



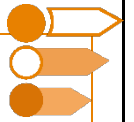
Website: contoureducation.com.au | Phone: 1800 888 300

Email: hello@contoureducation.com.au

VCE Mathematical Methods ½
Quadratics Exam Skills [0.4]
Workshop

Section A: Recap

Sub-Section: Factorising Quadratics



Factorising Quadratics



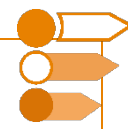
$$y = (x - a)(x - b)$$

► Steps:

1. Divide by the coefficient of the leading term. (If applicable)
2. Consider the factors of the constant term.
3. (If Positive Constant Term): See which pair of factors can add up to the coefficient of the x term.
(If Negative Constant Term): See which pair of factors can subtract from the coefficient of the x term.
4. Construct the linear factors.

Space for Personal Notes

Sub-Section: Perfect Squares



Perfect Squares

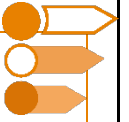
$$(a + b)^2 = a^2 + 2ab + b^2$$

$$(a - b)^2 = a^2 - 2ab + b^2$$

- ▶ Perfect squares are special quadratic expressions that are made up of two **identical** linear factors.
- ▶ In other words, when a linear factor is squared, it becomes a perfect square.

Space for Personal Notes

Sub-Section: Difference of Squares



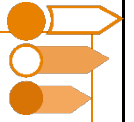
Difference of Squares

$$a^2 - b^2 = \underline{(a-b)(a+b)}$$



Space for Personal Notes

Sub-Section: Completing the Square



Completing the Square

- ▶ When we complete the square of a quadratic $x^2 + bx + c$, we write it in the form:

$$x^2 + bx + c = \left(x + \frac{b}{2} \right)^2 - \left(\frac{b}{2} \right)^2 + c$$

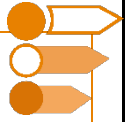
(Note: In the original image, 'x' and 'b' are blue, '2' is red, and a red squiggle is under the denominator of the second term.)

- ▶ Steps:

1. We halve the coefficient of x .
2. Subtract the half of the coefficient of x squared outside the square bracket.

Space for Personal Notes

Sub-Section: Solving by Factorisation



Solving by Factorisation

Null factor

$$(x - a)(x - b) = 0$$

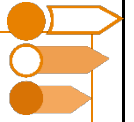
$$\Rightarrow x = a \text{ or } b$$

► Steps:

1. Factorise the quadratic.
2. Equate each factor to 0 and solve for x .

Space for Personal Notes

Sub-Section: Quadratic Formula



The Quadratic Formula

$$\text{for } ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Space for Personal Notes

Sub-Section: Discriminant



The Discriminant

Definition:

- The discriminant, often denoted by Δ (Delta), is the part **inside** the square root of the quadratic formula.

$$\text{Discriminant} = \Delta = b^2 - 4ac$$

if $\Delta > 0$, there are 2 solutions.

if $\Delta = 0$, there is 1 solution.

if $\Delta < 0$, there are 0 solutions.

Space for Personal Notes

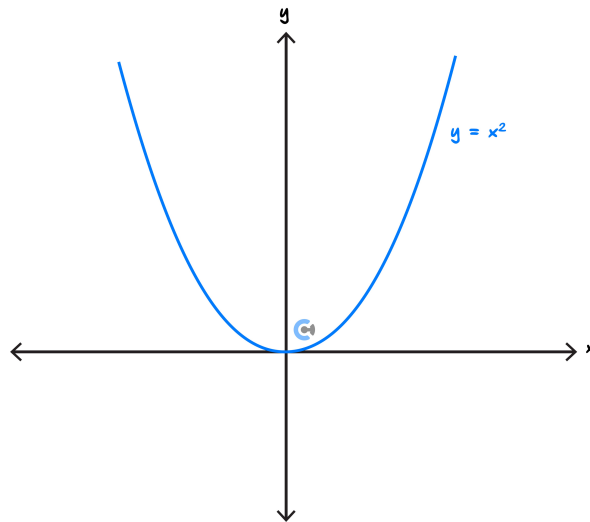
Sub-Section: Parabola and Symmetry



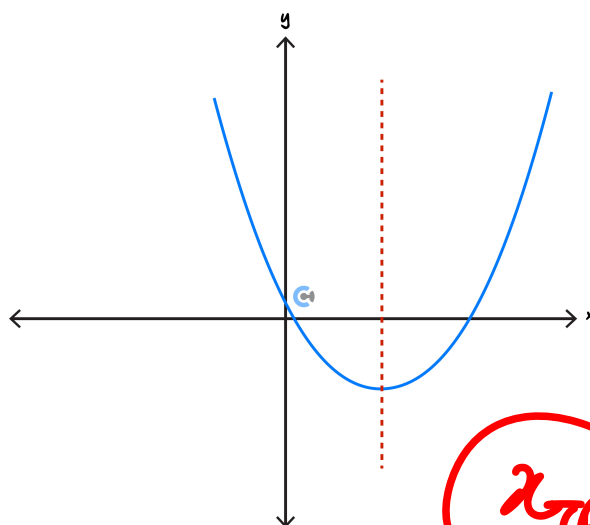
Parabola

► Definition:

- The shape of the graph of a quadratic is known as a parabola.



