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VCE Mathematical Methods ½

AOS 1 Revision [1.0]

Contour Check Part 1



Contour Check

[1.1] - Linear & Coordinate Geometry (Checkpoints)

- [1.1.1] - Solve and Graph Linear Equations and Inequalities Pg 3-5
- [1.1.2] - Find the Midpoint and Distance Between Two Points or Functions Pg 6-7
- [1.1.3] - Find Parallel and Perpendicular Lines Pg 8-9
- [1.1.4] - Finding the Angle Between a Line and the x -axis or Between Two Lines Pg 10-11
- [1.1.5] - Find the Unknown Value For a System of Linear Equations Pg 12-15

[1.2] - Linear & Coordinate Geometry Exam Skills (Checkpoints)

- [1.2.1] - Applying Midpoint to Find Reflected Points Pg 16-17
- [1.2.2] - Find Vertical and Horizontal Distance Between Functions Pg 18-19
- [1.2.3] - Finding Distance Between a Point and a Function Pg 20-21

[1.3] - Quadratics (Checkpoints)

- [1.3.1] - Rewriting Quadratics in Different Forms Pg 22-25
- [1.3.2] - Find Solutions and Number of Solutions to Quadratic Equations Pg 26-29
- [1.3.3] - Graph and Find Rules From the Graph of Quadratic Equations Pg 30-33
- [1.3.4] - Solving Quadratic Inequalities and Hidden Quadratics Pg 34-36

[1.4] - Quadratics Exam Skills (Checkpoints)

- [1.4.1] - Find Turning Point Form Using Turning Points Pg 37-38
- [1.4.2] - Apply Quadratics to Model a Scenario Pg 39-40
- [1.4.3] - Apply Family of Functions to Find an Unknown of Function Pg 41-42
- [1.4.4] - Harder Quadratic Inequalities Pg 43-44

[1.5] - Polynomials (Checkpoints)

- [1.5.1] - Identify the Properties of Polynomials and Solve Long Division Pg 45-47
- [1.5.2] - Apply Remainder and Factor Theorem to Find Reminders and Factors Pg 48-51
- [1.5.3] - Find Factored Form of Polynomials Pg 52-54
- [1.5.4] - Graph Factored and Unfactored Polynomials Pg 55-61

[1.6] - Polynomials Exam Skills (Checkpoints)

- [1.6.1] - Solve Polynomial Inequalities Pg 62-65
- [1.6.2] - Solve Number of Solution Problems Pg 66-70
- [1.6.3] - Apply Bisection Method to Approximate x -Intercepts Pg 71-72

[1.1 - 1.6] - Exam 1 Overall Pg 73-90

Section A: [1.1] - Linear & Coordinate Geometry (Checkpoints)

Sub-Section [1.1.1]: Solve and Graph Linear Equations and Inequalities



Question 1



Solve the following linear equations and inequalities for x :

a. $3x + 8 = 20$

b. $2x + 6 = 3(x - 2)$

c. $5x + 2 < 4x + 10$

Question 2



Solve the following linear equations and inequalities for x :

a. $3x + 2 = 12x + 3$

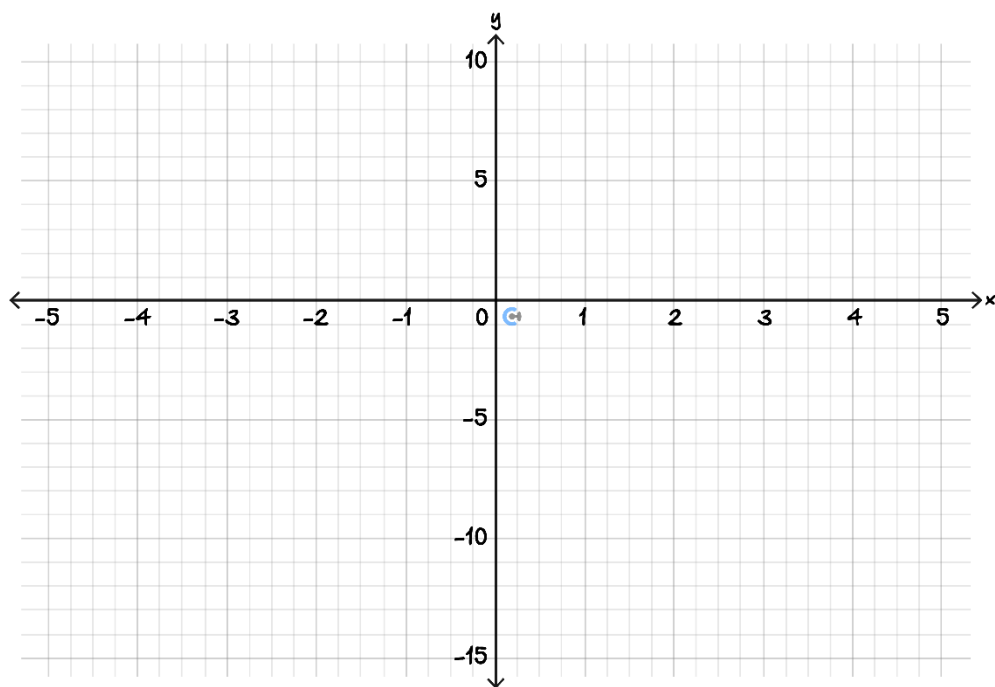
b. $\frac{2x+3}{3} > 3(x-5)$

c. $\frac{5x+3}{4} \leq 10x+8$

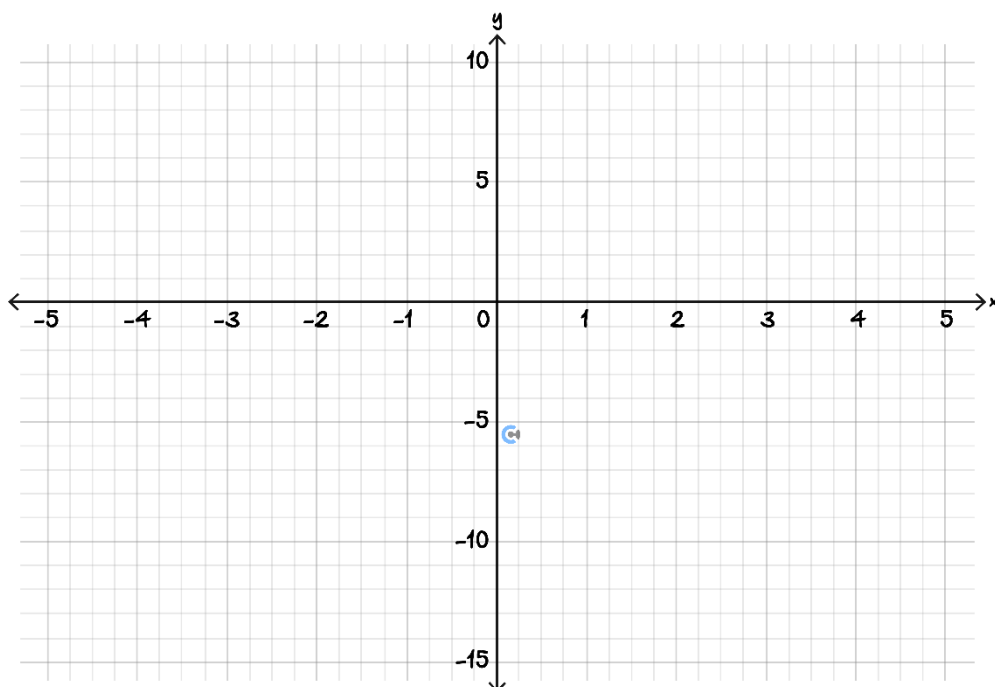
Question 3



- a. Sketch the line governed by the equation $2y - 4x = -8$ on the axis below. Label all axes intercepts.



b. Shade the region governed by the equation $2y - 4x > -8$ on the axis below.



Question 4



Solve the inequality $\frac{1}{4}(5x - 3) \geq 2x + 8$ for x .

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Sub-Section [1.1.2]: Find The Midpoint and Distance Between Two Points or Functions

Question 5



- a. Find the midpoint of $(1, -3)$ and $(6, -10)$.

- b. The points (a, b) and $(3, 4)$ have a midpoint $(2, 3)$. Find the values of a and b .

Question 6



- a. Find the distance between points $(2, 5)$ and $(5, 2)$.

- b. The curve $y = (x - 1)^2 + k$ and the line $y = 3$ has a minimum vertical distance of 4. Find the value of k .

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Question 7


The distance between the point $(2, 2)$ and a point P on the line $y = 2x + 2$ is 4 units. Find all possible coordinates for P .

Question 8


The distance between the point $(1, 2)$ and a point P on the line $y = 3x - 1$ is 4 units. Find all possible coordinates for P .

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Sub-Section [1.1.3]: Find Parallel and Perpendicular Lines

Question 9



State whether the following lines are parallel or perpendicular:

a. $y = 3x + 1$ and $y = 3x + 3$

b. $y = 2x + 3$ and $y = -\frac{1}{2}x + 2$

Question 10



Find the equation of the line that is parallel to the line $y = 2x + 1$ and passes through the point $(5, 2)$.

