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VCE Mathematical Methods ¾
Transformations [0.3]

Workshop



## Section A: Recap

## **Sub-Section**: Image and Pre-Image

T\_\_\_\_\_\_(x', y')



**Image and Pre-Image** 



- The original coordinate is called the \_\_\_\_\_\_.
- The transformed coordinate is called the \_\_\_\_\_\_.

Pre-Image: (x, y)

Image: (x', y')



## **Sub-Section**: Dilation



#### **Dilation**



Dilation by a factor a from the x-axis: y' = ay

Dilation by a factor b from the y-axis: x' = bx

**NOTE:** We are applying the transformations on (x, y) not (x', y').





## **Sub-Section**: Reflection



#### Reflection



Reflection in the *x*-axis: y' = -y

Reflection in the *y*-axis: x' = -x



## **Sub-Section**: Translation



#### **Translation**



Translation by c units in the positive direction of the x-axis: x' = x + c

Translation by d units in the positive direction of the y-axis: y' = y + d





## **Sub-Section**: The Order of Transformations



**The Order of Transformation** 



Order = BODMAS Order

Space for Personal Notes		



## **Sub-Section**: Interpreting the Transformation of Points



#### **Interpretation of Transformations**



 $\blacktriangleright$  When the \_\_\_\_\_\_ x' and y' are the subjects, we can read the transformation \_\_\_\_\_

$$x' = x + 5 \rightarrow 5 \text{ right}$$

- $\blacktriangleright$  When the \_\_\_\_\_\_ x and y are the subjects instead, we must read the transformation in the \_\_\_\_\_ way.
- This includes the order of transformation!

$$x = x' - 5 \rightarrow 5 \text{ right}$$

**NOTE**: This includes the order of transformation!



**TIP:** It is best to make x' and y' the subject before you interpret the transformations.





## **Sub-Section:** Applying Transformations to Functions



#### **Transformation of Functions**



The aim is to get rid of the old variables, x and y, and have the new variables, x' and y', instead.

$$y = f(x) \rightarrow y' = f(x')$$

- Steps:
  - 1. Transform the points.
  - 2. Make x and y the subjects.
  - **3.** Substitute them into the function.



## **Sub-Section**: Finding the Applied Transformations



### Now, let's go backwards!



#### **Reverse Engineering**



- Steps:
  - **1.** Add the dashes (') back to the transformed function.
  - **2.** Make f() the subject.
  - **3.** Equate the LHS of the original and transformed functions to the RHS of the original and transformed functions.
  - **4.** Make x' and y' the subjects and interpret the transformations.



## Section B: Warmup

Question 1		
Consider the transformation:		
	$T: \mathbb{R}^2 \to \mathbb{R}^2, T(x, y) = (2x + 1, 3y - 2)$	
a.	Find the image of the point $P(1,2)$ under $T$ .	
b.	Write out what the transformation T does in the order DRT.	
c.	Find the image of the curve, $y = \frac{1}{3}x^2$ under the transformation T.	



## Section C: Exam 1 (21 Marks)

Question 2 (4 marks)

Let  $f : \mathbb{R} \to \mathbb{R}$ ,  $f(x) = x^2 - 4$ .

**a.** Find the coordinates of all axis intercepts of f. (1 mark)

(-2,0)	(a,-4)
(2,0)	·

- **b.** Let the graph of g be a transformation of the graph of f where the transformations have been applied in the following order:
  - Dilation by a factor of  $\frac{1}{2}$  from the y-axis.
  - $\triangleright$  Dilation by a factor of 3 from the x-axis.
  - Translation 1 unit to the left.

Find the rule for g(x). (2 marks)

3)  $\frac{1}{3}y' = (2(x^{1}+1))^{2} - 4$   $\frac{1}{3}y' = 3y' - 12$   $\frac{1}{3}y' = (2(x^{1}+1))^{2} - 4$   $\frac{1}{3}y' = (2(x^{1}+1))^{2} - 4$   $\frac{1}{3}y' = 3y' - 12$   $\frac{1}{3}y' = 3y' - 12$   $\frac{1}{3}y' = 3y' - 12$ 

**c.** State the coordinates for the axis intercepts of g. (1 mark)

(-2,0)	
(0,0)	



Question 3 (3 marks)

Consider the function:  $f(x) = \frac{1}{2}(x+1)^2 - \frac{3}{2}$ 

Apply the following transformation to f(x):

Dilation by a factor 3 from the *x*-axis.