Axis of Symmetry



Axis of symmetry: $x = -\frac{b}{2a}$

Sub-Section: Graphing Quadratics



Turning Point Form



- ▶ The turning point form of a quadratic is given by:

$$y = a(x - h)^2 + k$$

$$\text{Turning point} = \underline{(h, k)}$$

- ▶ The turning point form is obtained by **completing the square**.

Intercept Form



- ▶ The x -intercept form of a quadratic is given by:

$$y = a(x - b)(x - c)$$

$$x\text{-intercepts: } \underline{(b, 0)} \text{ and } \underline{(c, 0)}$$

- ▶ The axis of symmetry is located exactly in the middle of the two x -intercepts.

NOTE: When a is negative, the x -intercepts stay the same, but the **shape** of the parabola becomes a **negative** parabola instead.



Space for Personal Notes

Sub-Section: Finding a Rule of a Quadratic from a Graph

Finding the Equation of a Quadratic

Form 1: Turning Point Form

$$y = a(x - h)^2 + k$$

Sub in another point

- Recommended when a turning point is easy to identify.

Form 2: x -intercept Form

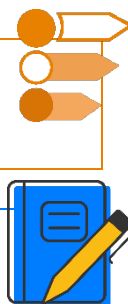
$$y = a(x - b)(x - c)$$

- Recommended when both x -intercepts are easy to identify.

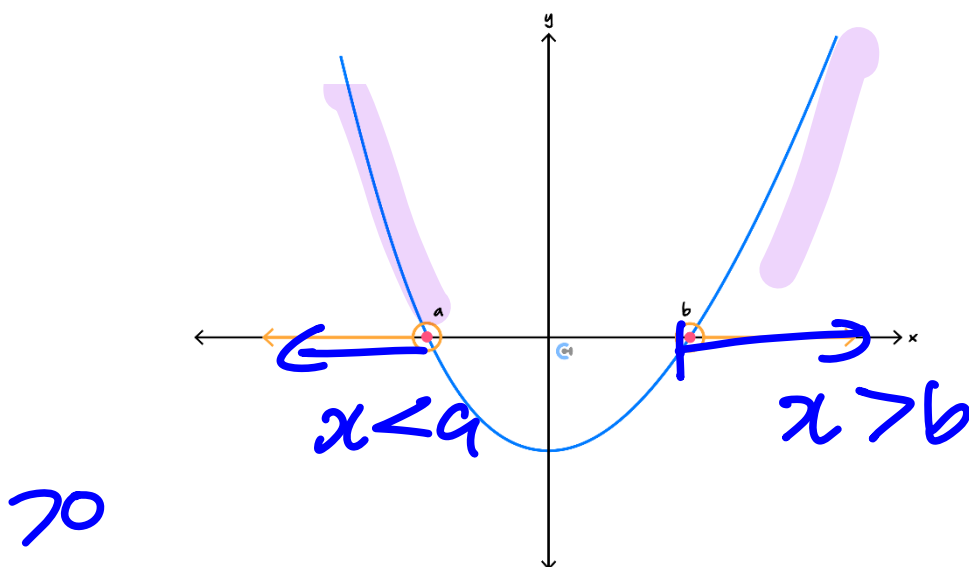
NOTE: Never forget the a coefficient!

Space for Personal Notes

Sub-Section: Quadratic Inequalities



Quadratic Inequalities



► For quadratic inequalities, we always Sketch the function.

► Steps:

1. Sketch the function.
2. See where the y -value is within the inequality.
3. Find the corresponding x -values.

Space for Personal Notes

Sub-Section: Hidden Quadratics

Hidden Quadratics

► Instead of:

$$\begin{aligned} & (x^2)^2 \\ & x^4 \quad \downarrow \quad A = x^2 \\ & af(x)^2 + bf(x) + c = 0 \end{aligned}$$

► We can let $f(x) = X$ to have:

$$aX^2 + bX + c = 0$$

Completing the square quickly.

$$y = a(x - h)^2 + k$$

► Steps

1. Find the turning point using $\left(-\frac{b}{2a}, f\left(-\frac{b}{2a}\right)\right)$.
2. Use the leading coefficient as a .

Modelling with Quadratics

Focus on key points such as turning points, x -intercepts and y -intercepts.

Family of Functions

- **Definition:** Functions with unknowns.
- **Question Type:** Find the unknown value to satisfy a certain condition.

Space for Personal Notes

Section B: Warmup

Question 1

Let $f(x) = -\frac{x^2}{2} + 3x - \frac{5}{2}$.