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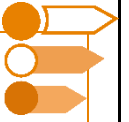
Question 11


Find the equation of the line that is perpendicular to $y = 3x + 6$ and passes through the point $(6, 3)$.

Question 12


Find the equation of the line that is perpendicular to $y = \sqrt{3}x + 1$ and passes through the point $(2, 4)$.

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Sub-Section [1.1.4]: Finding The Angle Between a Line and the x -axis or Between Two Lines

Question 13



Find the angle that $y = -x + 1$ makes with the positive direction of the x -axis.

Question 14



A line that makes an angle of 30° with the positive x -axis passes through the point $(1, 1)$. Find the equation of the line.

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Question 15


It is known that the lines $y = mx + 3$ and $y = 4x - 2$ make an angle of 45° when they intersect. Find all possible values of m .

Question 16


Find the acute angle made between the lines $y = \sqrt{3}x + 1$ and $y = \frac{x}{\sqrt{3}} - 1$. Give your answer in degrees correct to two decimal places.

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Sub-Section [1.1.5]: Find The Unknown Value for a System of Linear Equations

Question 17



Consider the simultaneous linear equations:

$$y = kx + 6$$

$$y = 2x + 5$$

Where $x, y \in R$ and k is a real constant.

- a.** Find the value(s) of k for which the system of equations has no solution.

- b.** Find the value(s) of k for which the system of equations has infinitely many solutions.

- c.** Find the value(s) of k for which the system of equations has a unique solution.

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Question 18

Consider the simultaneous linear equations:

$$-3kx + y = k$$

$$-3x + ky = -1$$

Where $x, y \in R$ and k is a real constant.

- a.** Find the value(s) of k for which the system of equations has no real solution.

- b.** Find the value(s) of k for which the system of equations has infinitely many solutions.

- c.** Find the value(s) of k for which the system of equations has a unique solution.

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Question 19

Consider the simultaneous linear equations:

$$kx + y = 2$$

$$2x + (k - 2)y = 4$$

Where $x, y \in R$ and k is a real constant.

- a.** Find the value(s) of k for which the system of equations has no real solution.

- b.** Find the value(s) of k for which the system of equations has infinitely many solutions.

- c.** Find the value(s) of k for which the system of equations has a unique solution.

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**Question 20**

Consider the simultaneous linear equations:

$$(k - 2)x + 3y = 5$$

$$4x + (k + 1)y = k + 7$$

Where $x, y \in R$ and k is a real constant.

Find the value(s) of k for which the system has no real solution.

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Section B: [1.2] - Linear & Coordinate Geometry Exam Skills (Checkpoints)

Sub-Section [1.2.1]: Applying Midpoint to Find Reflected Points



Question 21



Find the reflection of the point $(4, 6)$ about the line $y = 4$.

Question 22



The point $(3, 2)$ is reflected in the line $y = b$, and to become the point $(3, -6)$. Find the value of b .

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Question 23


Consider the function $f(x) = x^2 + 1$.

- a. The point $A(1, 1)$ on the graph of $y = f(x)$ is reflected about the line $y = 0$. Find the coordinates of the reflected points' position.

- b. The entire graph of $y = f(x)$ is reflected about the line $y = 0$. Find the equation of this new graph.

Question 24


The function $y = (x - 1)^2 + 3$ is reflected about the line $x = 3$ and then reflected about the line $y = 2$. Find the equation of the graph after these reflections.

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Sub-Section [1.2.2]: Find Vertical and Horizontal Distance Between Functions

Question 25



Find the vertical distance between $f(x) = 3x + 1$ and $g(x) = x + 3$ when $x = 2$.

Question 26



Find the horizontal distance between the function $f(x) = x + 1$ and $g(x) = x^2 - 1$ when $y = 8$.

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Question 27

Consider the functions $y = x + 3$ and $y = x^2 + 1$.

- a. Solve the inequality $x + 3 > x^2 + 1$.

- b. Hence, determine the vertical distance between the two functions when $x = 1$.

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Sub-Section [1.2.3]: Finding Distance Between a Point and a Function

Question 28



Find the distance between the point $(1, 2)$ and the function $y = x^2$, when $x = 3$.

Question 29



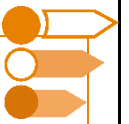
The distance between the point $A(4, 1)$ and the point $B(-3, m)$ is 7, find the possible value(s) of m .

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Question 30


Find the point(s) on the line $y = 3x + 3$ which have a distance of 5 from the point $(1, 1)$.

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Section C: [1.3] - Quadratics (Checkpoints)**Sub-Section [1.3.1]: Rewriting Quadratics in Different Forms****Question 31**

Find the factorised forms of these quadratics:

a. $x^2 - 4$

b. $x^2 - 3x$

c. $5x^2 + 10x$

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Question 32

- a. Express $x^2 + 4x + 3$ in intercept form, $(a(x - b)(x - c))$.

- b. Express $x^2 - 2x + 3$ in turning point form, $(a(x - h)^2 + k)$.

- c. Factorise $x^2 + 6x + 9$.

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Question 33

a. Factorise $3x^2 - 12x - 15$.

b. Express $2x^2 - 12x + 9$ in turning point form.

c. Express $2(x - 1)(x + 3)$ in turning point form.

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Question 34


Factorise $6x^2 - \sqrt{5}x - 5$.

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Sub-Section [1.3.2]: Find Solutions and Number of Solutions to Quadratic Equations

Question 35



Find all real solutions to the following equations:

a. $x^2 = -5x$

b. $4x^2 - 16 = 0$

c. $2x^2 - 18x = 0$

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Question 36

- a. Find all real solutions to the equation $x^2 - 10x + 25 = 0$.

- b. How many solutions does the equation $x^2 + 2x - 15$ have?

- c. Find all real solutions to the equation $3(x + 1)^2 = 12$.

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Question 37

- a. Find all real solutions to the equation $x^2 - 6x = 4$.

- b. For what values of a does the equation $ax^2 - 6x = 18$ have no real solutions?

c. Find all real solutions to the equation $5x^2 + 20x = 15$.

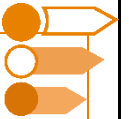
Question 38



For what values of b does the equation $2x(b - x) = 5$ have no real solutions?

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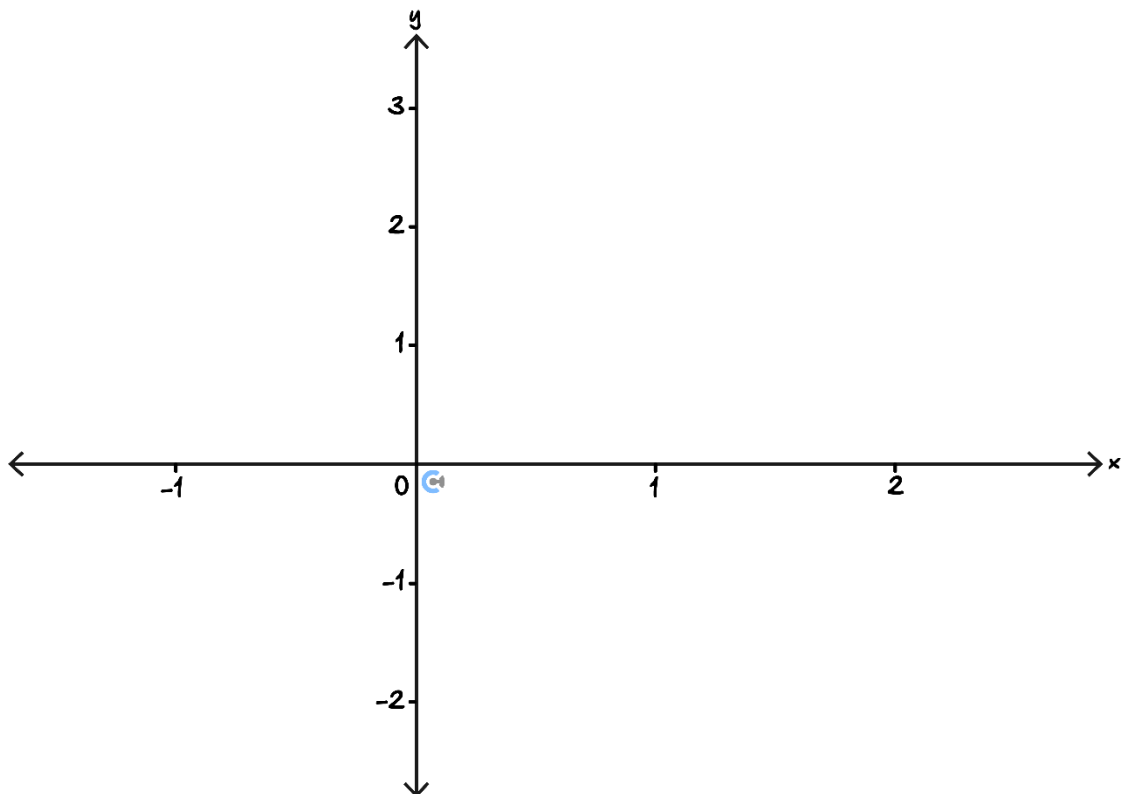
Sub-Section [1.3.3]: Graph and Find Rules From the Graph of Quadratic Equations



Question 39



Sketch the graph of $y = (x + 1)(x - 2)$ on the axis below.