Translated 4 units in the negative direction of the *x*-axis.

Reflection in the *y*-axis.

Translated 2 units in the positive direction of the *y*-axis.

Dilation by a factor of  $\frac{1}{3}$  from the *y*-axis.

	1
$y = -\frac{1}{2}(x-4)$	3)
3,	$y = \frac{1}{2}(x+1)^2 - \frac{3}{2}$
y = 3y+2	0
	$\frac{4^{1-2}}{3} = \frac{1}{2} \left( -3x^{1} + 4 + 1 \right)^{2} - \frac{3}{2}$
$-3x^{1}=x-4$	3
-31+4=76	$4^{1-2} = \frac{3}{2} (-3x^{1}+5)^{2} = \frac{9}{2}$
$\frac{y_{1-2}}{3} = y$	$y = \frac{2}{3} \left( -3n + 5 \right)^2 - \frac{3}{2}$
	$=\frac{3}{2}(3x-2)^{2}-\frac{2}{2}$



Question 4 (4 marks)

Let 
$$f(x) = \frac{1}{3x+3}$$
.



**a.** The transformation  $T_1$  given by:

$$T_1: \mathbb{R}^2 \to \mathbb{R}^2, T_1(x, y) = (x + a, by),$$

maps the graph of y = f(x) onto the graph of  $y = \frac{1}{x}$ .

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Find the values of a and b. (2 marks)

Dil 3 fran 1c.

 $c = \frac{1}{3}, d = -3.$ 

$$x^{l} = xt!$$

b = 3.

**b.** The transformation  $T_2$  given by:

 $T_2: \mathbb{R}^2 \to \mathbb{R}^2, T_2(x, y) = (c(x+d), y),$ 

maps the graph of  $y = \frac{1}{x}$  onto the graph of y = f(x).

Find the values of c and d. (2 marks)

t	32143= 2
y = 7.	3×1= 11-3
y= <del>3x+3</del> .	$n' = \frac{1}{3}(x-3)$
3213.	



Question 5 (7 marks)

Consider the cubic function:

$$f(x) = \frac{x^3 - 2x^2 - x + 2}{x^3 - x + 2}$$

**a.** Find the x-intercepts of the graph y = f(x). (3 marks)

$f(x) = \frac{x^2(x-2) - (x-2)}{x^2}$	
$= (21^2-1)(21-2)$	
= (1+1)(2-1)(2-2)	
-	
(4,0) (1,0). (2,0)	

Let g(x) = 2f(2x - k).

**b.** Find the transformations required for f(x) to transform to g(x). Give your answer in DRT order. (2 marks)

	Supplies (S)
2f(2n-k)	July Dll 2 from x auch
	Dil & from y aven
2x1-k=x	Trouble & units right.
-2x'=21+14	
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c. Find the value(s) of k such that, there is only one negative x-intercept for g(x). (2 marks)

$$-\frac{1}{2} + \frac{1}{k} < 0, \quad 0 \leq \frac{1}{2} + \frac{1}{k}$$

4 Check the dem of K.

**Question 6** (3 marks)

The image of the curve  $y = \sqrt{16 - x^2}$  under a transformation T, has the equation  $y = \sqrt{55 - 6x - x^2}$ .

Find the transformations that make up T, with dilations before translations.

55-671-×2	y = \[ \( \( \left( \frac{16 - 21^2}{2} \right) \)
$= -\left[ x^2 + 6x - 55 \right]$	
_	y= \( \begin{align*} 64 - (\chi \chi +3)^2 \end{align*}
$= -[(31+3)^2-64]$	
$= (4-(n+3)^2)$	$= 2 \int 16 - \frac{1}{4} (2+3)^2$
	$=2\int_{0}^{\infty} \frac{(2+3)^{2}}{(2+3)^{2}}$
$\frac{x^{1}\pm3}{2}=x$	
	DI 2 from or ach
a +3=2x	Dil 2 for y are
$\alpha' = 2\alpha - 3$	Traveloke 3 units left



### Section D: Tech Active Exam Skills

**Calculator Tip:** Finding Transformed Functions





Save the function as f(x).