- a. Write $f(x)$ in turning point form. *→ complete the square*

$$-\frac{1}{2}(x^2 - 6x + 5)$$

$$= -\frac{1}{2}((x-3)^2 + 5 - (-3)^2)$$

$$= -\frac{1}{2}((x-3)^2 - 4)$$

$$= -\frac{1}{2}(x-3)^2 + 2$$

- b. Solve the equation $f(x) = 0$.

$$0 = -\frac{1}{2}(x-3)^2 + 2$$

$$\frac{1}{2}(x-3)^2 = 2$$

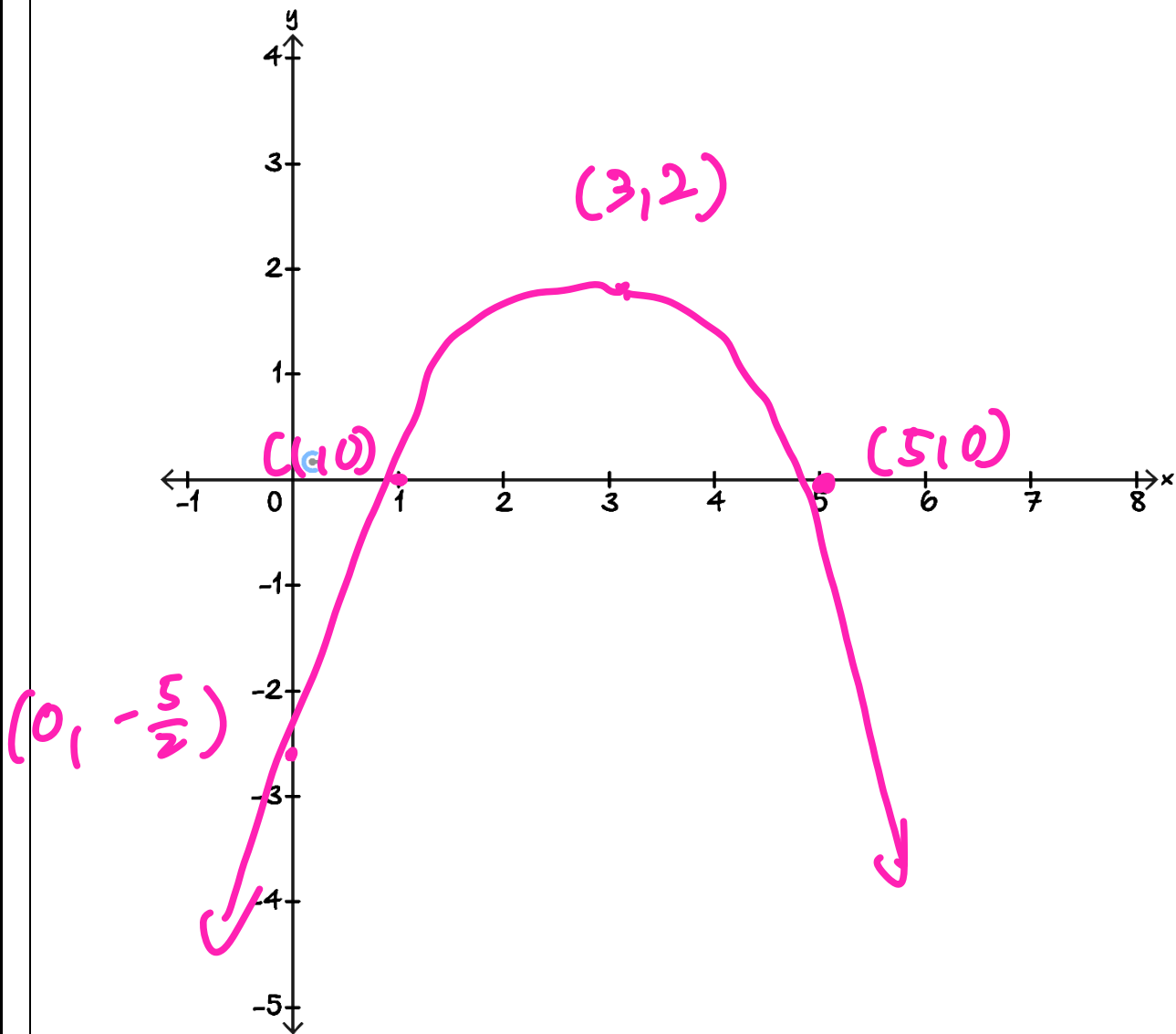
$$(x-3)^2 = 4$$

$$x-3 = \pm 2$$

$$x = 3 \pm 2$$

$$x = 5, 1$$

- c. Sketch the graph of $y = f(x)$ on the axes below, Label all axes intercepts and the turning point.



- d. Find the value of m such that the line $y = mx - 2$ intersects the graph of $y = f(x)$ exactly once.

$$y = -\frac{x^2}{2} + 3x - \frac{5}{2}$$

$$mx - 2 = -\frac{x^2}{2} + 3x - \frac{5}{2}$$

$$0 = -\frac{x^2}{2} + 3x - \frac{5}{2} + 2 - mx$$

$$0 = -\frac{x^2}{2} + (3-m)x - \frac{1}{2}$$

$$\Delta = 0 \quad (3-m)^2 - 4(-\frac{1}{2})(-\frac{1}{2}) = 0$$

$$(3-m)^2 - 1 = 0$$

$$(3-m)^2 = 1$$

$$3-m = \pm 1$$

$$m = 3 \pm 1$$

$$m = 2, 4$$

Section C: Exam 1 (22 Marks)

Question 2 (3 marks)

The sum of the ages of a man and his son is 30, and the product of their ages is 125.