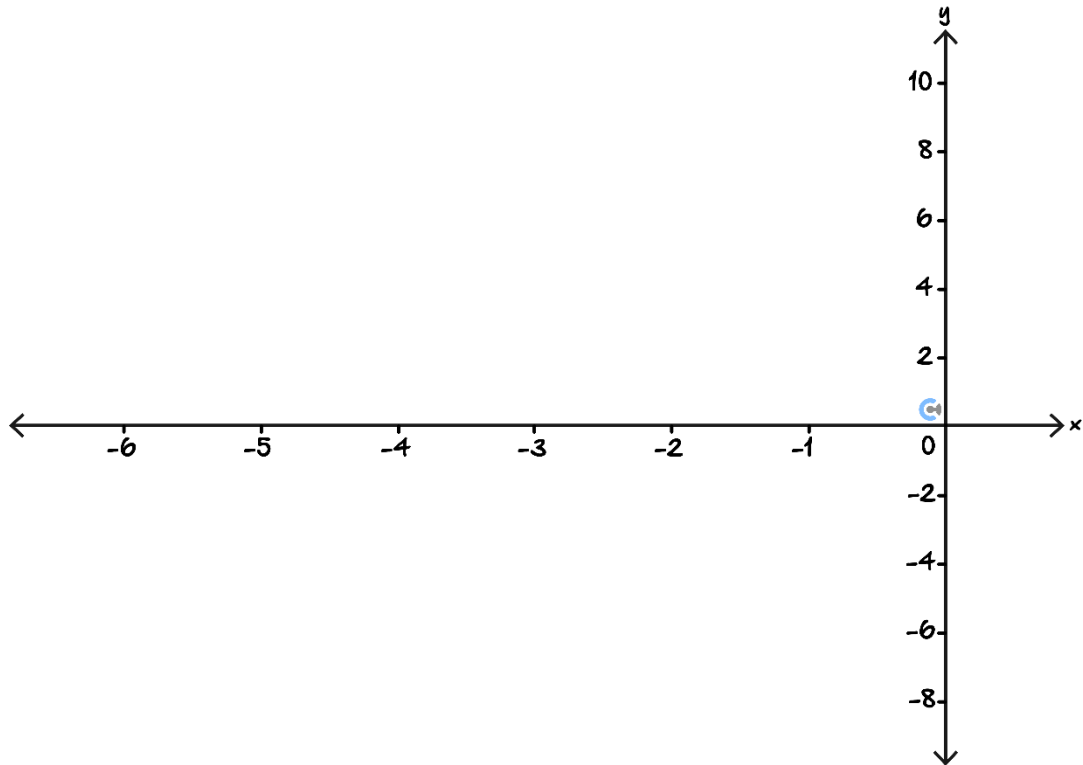


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Question 40



Sketch the graph of $y = 2(x + 3)^2 - 8$ on the axis below, labelling axis intercepts and turning points with their coordinates.

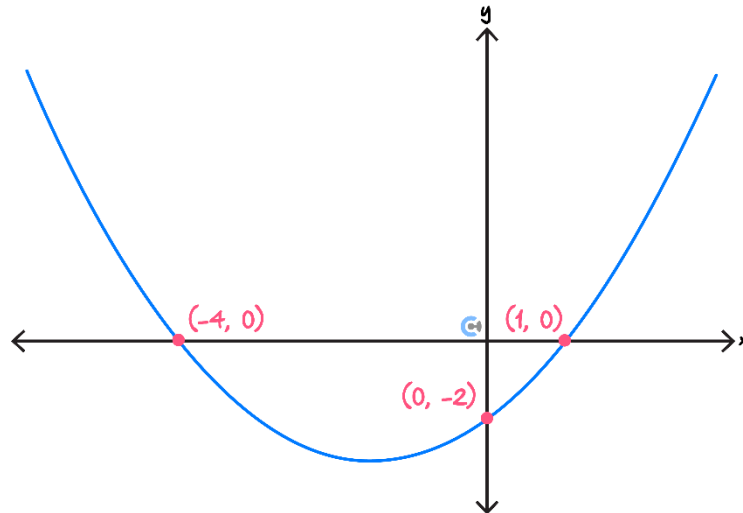


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Question 41

The graph of a parabola is shown below.

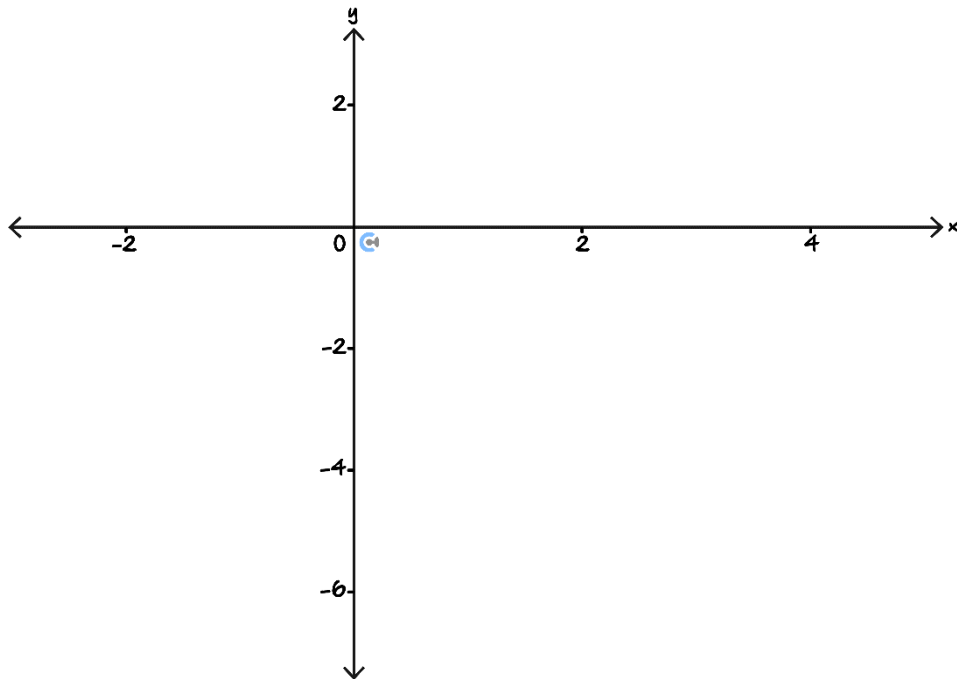


Find the rule of this parabola.

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Question 42

Sketch the graph of $3y = 5 - (x - 1)^2$ on the axis below, labelling axis intercepts and turning points with their coordinates.



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Sub-Section [1.3.4]: Solving Quadratic Inequalities and Hidden Quadratics



Question 43



a. Solve $x^2 > 1$ for x .

b. Solve $x(x - 2) \leq 3$ for x .

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Question 44


Solve $(x - 1)^4 - (x - 1)^2 = 12$ for x .

Question 45


Solve $x^2 + 6x + 8 \geq 2$ for x .

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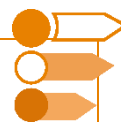
Question 46


For what values of x is $ax^2 + bx + c < d$, where $a, b, c, d \in R$, $a < 0$ and $c > d$?

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Section D: [1.4] - Quadratics Exam Skills (Checkpoints)

Sub-Section [1.4.1]: Find Turning Point Form Using Turning Points



Question 47



Find the turning point of the parabola $y = 2(x - 1)^2 + 3$.

Question 48



Find the equation of a parabola that has a turning point at $(5, 3)$ and has a y -axis intercept of 8.

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Question 49

Find the turning point of the parabola $y = 2x^2 - 4x + 5$.

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Sub-Section [1.4.2]: Apply Quadratics to Model a Scenario

Question 50



A ball is thrown up into the air from a height of 1 metre. It reaches its maximum height of 2 metres after 1 second. The height in metres of the ball h , t seconds after the ball is launched is:

$$h(t) = a(t - 1)^2 + 2$$

Find the value of a .

Question 51



A parabola-shaped bridge is used to cross a long river. The height of the bridge above the water level in metres, h , is a quadratic function of the horizontal distance of a point of a bridge from the starting river bank, x .

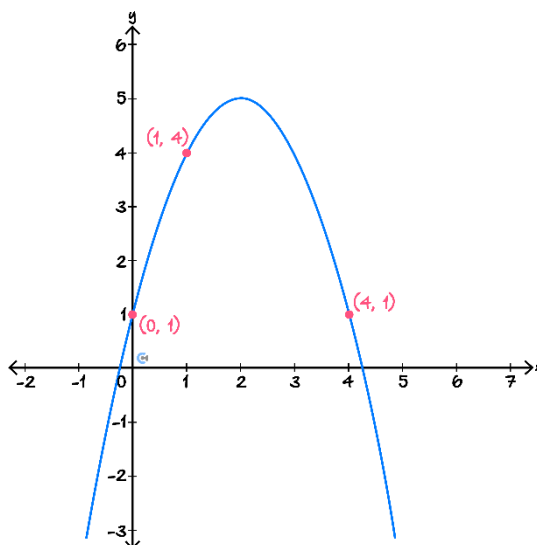
At the starting river bank, the height of the bridge is 2 metres above water level, and 5 metres away from the starting point ($x = 5$), the bridge is at its highest point, 6 metres above the water level ($h = 6$).