Substitute the x and y in terms of x' and y'.

2fc 25 ) ent

Solve for y!

Can also apply the transformations directly to f(x). Must make sure you interpret the transformations correctly or you can easily make a mistake doing this.



#### **Mathematica UDF:**

ApplyTransformList[]

ApplyTransformList[ f[x],  $\{x, y\}$ , list of transforms ]

Applies the list of transforms to f[x] in the chronological order.

ApplyTransformList[ $x^2$ , {x, y}, {x-1, 2x, y+3}]

$$4 + x + \frac{x^2}{4}$$

 $ApplyTransformInvList[f[x], \{x, y\}, \{x-1, 2x, y+3\}]$ 

$$-3 + f[2(-1 + x)]$$

ApplyTransformInvList[Sin[x],  $\{x, y\}$ ,  $\{x - \pi/2, 2y, y - 1\}$ ]

$$\operatorname{Sin}\left[\frac{\mathsf{X}}{2}\right]^2$$

ApplyTransformInvList[]

ApplyTransformInvList[ f[x],  $\{x, y\}$ , list of transforms ]

Applies the list of transforms to f[x] in reverse order and as the inverse to the transforms of ApplyTransformList.

In[ $\circ$ ]:= ApplyTransformInvList[ $x^2$ , {x, y}, {x-1, 2\*x, y+3}]
Out[ $\circ$ ]=

 $1 - 8 x + 4 x^2$ 

ApplyTransformInvList[f[x],  $\{x, y\}$ ,  $\{x-1, 2*x, y+3\}$ ]

-3+f[2(-1+x)]

Sin[x]



#### TI UDF:

Out[0]=

transform()

#### Transform a Function

transform  $\left| \sin(x), x, \left\{ x - \frac{\pi}{2}, 2 \cdot y, y - 1 \right\} \right|$ 

- ▶ Translation  $\frac{\pi}{2}$  units along the neg. x-dir.  $\cos(x)$
- ▶ Dilation by factor of 2 from the x-axis 2·cos(x)
- ▶ Translation -1 unit along the neg. y-dir.
  2·cos(x)-1

#### Overview:

Apply any sequence of transformations to a function. The program will display the transformed function after each step.

#### Input:

#### Other notes:

The list of transformations can either be presented in a (horizontal or vertical) matrix of expressions or a list of expressions



transform\_inv()

#### Invert a Transformation

$$transform_inv(x^2,x,\{x-1,2\cdot x,y+3\})$$

▶ Inverted Transformations:

$$\left\{y-3,\frac{x}{2},x+1\right\}$$

- ▶ Translation -3 units along the neg. y-dir.  $x^2$ -3
- ▶ Dilation by factor of  $\frac{1}{2}$  from the y-axis

$$4 \cdot x^2 - 3$$

▶ Translation 1 unit along the pos. x-dir.

$$4 \cdot x^2 - 8 \cdot x + 1$$

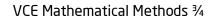
#### Overview:

Find the preimage of a function under a list of transformations. The program will display the list of inverted transformations and the transformed function after each step.

#### Input:

#### Other notes:

The list of transformations can either be presented in a row or column matrix, or a list of expressions





## Section E: Exam 2 (21 Marks)

€(<del>2</del>) ±4.)

#### Question 7 (1 mark)

Find the possible transformation(s) for the function  $f(x) = x^2$  to transform into  $g(x) = 4x^2 + 4$ .

- **A.** Dilation by a factor of 4 from the y-axis, translation of 4 units in the positive direction of the y-axis.
- **B.** Dilation by a factor of 4 from the y-axis, translation of 4 units in the negative direction of the y-axis.
- C. Dilation by a factor of  $\frac{1}{4}$  from the y-axis, translation of 4 units in the positive direction of the y-axis.
- **D.** Dilation by a factor of  $\frac{1}{2}$  from the y-axis, translation of 4 units in the positive direction of the y-axis.