- a. Write down a quadratic equation in the form $ax^2 + bx + c = 0$ that can be solved to find the ages of the man and his son, where x is the age of the son. (1 mark)

$$\begin{cases} x + y = 30 \\ xy = 125 \end{cases} \Rightarrow y = -x + 30$$

$$x(-x + 30) = 125$$

$$-x^2 + 30x = 125$$

$$0 = x^2 - 30x + 125$$

- b. Find the ages of the man and his son. (2 marks)

$$0 = (x - 5)(x - 25)$$

$$x = 5 \quad | \quad 125$$

$$y = -5 + 30 \quad | \quad y = -25 + 30$$

$$y = 25 \quad | \quad y = 5$$

$$x = 5, y = 25 \quad | \quad x = 25, y = 5$$

$\rightarrow \therefore$ Son is 5 yrs old
and father is 25 yrs old

Space for Personal Notes

Question 3 (6 marks)

Consider the function $f(x) = 2x^2 - 4x - 6$.

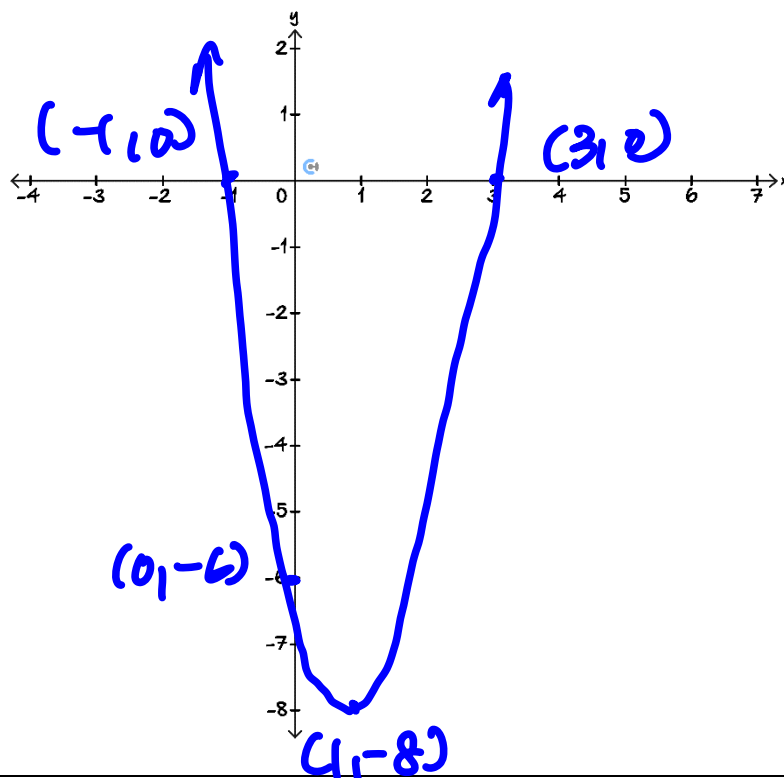
- a. Solve the equation $f(x) = 0$. (1 mark)

$$\begin{aligned} 2x^2 - 4x - 6 &= 0 \\ 2(x^2 - 2x - 3) &= 0 \\ 2(x - 3)(x + 1) &= 0 \\ x &= 3, -1 \end{aligned}$$

- b. Write $f(x)$ in turning point form. (1 mark)

$$\begin{aligned} f(x) &= 2x^2 - 4x - 6 \\ &= 2(x^2 - 2x - 3) \\ &= 2((x - 1)^2 - (-1)^2 - 3) \\ &= 2((x - 1)^2 - 4) \\ &= 2(x - 1)^2 - 8 \end{aligned}$$

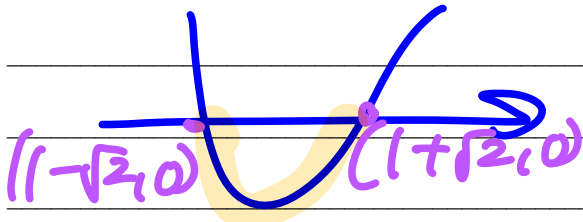
- c. Sketch the graph of $y = f(x)$ on the axes below. Label the turning point and all axes intercepts with coordinates. (2 marks)



d. Find the value(s) of x such that $f(x) + 4 < 0$. (2 marks)

$$2x^2 - 4x - 6 + 4 < 0$$

$$2x^2 - 4x - 2 < 0$$



$$2x^2 - 4x - 2 = 0$$

$$x^2 - 2x - 1 = 0$$

$$x = \frac{2 \pm \sqrt{4 + 4}}{2}$$

$$x = \frac{2 \pm 2\sqrt{2}}{2}$$

$$x = 1 \pm \sqrt{2}$$

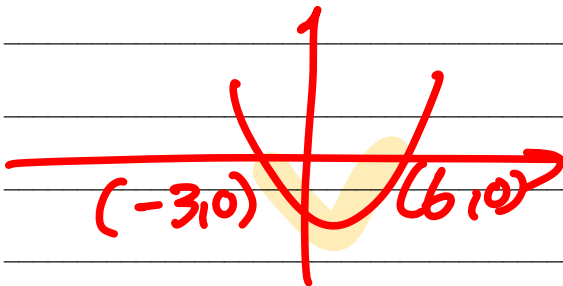
$$1 - \sqrt{2} < x < 1 + \sqrt{2}$$

Question 4 (2 marks)

Solve the inequality $-x^2 + 3x + 18 \geq 0$.