Relate x and h .



Question 52

A river passes through 3 points in a park as shown below:



Where the x -axis represents the position due east from the centre of the park, and the y -axis represents the position due north from the centre of the park. We can relate the north position (y) of the river to the east position (x) of the river through the equation:

$$y = ax^2 + bx + c$$

Find the values of a , b and c .



Sub-Section [1.4.3]: Apply Family of Functions to Find an Unknown of Function

Question 53



Consider the parabola $y = kx^2 - 6$. Find the value(s) of k such that the horizontal distance between x -axis intercepts of the parabola is less than 4.

Question 54



Let $y = x^2 + 4kx - 1$. Find the values of k such that $y \geq -2$ for all x .


Question 55

Find all values of k such that the equation $(x - k - 1)^2 - 4 = k$ has two real solutions for x , one positive and one negative.

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Sub-Section [1.4.4]: Harder Quadratic Inequalities

Question 56



Solve $x(x + 3) > 4$ for x .

Question 57



Solve $1 + \frac{2}{x-2} \leq \frac{5}{(x-2)^2}$ for x .

Question 58


Solve $(x^2 + 2)^2 - 4 \geq 8x^2$ for x .

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Section E: [1.5] - Polynomials (Checkpoints)

Sub-Section [1.5.1]: Identify the Properties of Polynomials and Solve Long Division



Question 59



Consider the polynomial $f(x) = 3x^2 - 4x^4 + 1 - 2x$.

a. State the degree of $f(x)$.

b. State the leading coefficient of $f(x)$.

c. State the constant term of $f(x)$.

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Question 60


Simplify the following using polynomial long division:

$$\frac{x^3 + 2x^2 - 5x - 6}{x - 2}$$

Question 61


The polynomial $P(x) = x^4 - 2x^2 - 5x + 3$ can be written in the form $P(x) = Q(x)(x - 2) + r$, where $r \in R$ and $Q(x)$ is a real valued polynomial. Find $Q(x)$ and r .


Question 62

The polynomial $P(x) = 2x^4 + 3x^3 - 5x + 1$ can be written in the form $P(x) = Q(x)(x^2 - 2x + 3) + R(x)$, where $R(x)$ is a polynomial of degree 1 and $Q(x)$ is a polynomial.

- a.** State the degree of $Q(x)$.

- b.** Find $Q(x)$ and $R(x)$.

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Sub-Section [1.5.2]: Apply Remainder and Factor Theorem to Find Reminders and Factors

Question 63



Find the remainder of the division $\frac{f(x)}{g(x)}$, where:

a. $f(x) = x^3 - 7x + 8$ and $g(x) = x + 3$.

b. $f(x) = 2x^3 - 6x^2 - 2x + 4$ and $g(x) = x - 1$.

c. $f(x) = -3x^3 + 8x^2 - 3x + 2$ and $g(x) = 3x + 1$.

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Question 64

For the polynomial $f(x) = ax^3 + 2x^2 - 3ax + 1$, we get a remainder of 5 when $f(x)$ is divided by $x + 2$. Find the value of a .

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Question 65



Consider the expression:

$$f(x) = 2x^3 - ax^2 + b$$

Where a and b are non-zero constants.

It is known that $x + 1$ is a factor of $f(x)$ and that the remainder when $f(x)$ is divided by $x - 2$ is 3. Find the values of a and b .

[illegible]

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Question 66

Find a cubic polynomial $f(x)$ which has the following properties:

- $f(x)$ has a leading coefficient of -2 .
- $f(x)$ divided by $x^2 - 1$ leaves a remainder of 1 .
- $x - 3$ is a factor of $f(x)$.

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Sub-Section [1.5.3]: Find Factored Form of Polynomials

Question 67



Factorise $x^3 - 2x^2 - x + 2$ as a product of three linear factors.

Question 68



Factorise $x^3 - 6x^2 + 3x + 10$ as a product of three linear factors.


Question 69

Factorise $2x^3 + \frac{25x^2}{3} + x - \frac{4}{3}$ as a product of three linear factors.

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Question 70

Use the fact that $x^n - 1 = (1 + x + x^2 + \dots + x^{n-1})(x - 1)$ to factorise $1 + x^2 + x^4 + x^6 + x^8$ as a product of two-degree four polynomials.

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Sub-Section [1.5.4]: Graph Factored and Unfactored Polynomials

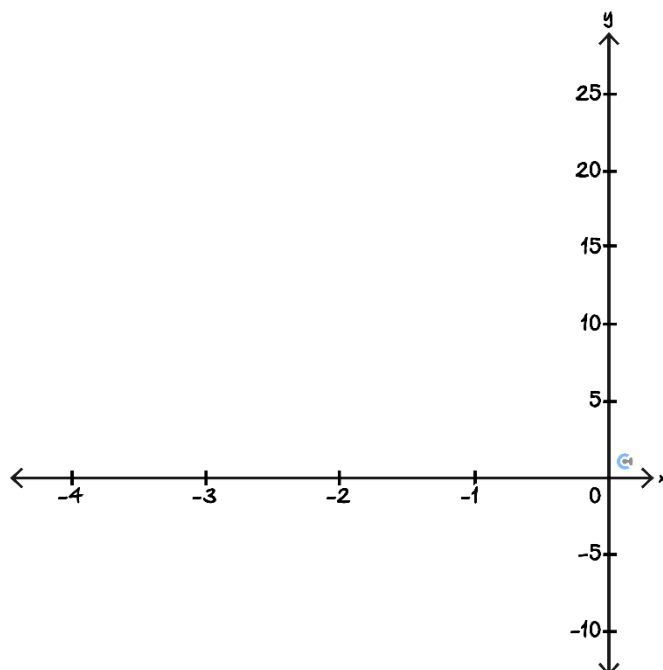


Question 71

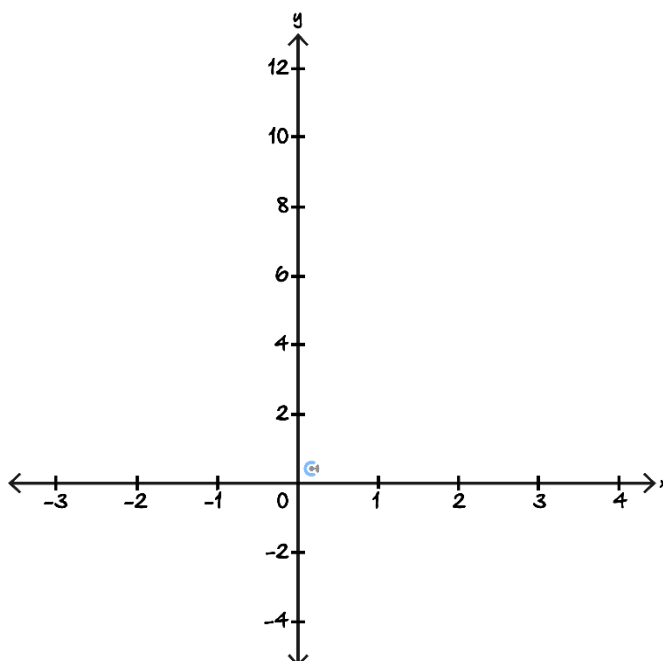


Sketch the graphs of each of the functions on the axes provided.