#### Question 8 (1 mark)



Given that f(x) is a function with a local minimum point at (-2,3). The graph of y = -2f(3x + 2) - 2 must have which of the following?

- A. Local minimum at -4-8
- og: f(-21=3
- $3x^{1}+2=x$

**B.** Local minimum at  $\left(-\frac{4}{3}\right)$  – 8).

 $x' = \frac{1}{3}(x-2)$ 

- C. Local maximum at (-4) +8).
- Mer: f(3(=3)+2)
- x1= 3 (2)-2)

**D.** Local maximum at  $\left(-\frac{4}{3}\right)$  -8

# = 4

#### Question 9 (1 mark)

There exists a function where dilating by a factor of 2 from the x-axis gives the same image as dilating it by a factor of  $\frac{1}{4}$  from the y-axis. Which of the following could be the function?

 $\mathbf{A.} \ f(x) = x^2$ 

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**B.**  $f(x) = 2\sqrt{x}$ 

x= 4×

 $\mathbf{C.} \ \ f(x) = \sqrt{x} - 4$ 

 $2 \cdot f(x) = f(4n)$ 

- **D.**  $f(x) = \frac{1}{x}$
- TI: Math, 1) fave each option as for
  - 2) 2 f(x) = f(4x): "True".
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- 1)

2)

(O=O)





Question 10 (1 mark)

Which one of the following sequences of transformations is different from the rest?

- A. Dilation by a factor of 2 from the x-axis, dilation by a factor of  $\frac{1}{3}$  from the y-axis, reflection in the y-axis, translation 2 right, translation 4 up.
- **B.** Dilation by a factor of 2 from the x-axis, dilation by a factor of  $\frac{1}{3}$  from the y-axis, translation 2 left, translation 4 up, reflection in the y-axis.
- C. Reflection in the y-axis, translation 6 left, translation 2 up, dilation by a factor of 2 from the x-axis, dilation by a factor of  $\frac{1}{3}$  from the y-axis.  $x = \frac{1}{3}(-x 6) = -\frac{1}{3}x 2$
- **D.** Translation 6 left, translation 2 up, reflection in the y-axis, dilation by a factor of  $\frac{1}{3}$  from the y-axis, dilation by a factor of 2 from the x-axis.

Question 11 (1 mark)

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The graph of the function f is obtained from the graph of the function g with rule  $g(x) = 3\cos\left(x - \frac{\pi}{6}\right)$  by a dilation of a factor of  $\frac{1}{2}$  from the x-axis, a reflection in the y-axis, a translation of  $\frac{\pi}{6}$  units in the negative x-direction and a translation of 4 upits in the negative y-direction, by that order.

The rule of f is:

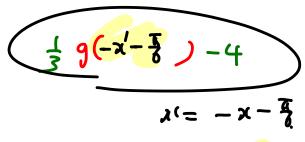
A. 
$$f(x) = \frac{3}{2} \cos\left(-x - \frac{\pi}{3}\right) - 4$$

B. 
$$f(x) = \frac{3}{2} \cos(-x) - 4$$

C. 
$$f(x) = \frac{3}{2}\cos(x) - 4$$

**D.** 
$$f(x) = -3\cos\left(\frac{x}{2} - \frac{\pi}{3}\right) - 4$$

E. 
$$f(x) = \frac{3}{2} \cos\left(-x + \frac{\pi}{3}\right) - 4$$





Question 12 (1 mark)

The curve with the equation  $y = e^x$  is transformed by a dilation from the y-axis by a scale factor of 2, a translation by one unit to the left in the x-direction and a translation of two units downwards in the y-direction. The equation of the transformed curve is:

- **A.**  $y = 0.5e^{x-1} 2$
- **B.**  $y = 2e^{x-1} 2$
- C.  $y = e^{0.5(x+1)} 2$

f( = (x+1)) -2

**D.**  $y = e^{2(x+1)} - 2$ 

**Question 13** (7 marks)

Consider the function,  $f: \mathbb{R} \to \mathbb{R}$ , f(x) = (x-1)(x+1)(2x-1)(x+2).

