 1) $f_1(0) = 0$
- 2) $f_1(200) = -2$
- 3) $f_1'(200) = -\frac{1}{50}$; "Join Smoothly"

d. Hence, find the values of m , n and k . (1 mark)

Handwritten solution for part d:

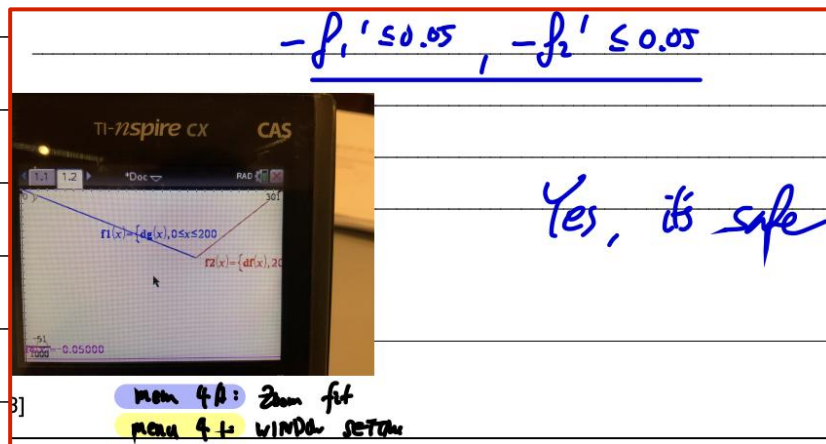
$$\begin{cases} m \cdot x^2 + n \cdot x + k = g(x) \\ \frac{d}{dx}(g(x)) = dg(x) \end{cases}$$

Solve $\begin{cases} g(0)=0 \\ g(200)=-2 \\ dg(200)=df(200) \end{cases}, \{m, n, k\}$

$k=0$ and $m=-\frac{1}{20000}$ and $n=0$

It is considered too dangerous if the magnitude of the gradient of the track exceeds 0.05 at any point.

e. Does the design of this track meet the safety requirements? (1 mark)



Space for Personal Notes

VCE Mathematical Methods $\frac{3}{4}$ Free 1-on-1 Support



Be Sure to Make The Most of These (Free) Services!

- Experienced Contour tutors (45+ raw scores, 99+ ATARs).
- For fully enrolled Contour students with up-to-date fees.
- After school weekdays and all-day weekends.

<u>1-on-1 Video Consults</u>	<u>Text-Based Support</u>
<ul style="list-style-type: none">➤ Book via bit.ly/contour-methods-consult-2025 (or QR code below).➤ One active booking at a time (must attend before booking the next).	<ul style="list-style-type: none">➤ Message +61 440 138 726 with questions.➤ Save the contact as "Contour Methods".

[Booking Link for Consults](https://bit.ly/contour-methods-consult-2025)
bit.ly/contour-methods-consult-2025



[Number for Text-Based Support](tel:+61440138726)
[+61 440 138 726](tel:+61440138726)