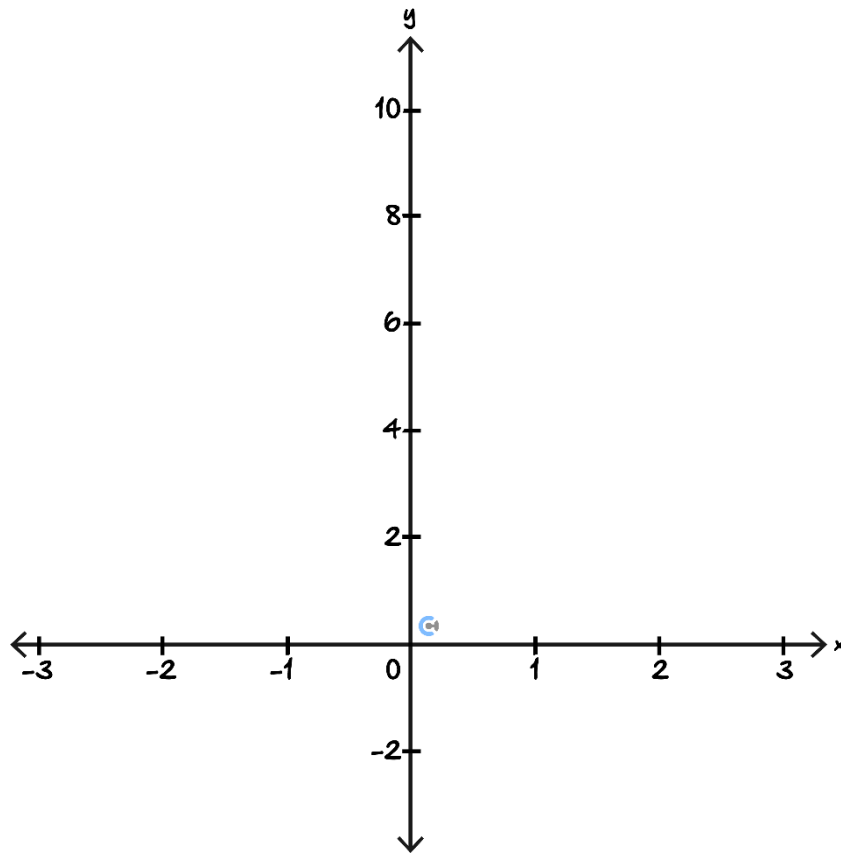
a. $y = 8 - (x + 2)^3$



b. $y = (x - 1)(x + 2)(x - 3)$



c. $y = 2 + (x - 1)^4$

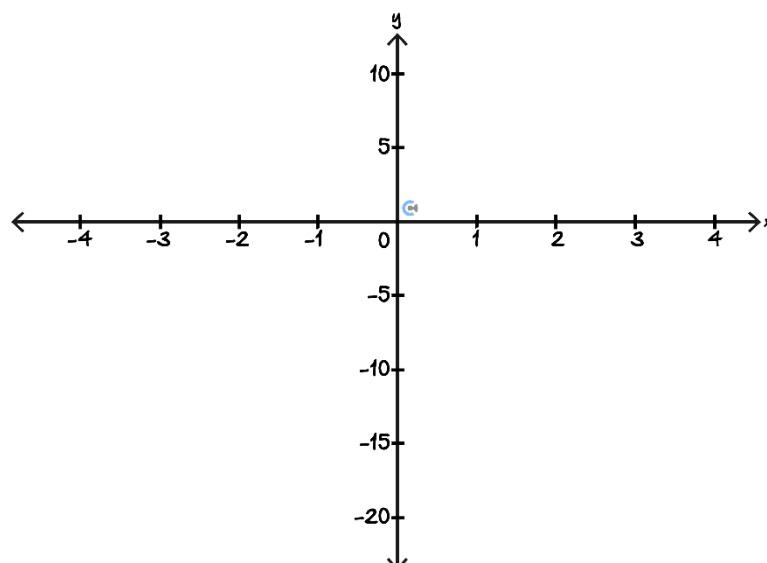


Question 72

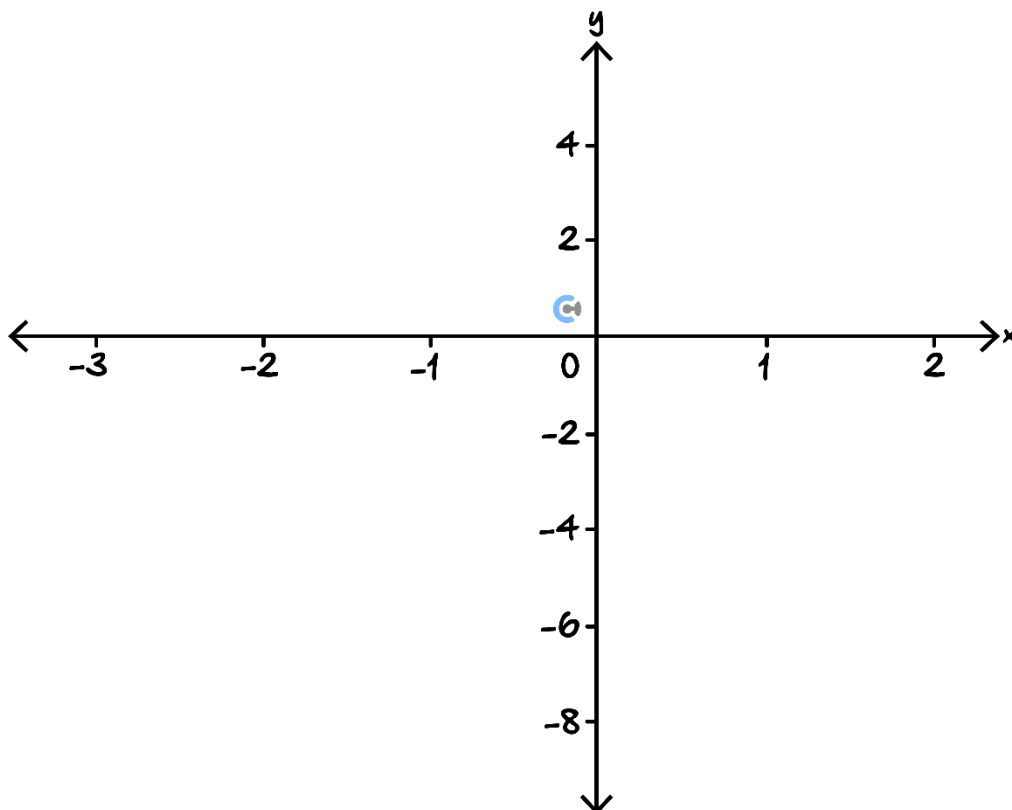


Sketch the graphs of each of the functions on the axes provided.