**a.** State the values of x for which, f(x) = 0. (1 mark)

$$y_{c} = -2, -1, \frac{1}{2}, 1$$

- b. The graph of y = f(x) is translated a units to the right, where  $a \in \mathbb{R}$  to become the graph y = g(x). Find the values of a for which, the graph y = g(x) has:
  - i. Three positive x-intercepts. (2 marks)

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ii. Four negative x-intercepts. (1 mark)

(ta < 0

a <-1



Let h be the function,  $h: \mathbb{R} \to \mathbb{R}$ ,  $h(x) = (x-1)^2(x+2)^2$ , which has a local maximum at



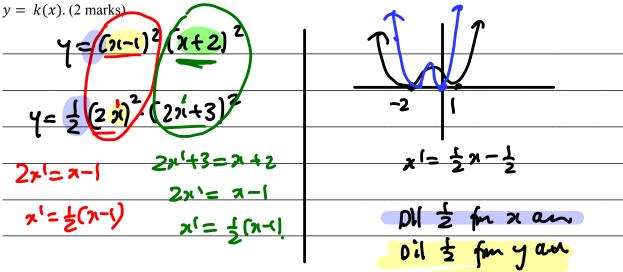
Let k be the function,  $k : \mathbb{R} \to \mathbb{R}$ ,  $k(x) = 2x^2(2x+3)^2$ , which has a local maximum at



**c.** Using translations only, describe a sequence of transformations of k, for which its image would have a local maximum at the same coordinates as that of h. (1 mark)

<u>-3</u> → -½	$\frac{\mathcal{S}I}{32} \rightarrow \frac{\mathcal{S}I}{\mathcal{C}}.$
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**d.** Find a sequence of transformations in the order DRT that maps the graph of y = h(x) to the graph of

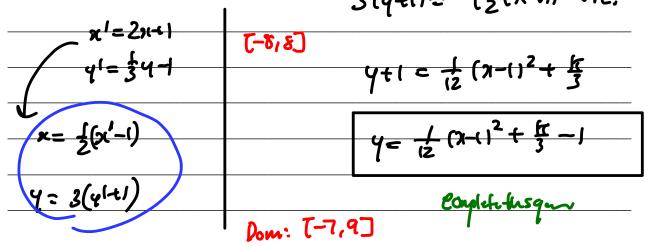




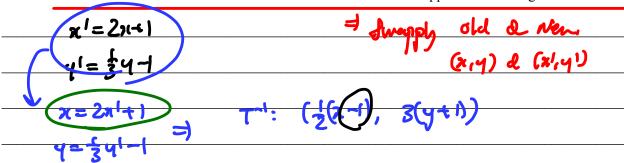
Question 14 (8 marks)

Consider the function,  $f(-4,4] \rightarrow R$ ,  $f(x) = x^2 + k$ , where k is a real number.

a. Consider the transformation,  $T(x,y) = (2x + 1, \frac{1}{3}y - 1)$ . Find the transformed function of y = f(x) under the transformation T, and also state its domain. (3 marks)  $3(y+1) = (\frac{1}{2}(x+1))^2 + K.$ 

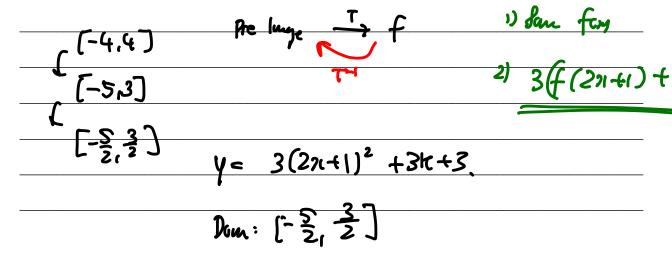


**b.** Find the inverse transformation of T and call it  $T^{-1}$ . (2 marks) **NOTE:** The inverse transformation is a transformation which works in opposite to the original transformation.



c. Using  $T^{-1}$ , find the equation of the pre-image of y = f(x) under the transformation T. State the domain also. (3 marks)