$$x^2 - 3x - 18 \leq 0$$

$$(x+3)(x-6) \leq 0$$



$$-3 \leq x \leq 6$$

Space for Personal Notes

Question 5 (3 marks)

Solve the equation $2x^4 - 20x^2 + 18 = 0$, for real values of x .

$$(x^2)^2$$

$$\text{Let } A = x^2$$

$$2A^2 - 20A + 18 = 0$$

$$2(A^2 - 10A + 9) = 0$$

$$2(A - 9)(A - 1) = 0$$

$$A = 1, 9$$

$$x^2 = 1, 9$$

$$x = \pm 1, \pm 3$$

Space for Personal Notes

Question 6 (4 marks)

Consider the function $f(x) = x^2 - 3kx + 6$, where k is a real number.

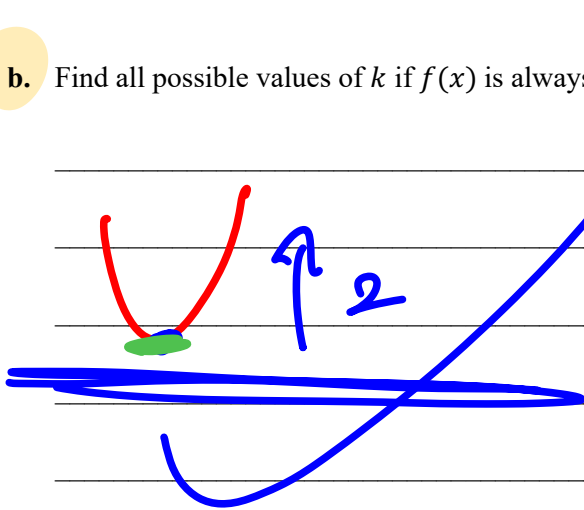
- a. Find the turning point of $f(x)$ in terms of k . (2 marks)

$$f(x) = \left(x - \frac{3k}{2}\right)^2 - \left(-\frac{3k}{2}\right)^2 + 6$$

$$= \left(x - \frac{3k}{2}\right)^2 - \frac{9k^2}{4} + 6$$

$$TP\left(\frac{3k}{2}, 6 - \frac{9k^2}{4}\right)$$

- b. Find all possible values of k if $f(x)$ is always greater than 2. (2 marks)



$$6 - \frac{9k^2}{4} > 2$$

$$- \frac{9k^2}{4} > -4$$

$$\frac{9k^2}{4} < 4$$

$$9k^2 < 16$$

$$k^2 < \frac{16}{9}$$

$$k^2 - \frac{16}{9} < 0$$

$$k^2 - \left(\frac{4}{3}\right)^2 < 0$$

Space for Personal Notes

$$(k - \frac{4}{3})(k + \frac{4}{3}) < 0$$


$$-\frac{4}{3} \quad \frac{4}{3} \quad k$$

$$-\frac{4}{3} < k < \frac{4}{3}$$

Question 7 (4 marks)

Consider the function $f(x) = x^2 + 2kx - 4$, where k is a real number.

- a. Show that the graph $y = f(x)$ always has two x -intercepts. (1 mark)

$$\Delta = (2k)^2 - 4(1)(-4)$$

$$= 4k^2 + 16$$

$$k^2 \geq 0$$

$$4k^2 \geq 0$$

$$4k^2 + 16 > 0$$

$$\Delta > 0$$

\Rightarrow 2 roots

- b. Find the values of k such that the distance between the two x -intercepts is less than 6. (3 marks)

$$y = x^2 + 2kx - 4$$

$$x = \frac{-2k \pm \sqrt{4k^2 + 16}}{2}$$

$x =$

2

$$= \frac{-2k \pm 2\sqrt{k^2 + 4}}{2}$$

$$= -k \pm \sqrt{k^2 + 4}$$

$$-k + \sqrt{k^2 + 4}$$

$$-k - \sqrt{k^2 + 4}$$

$$\sqrt{3}$$

Space for Personal Notes

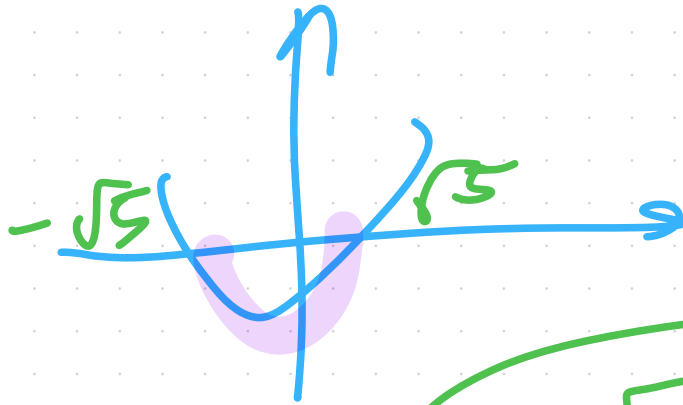
$$(-k + \sqrt{k^2 + 4}) - (-k - \sqrt{k^2 + 4})$$

$$2\sqrt{k^2 + 4} < 6$$

$$\sqrt{k^2 + 4} < 3$$

$$k^2 + 4 < 9$$

$$k^2 - 5 < 0$$



$$k^2 - 5 = 0$$
$$k = \pm\sqrt{5}$$

$$-\sqrt{5} < k < \sqrt{5}$$

Section D: Tech Active Exam Skills

Calculator Commands: Solving equations



Mathematica

Solve[

In[122]:= Solve[x^2 - 4x - 9 == 0, x]
 Out[122]:= {{x -> 2 - Sqrt[13]}, {x -> 2 + Sqrt[13]}}