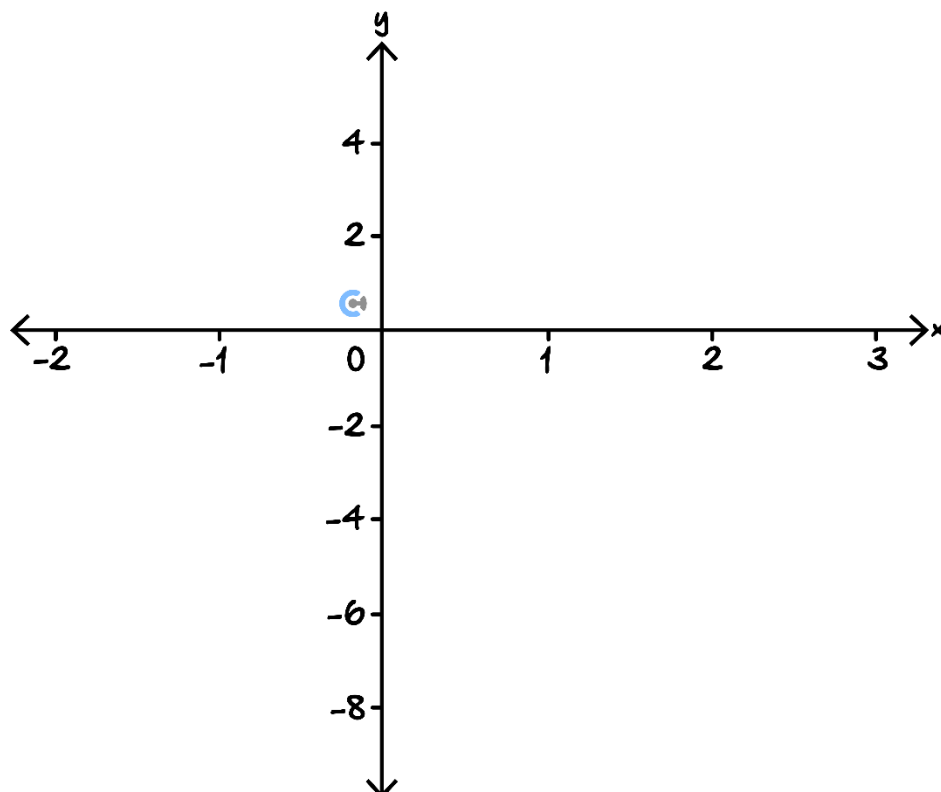
a. $y = (x + 3)^2(x - 2)$



b. $y = (x - 1)(x + 2)^3$



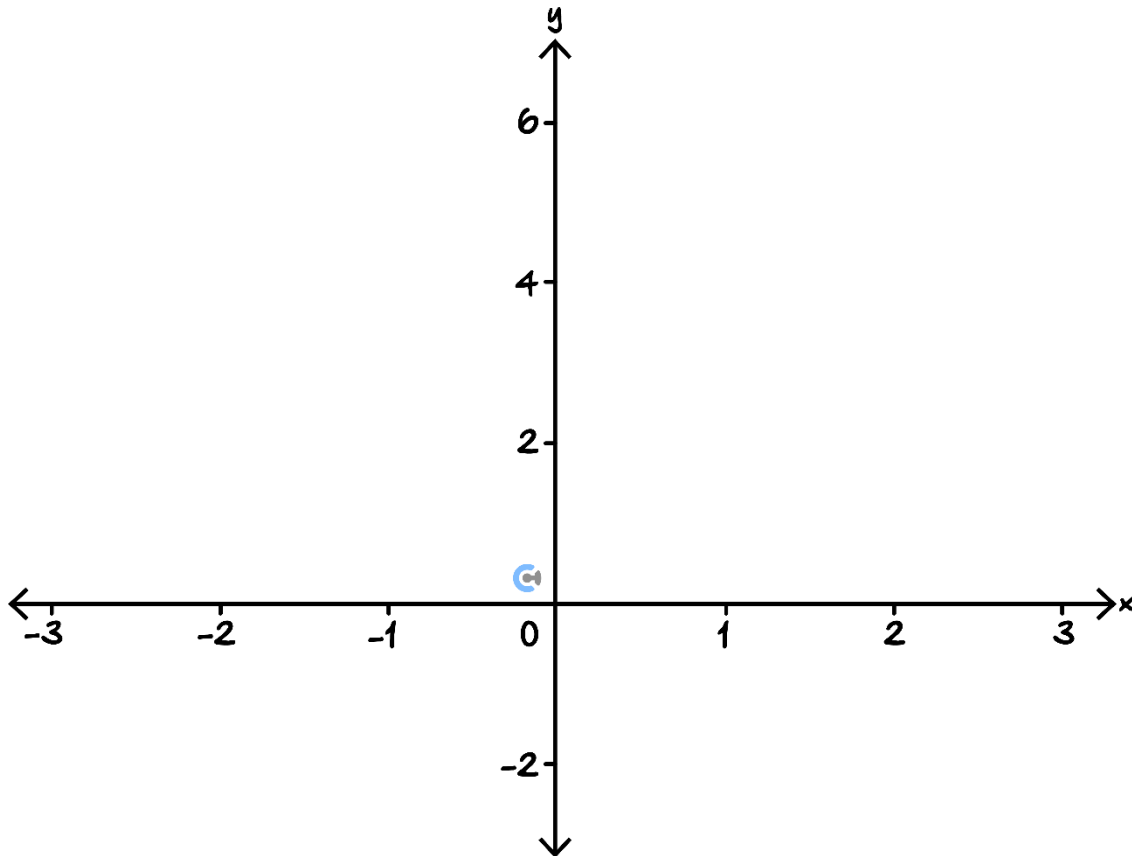
c. $y = (x + 1)^2(x - 3)^3$



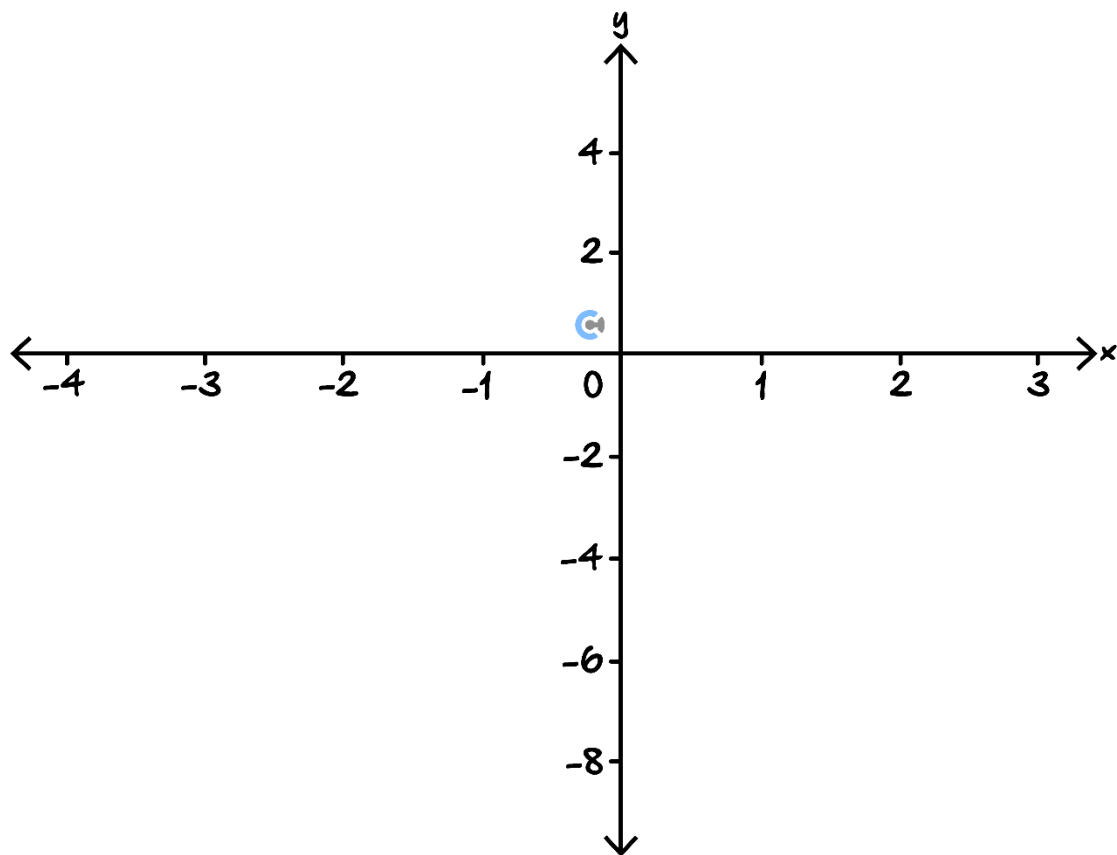

Question 73

Factorise and hence, sketch the graphs of each of the functions on the axes provided.