**NOTE:** Pre-image is the function you would have had before the transformation.





## Section F: Extension Exam 1 (14 Marks)

**Question 15** (5 marks)

$$f(x) = (2x)^2 + 4$$

$$g(x) = (4x - 3)^2 - 1$$

or value

a. Identify a sequence of transformations that take f(x) to g(x) without the use of dilation from the y-axis (2 marks)

$y = 2(x)^2 + 4$	12- 18 - 141	x1-3 = >1
y'= (16)(x'-३)2-1	8(4-4)=41+1	

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**b.** Identify a sequence of transformations that take f(x) to g(x) without the use of dilation from the x-axis. (2 marks)

2 x 2,	y valu
y= ([])2+4	
	Translate 5 down
$y' = (421-3)^2 - 1$	Dil 13 y aut
	Trach & ryn.
$4n^{(-3)} = \sqrt{2}n$	
4x'= J2n+3	
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c. Assume that the domain of f and the domain of g are appropriately restricted such that,  $f^{-1}$  and  $g^{-1}$  both exist. Identify the transformations that take  $f^{-1}(x)$  to  $g^{-1}(x)$  without the use of dilation from the x-axis (1 mark)

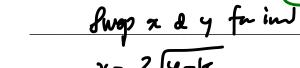
a) $f \rightarrow 5$	1 al 4→	g withat	all feg
Dil 8 from ®	b) ++0	J 14 1	
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f-1 -> g-1. Dil 8 from y	
Transp 33 left	
Tranker of up	

**Question 16** (5 marks)

Consider the function,  $f(x) = 2\sqrt{x - k}$ , where  $k \in R$ .

**a.** Find a sequence of transformations that may  $y = x^2$  o  $y = f^{-1}(x)$ . (2 marks)

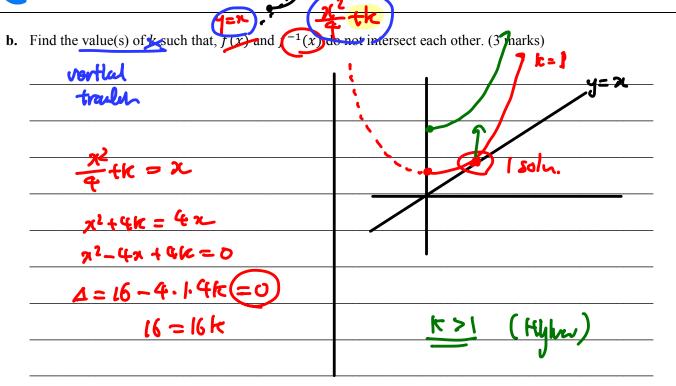


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$$\frac{x^2}{4} = y - k$$

$$=\left(\frac{x}{2}\right)^2+\kappa$$

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#### **Question 17** (4 marks)

The image of the curve,  $y = 3\sqrt{x^2 + 4x + 7} - 1$  under a transformation T, has the equation  $y = \sqrt{4x^2 - 16x + 19}$ . Find the transformations that make up T, with dilations before translations.

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## Section G: Extension Exam 2 (17 Marks)

#### Question 18 (1 mark)

The function tangent to g(x) at x = 1 has an equation y = 2x - 4. What is the equation of the tangent of 2g(2x) + 1 at  $x = \frac{1}{2}$ ?

- **A.** y = 4x 4
- **B.** y = 4x 5
- C. y = 8x 7
- **D.** y = 8x 11

#### Question 19 (1 mark)

The transformation which maps  $f(x) = \log_2(x)$  to  $g(x) = 2\log_2(2x)$  is:

- A. Dilated by factor 2 from the x-axis, translated 2 units in the positive direction of the y-axis.
- **B.** Dilated by factor 2 from the x-axis, dilated by factor 2 from the y-axis.
- C. Dilated by factor 2 from the x-axis, translated 1 unit in the positive direction of the y-axis.
- **D.** Dilated by factor 2 from the x-axis, dilated by factor  $\frac{1}{2}$  from the y-axis.