TI-Nspire

Menu -> 3 -> 1.

solve(x^2 - 4x - 9 = 0, x)
 $x = -(\sqrt{13} - 2)$ or $x = \sqrt{13} + 2$

Casio Classpad

Action -> Advanced -> Solve.

solve(x^2 - 4x - 9 = 0, x)
 $\{x = -\sqrt{13} + 2, x = \sqrt{13} + 2\}$

Calculator Commands: Completing the Square



TI-Nspire

Menu -> 3 -> 5 completeSquare
 (func, var).

completeSquare(x^2 - 6x + 8, x) $(x - 3)^2 - 1$

Mathematica

No inbuilt function need udf.

Compsq

Compsq[a x^2 + b x + c, x]
 Converts a standard form quadratic to turning point form.

Compsq[a, b, c]
 Uses the coefficients of a quadratic to return the turning point form.

in: 1
 out: 1

Compsq[1, 2, 3]

2 (1 + x)^2

in: 2
 out: 2

Compsq[2 x^2 + 3 x - 5, x]

Continue [-5 + 3 x + 2 x^2, x]

Casio Classpad

No function

converts

Space for Personal Notes

Section E: Exam 2 (28 Marks)

Question 8 (1 mark)

Find the value(s) of k for which the quadratic equation below has exactly one unique real solution.

$$2x^2 - 3kx + 3k = 0$$

$$\Delta = 0$$

A. $k = \frac{8}{3}$

B. $k = 0, \frac{8}{3}$

C. $k > \frac{8}{3}$

D. $k = 0, 3$

solve $((-3 \cdot k)^2 - 4 \cdot 2 \cdot 3 \cdot k = 0)$

$k=0$ or $k=\frac{8}{3}$

Question 9 (1 mark)

A quadratic function has a turning point at $(4, 3)$ and goes through the point $(6, 7)$. What is the equation of the function?

A. $2(x - 4)^2 + 3$

B. $-(x - 4)^2 + 3$

C. $(x - 3)^2 + 4$

D. $(x - 4)^2 + 3$

solve $y = a(x-4)^2 + 3, a$ at $x=6$ and $y=7$

$a=1$

$y = a(x-4)^2 + 3$

Question 10 (1 mark)

The function $f(x) = x^2 + mx + 2$ is always greater than -1 . The possible values of m are:

A. $-\sqrt{3} < m < \sqrt{3}$

B. $-2\sqrt{2} < m < 2\sqrt{2}$

C. $-2\sqrt{3} < m < 2\sqrt{3}$

D. $-1 < m < 1$

completeSquare $(x^2 + m \cdot x + 2, x)$

$\left(x + \frac{m}{2}\right)^2 - \frac{m^2}{4} + 2$

$m^2 < 12$

solve $\left(-\frac{m^2}{4} + 2 > -1\right)$
 $-\frac{m^2}{4} > -3$
 $-m^2 > -12$

Question 11 (1 mark)

If one root of the quadratic equation $2x^2 + px - 35 = 0$ is -7 the value of p is:

A. -9

B. 9

C. -4

D. 4

solve $(2 \cdot x^2 + p \cdot x - 35 = 0, p) | x = -7$

$p = 9$

Question 12 (1 mark)

The equation $ax^2 + 6x + c = 0$ has only one real solution if:

A. $ac > -9$

B. $2ac = 9$

C. $ac = -9$

D. $ac = 9$

$\Delta = 0$

$6^2 - 4 \cdot a \cdot c = 0$

$36 = 4ac$

$9 = ac$

Space for Personal Notes

Question 13 (14 marks) **① define**
 Consider the quadratic function $f(x) = x^2 - 4x + 2$.

a.

i. Solve the equation $f(x) = 0$. (1 mark)

$$\pm\sqrt{2+2}$$

ii. State the distance between the x -axis intercepts. (1 mark)

$$\sqrt{2+2} - (-\sqrt{2+2}) = 2\sqrt{2}$$

iii. Find the turning point of the graph of $y = f(x)$. (1 mark)

com. sq, $-\frac{b}{2a} \rightarrow f(\quad)$
 $(2, -2)$

iv. Hence write $f(x)$ in turning point form. (1 mark)

$$f(x) = (x-2)^2 - 2$$

v. Find the y -intercept of the graph of $y = f(x)$. (1 mark)