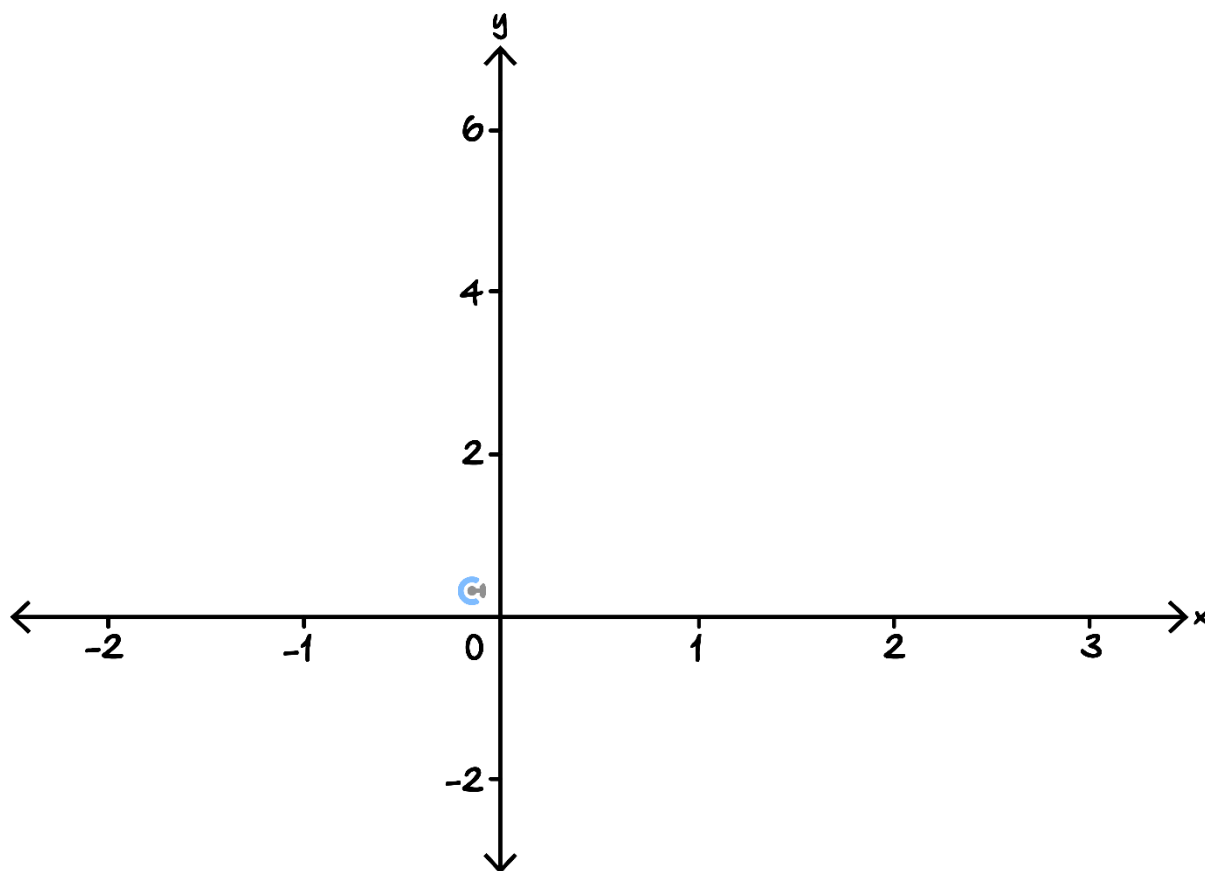
a. $y = x^3 - x^2 - 4x + 4$



b. $y = x^3 + 2x^2 - 5x - 6$



c. $y = x^4 - 2x^3 - 3x^2 + 4x + 4$



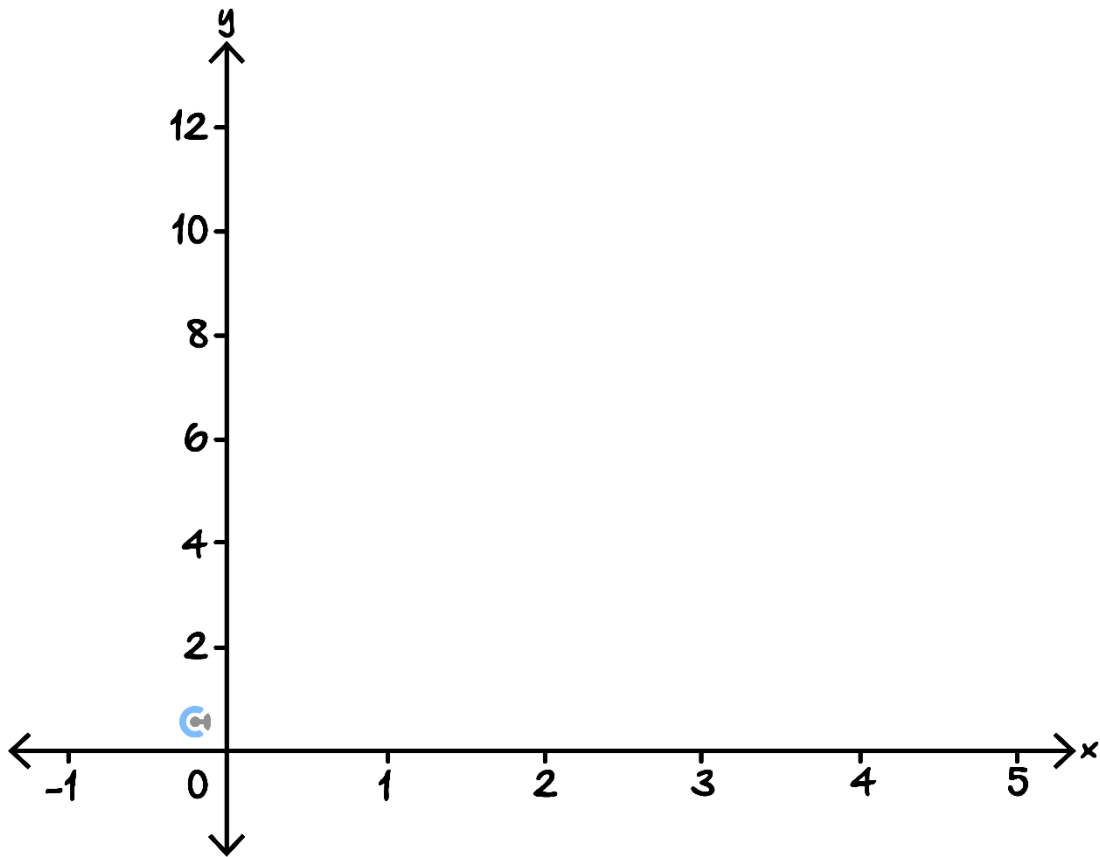
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Question 74

Sketch the graph of $y = x^4 - 8x^3 + 22x^2 - 24x + 10$ on the axis below.

Hint: Factorise $x^4 - 8x^3 + 22x^2 - 24x + 9$ instead.



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Section F: [1.6] - Polynomials Exam Skills (Checkpoints)

Sub-Section [1.6.1]: Solve Polynomial Inequalities



Question 75



Solve the following inequalities for x :

a. $x(x - 1)(x + 2) \leq 0$.

b. $(x - 2)(x + 1)(x + 3) > 0$.

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Question 76

Solve the following inequalities for x :

a. $(x - 5)(x^2 + x - 2) \leq 0$.

b. $(1 - x)(x^2 - 4x + 4) \geq 0$.

Space for Personal Notes

Question 77


Solve the following inequalities for x :

a. $x^3 - 5x^2 - 8x + 12 > 0$.

b. $-x^3 + 4x^2 + x - 4 \leq 0$.

Question 78


Solve the inequality $4x^5 - 16x^4 + 13x^3 - 3x^2 > 4x^3 - 16x^2 + 13x - 3$.

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Sub-Section [1.6.2]: Solve Number of Solution Problems

Question 79



Find the values of k , for which the equation $x(x^2 + 4) = 4kx^2$ has:

a. 1 solution.

b. 2 solutions.

c. 3 solutions.


Question 80

Find the values of k , for which the equation $kx^9 + 2x^6 + x^3 = 0$ has:

a. 1 solution.

b. 2 solutions.

c. 3 solutions.

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Question 81

Find the values of k , for which the equation $x(x - 2k - 2)(x^2 + kx + 4) = -x^2 - kx - 4$ has:

a. 4 solutions.

b. 3 solutions.

c. 2 solutions.

d. 1 solution.

e. No solutions.

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Consider the polynomial $P(x) = x^3 + ax + b$.

Show that if $\Delta = -4a^3 - 27b^2 = 0$, that $P(x) = 0$ has less than 3 solutions.

Hint: If r_1, r_2, r_3 are the roots of $P(x)$, show that $\Delta = (r_1 - r_2)^2(r_2 - r_3)^2(r_3 - r_1)^2$.

Please use a calculator.

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Sub-Section [1.6.3]: Apply Bisection Method to Approximate x -Intercepts

Question 83 CAS-Active.



Use the bisection method to find the approximate real solution to the equation $x^3 + 2x^2 - 5x + 3 = 0$. Use the interval $[-4, -3]$ for the first iteration and a maximum error of 0.1. Give your approximation correct to two decimal places.

Question 84 CAS-Active.



Use the bisection method to find the approximate real solution to the equation $x \log_2(x) + 3x = 4$. Use the interval $[0.1, 2]$ for the first iteration and a maximum error of 0.01. Give your approximation correct to two decimal places.

Question 85 CAS-Active.


Use the bisection method to approximate π correct to three decimal places.

Question 86


Explain why you cannot use the bisection method to approximate the solution to the equation $x^4 - 2x^2 + 1 = 0$.

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Section G: [1.1 - 1.6] - Exam 1 Overall**Question 87**

Let the coordinates of the point X be (a, b) . Find the coordinates of X' , which is the point on X reflected across the lines $x = 1$ and $y = -3$. Give your answer in terms of a and b .

Question 88

Find the equation of the line that is parallel to $y = -3x - 4$ and passes through the point $(7, 5)$.

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Question 89

Solve the simultaneous linear equations:

$$\frac{2}{3}x + \frac{1}{2}y = 4,$$

$$\frac{5}{4}x - \frac{5}{4}y = -\frac{5}{4}.$$

Question 90

Consider the functions $f(x) = 2x + 3$ and $g(x) = (x + 2)^2$.

- a. Find the vertical distance between f and g , when $x = 2$.

- b. Find the horizontal distance between f and g , when $y = 4$.

- c. Find the distance between the point $(2, 4)$ and $g(x)$, when $x = 14$.

Question 91

Consider the simultaneous linear equations:

$$\frac{m}{3}x - y = m,$$

$$4x + my = -7,$$

Where m is a real constant.

- a. Find the values of m for which there is a unique solution to the simultaneous equations.

- b. If possible, determine the value(s) of m for which there are infinitely many solutions.

- c. If possible, determine the value(s) of m for which there are no solutions.

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Question 92

Cam is standing at the point $(1, 6)$ when a bus goes past him. The bus' path is described by the line $2y - 3x = 4$. Find the shortest distance between Cam and the bus.

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Question 93 (4 marks)

- a. For what values of x is $x^2 - 7x + 12 > 0$? (2 marks)

- b. For what values of x is $1 - \frac{1}{x} - \frac{12}{x^2} > 0$? (2 marks)

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Question 94 (3 marks)

The sum of the age of a son and his father is 35 years and the product is 150. Find their ages.

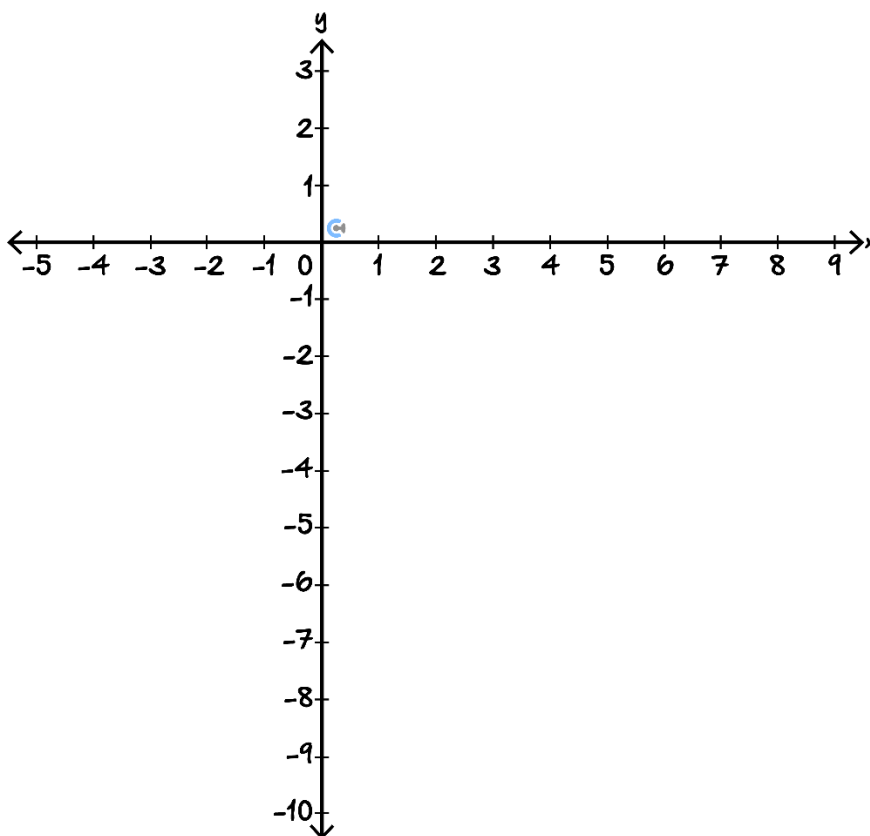
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Question 95 (4 marks)

Consider the function $f(x) = x^2 - 4x - 5$.