#### **Question 20** (1 mark)

The transformation,  $T: \mathbb{R}^2 \to \mathbb{R}^2$ , which maps the graph of  $y = 3 - \sqrt{\frac{x+1}{2}}$ , onto the graph of  $y = \sqrt{x}$  has the rule:

- **A.** T(x,y) = (2x + 1, -y 3)
- **B.**  $T(x,y) = \left(\frac{x+1}{2}, 3-y\right)$
- C. T(x,y) = (2x 1,3 y)
- **D.**  $T(x,y) = \left(\frac{x+1}{2}, -y 3\right)$



#### Question 21 (1 mark)

The image of the curve,  $y = \sqrt{x^2 + 4}$  under the transformation T, has the equation  $y = \sqrt{x^2 + 4x + 40}$ . The transformation T could be described as:

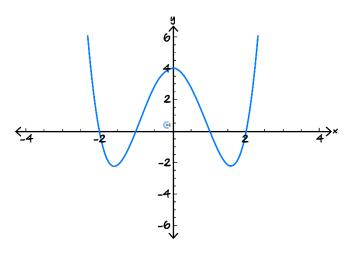
- **A.** A dilation by factor 3 from the y-axis followed by dilation by factor 2 from the x-axis and a translation 3 units to the right.
- **B.** A dilation by factor  $\frac{1}{3}$  from the *y*-axis followed by a dilation by factor 3 from the *x*-axis and a translation 2 units to the right.
- C. A dilation by factor 2 from the y-axis followed by a dilation by factor 3 from the x-axis and a translation 2 units to the left.
- **D.** A dilation by factor 3 from the y-axis followed by a dilation by factor 3 from the x-axis and a translation 2 units to the left.

2	Space for Personal Notes



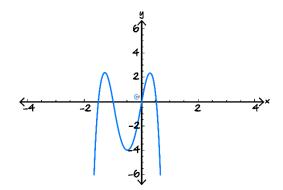
Question 22 (1 mark)

Part of the graph of y = f(x) is shown below.

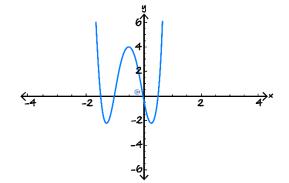


The corresponding part of the graph of y = -f(2x - 1) is best represented by:

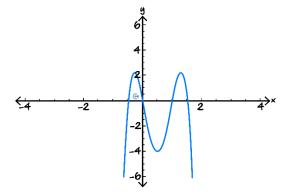
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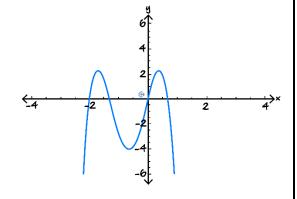
В.



C.



D.





Question 23 (12 marks)

Let  $f(x) = \log_e(x+3) + \log_e(x)$ .

**a.** State the domain of f(x). (1 mark)

Consider the function  $f_1$  where,  $f_1(x) = \log_e(x + 3 + k) + \log_e(x + k)$  and k is a negative real constant.

**b.** State the transformation required to get the graph of f to the graph of  $f_1$ . Give your answer in terms of k. (1 mark)

c. When k = -2, the line  $y = \frac{5x}{4} - \frac{15}{4} + \log_e(4)$  is tangent to the graph of  $y = f_1(x)$  when x = 3. When k = -3, find the equation of the line that is tangent to the graph of  $y = 2f_1(x) + 1$  when x = 4. (2 marks)

**d.** Find the value of x for which,  $f_1'(x) = 1$ . Express your answer in terms of k. (2 marks)



ov	w consider the function $f_2$ where, $f_2(x) = \log_e\left(\frac{x}{a} + 3\right) + \log_e\left(\frac{x}{a}\right)$ and $a$ is a positive real constant.
ov	we consider the function $f_2$ where, $f_2(x) = \log_e\left(\frac{x}{a} + 3\right) + \log_e\left(\frac{x}{a}\right)$ and $a$ is a positive real constant. State the transformation required to get the graph of $f$ to the graph of $f_2$ . Give your answer in terms of $a$ (1 mark)
	State the transformation required to get the graph of $f$ to the graph of $f_2$ . Give your answer in terms of $a$



	point of intersection	. Give your answers	$df_2^{-1}$ have only one correct to three dec	e point of intersect cimal places. (3 ma	ion. Give the coor	rdinate
pace for	Personal Notes					



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