$x=0$ $f(0) = 2$ $(0, 2)$

define

$$f(x) = x^2 - 4x + 2$$

$$\text{solve } (f(x)=0, x)$$

$$-(\sqrt{2-2}) - (\sqrt{2+2})$$

$$\frac{-4}{2 \cdot 1} = -\frac{b}{2a}$$

$$f(2)$$

$$f(0)$$

Done

$$x = -(\sqrt{2-2}) \text{ or } x = \sqrt{2+2}$$

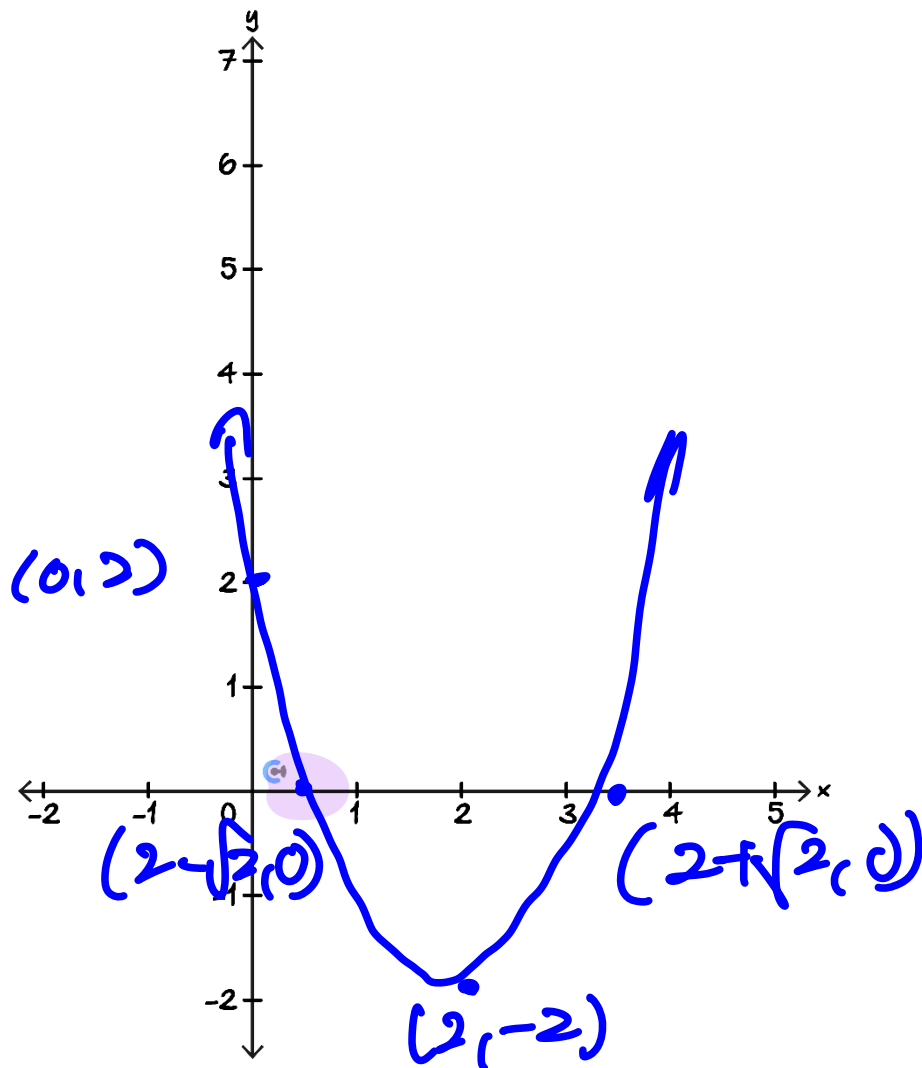
$$-2 \cdot \sqrt{2}$$

$$2$$

$$-2$$

$$2$$

b. Sketch the graph of $y = f(x)$ on the axes below. (2 marks)



c. If the graph of $y = f(x)$ is shifted k units to the left, find the values of k for which there is one negative x -axis intercept. (2 marks)

$$2 - \sqrt{2} < k < 2 + \sqrt{2}$$

- d. The graph of $y = f(x)$ is translated 1 unit to the left and 4 units up and now has the equation:

$$y = a(x - h)^2 + k, \quad a, h, k \in \mathbb{R}$$

Determine the values of a, h, k . (2 marks)

$$(2, -2) \rightarrow (1, 2)$$

$$y = 1(x - 1)^2 + 2$$

$$a = 1 \quad h = 1 \quad k = 2$$

- e. Consider the graph of the function $g(x) = 4x^2 + kx + 2(k + 1)$

Find the value(s) of k for which $g(x)$ will have:

- i. No real root. (1 mark)

$$\Delta < 0$$

CAS

$$16 - 12\sqrt{2} < k < 16 + 12\sqrt{2}$$

- ii. One real root. (1 mark)

$$\Delta = 0$$

CAS

$$k = 16 \pm 12\sqrt{2}$$

- iii. Two unique real roots. (1 mark)

$$\Delta > 0$$

$$k < 16 - 12\sqrt{2}$$

$$k > 16 + 12\sqrt{2}$$

Space for Personal Notes

Question 14 (9 marks)

A cricket player hits a ball, and the ball's trajectory is modelled by the quadratic equation:

$$h(x) = ax^2 + bx + c,$$

where $h(x)$ is the height of the ball (in metres) above the ground, and x is the horizontal distance (in metres) from where the ball was hit.