- a. Solve the equation $f(x) = 0$. (1 mark)

- b. Sketch the graph of $y = f(x)$ on the axes below. Label the turning point and all axes intercept with coordinates. (2 marks)



c. Hence, find the value(s) of x such that $f(x) + 5 < 0$. (1 mark)

Question 96 (2 marks)

Solve the inequality $x^2 - 6x - 7 \leq 0$.

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Question 97 (3 marks)

Consider the function $f(x) = kx^2 - 4x + 6$, where k is a real number. Find all possible values of k if $f(x)$ is always greater than 1.

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Question 98 (5 marks)

Consider the function $f(x) = x^2 - kx - 4$, where k is a real number.

- a.** Show that the graph $y = f(x)$ always has two x -intercepts. (1 mark)

- b.** Find the values of k such that the distance between the two x -intercepts is less than 6. (3 marks)

- c.** Find the minimum possible distance between the two x -intercepts. (1 mark)

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Question 99

Consider the polynomial $f(x) = x^3 - 7x + 6$.

a. Show that $f(1) = 0$.

b. Solve $f(x) = 0$ for x .

c. Hence, solve $f(x) \geq 0$ for x .

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Question 100

For what values of k does the equation $k(x^3 + x^2) = x$ have exactly one solution.

Question 101

Consider the polynomial $f(x) = x^3 - 3x^2 + x + 1$.

- a. Fully factorise $f(x)$ into linear factors.

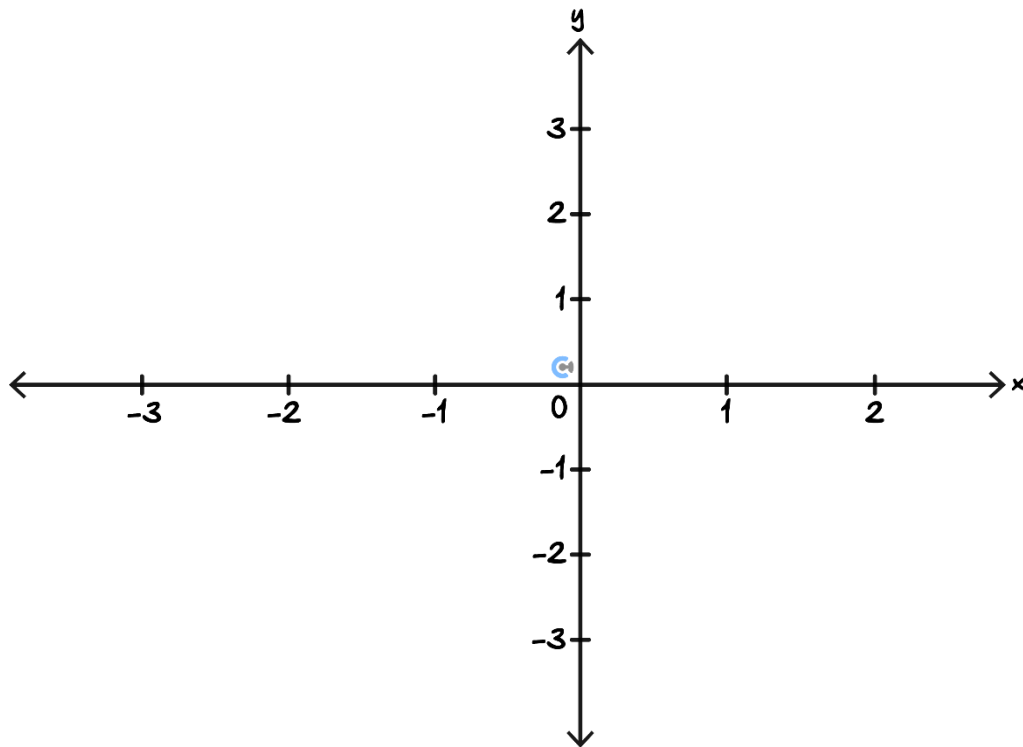
- b. A bisection method is used to solve $f(x) = 0$ with the first interval being $[2,3]$.
Use the fact that $\sqrt{2} \approx 1.4$ to write down the next 3 intervals.

Question 102

Let $f(x) = x^4 + 3x^3 + x^2 - 3x - 2$.

- a. Show that $x^2 - 1$ is a factor of f .

- b. Sketch the graph of $y = f(x)$ on the axis below. Label all axis intercepts with their coordinates.
Note that some turning points occur at $(-1.69, -0.40)$ and $(0.44, -2.83)$.



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Question 103 (5 marks)

Let P be a point on the straight line $y = 2x - 4$ such that the length of OP , the line segment from the origin O to P , is a minimum.

- a.** Find the coordinates of P . (3 marks)

- b.** Find the distance OP . Express your answer in the form $\frac{a\sqrt{b}}{b}$, where a and b are positive integers. (2 marks)

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Question 104

Consider the simultaneous linear equations:

$$kx - 3y = k + 3$$

$$4x + (k + 7)y = 1$$

Where k is a real constant.

- a. Find the value of k for which there are infinitely many solutions.

- b. Find the values of k for which there is a unique solution.

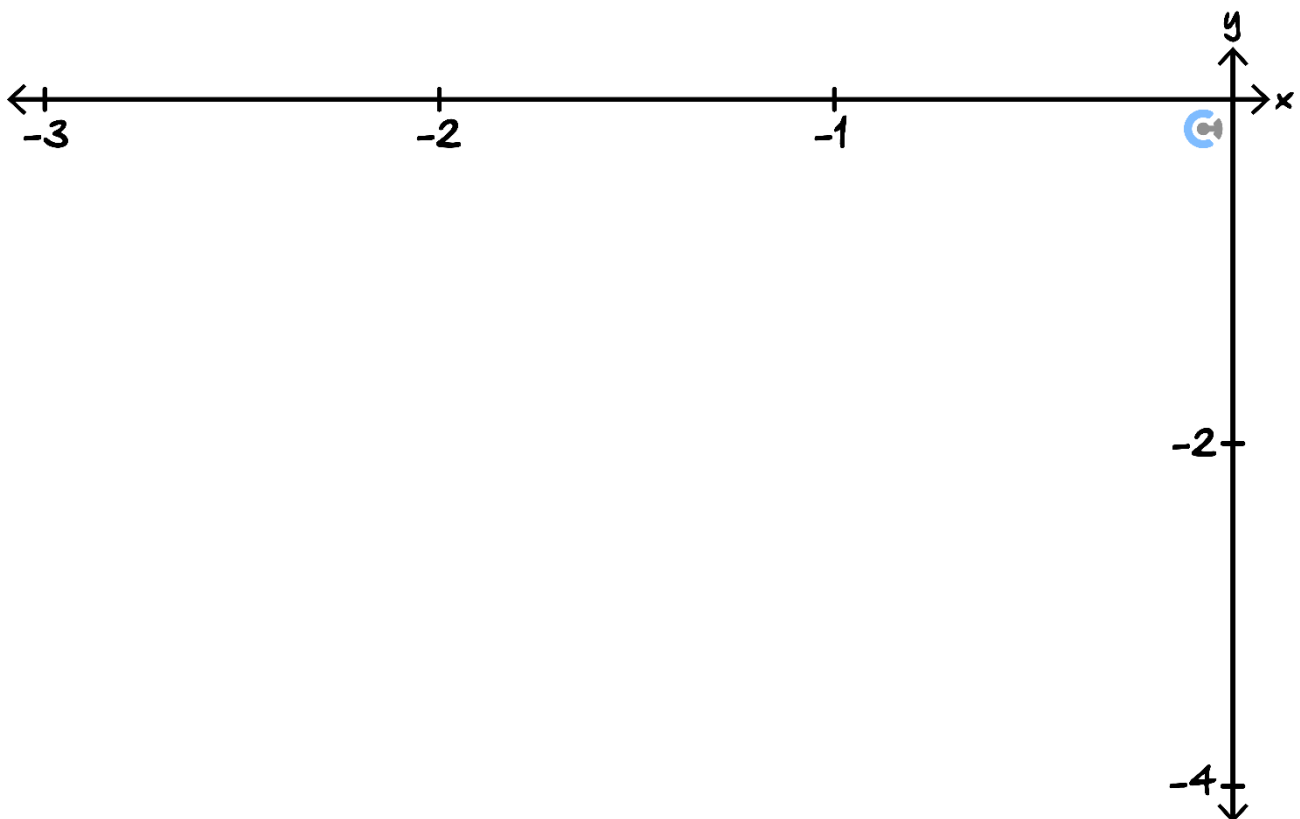
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Question 105 (4 marks)

Let $f: [-3, 0] \rightarrow \mathbb{R}, f(x) = (x + 2)^2(x - 1)$.

a. Show that $(x + 2)^2(x - 1) = x^3 + 3x^2 - 4$.

b. Sketch the graph of f on the axes below. Label the axis intercept and any stationary points with their coordinates.



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