The following conditions are given:

- The ball is hit from a height of 2 metres, i.e., $h(0) = 2$.
- The ball reaches a height of 15 metres when it has travelled 8 metres horizontally.
- The ball reaches a height of 25 metres when it has travelled 16 metres horizontally.

a. Using the given conditions, set up and solve a system of equations to determine the values of a , b , and c . (3 marks)

$$2 = a \times 0 + b \times 0 + c$$

$$15 = 64a + 8b + c$$

$$25 = 256a + 16b + c$$

CAS

max
graph

Define $h(x) = a \cdot x^2 + b \cdot x + c$

solve $\begin{cases} h(0)=2 \\ h(8)=15 \\ h(16)=25 \end{cases}, \{a, b, c\}$

Done

$$a = -\frac{3}{128} \text{ and } b = \frac{29}{16} \text{ and } c = 2$$

b. Determine the maximum height that the ball reaches. Give your answer correct to 2 decimal places. (1 mark)

Define $h(x) = a \cdot x^2 + b \cdot x + c$ and $a = -\frac{3}{128}$ and $b = \frac{29}{16}$ and $c = 2$

$$h(x) = -\frac{3}{128}x^2 + \frac{29}{16}x + 2$$

$$\text{completeSquare} \left(-\frac{3}{128}x^2 + \frac{29}{16}x + 2 \right)$$

$$\text{completeSquare} \left(-\frac{3}{128}x^2 + \frac{29}{16}x + 2 \right)$$

$$37.0417 - 0.023438 \cdot (x - 38.6667)^2$$

comp. 39

$$-\frac{b}{2a}$$

sub in

$$\frac{889}{24}$$

$$= 37.04$$

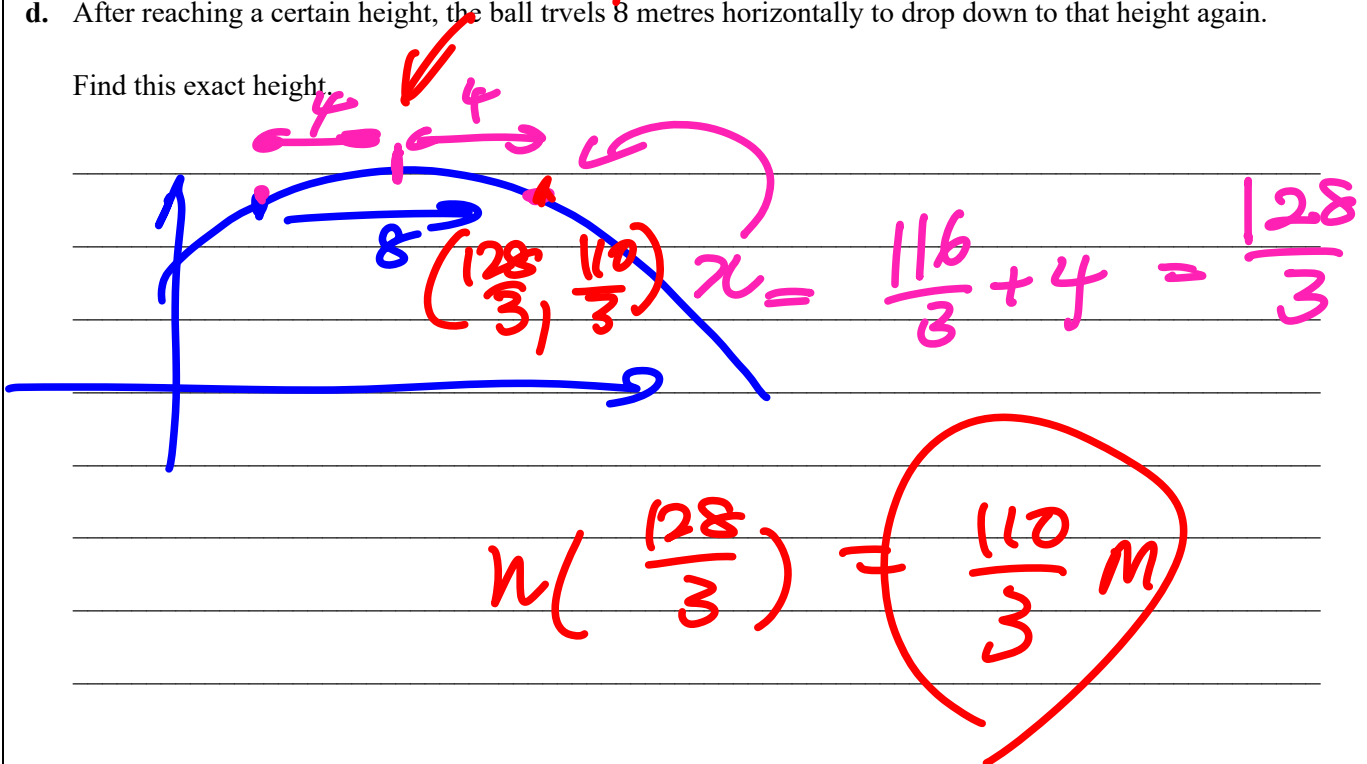
- c. Determine the horizontal distance the ball has travelled when its height is 20 metres. Provide both possible horizontal distance correct to two decimal places. (2 marks)

$$h(x) = 20$$

$$\text{solve}(h(x)=20, x)$$

$$x = 11.7017 \text{ or } x = 65.6317$$

- d. After reaching a certain height, the ball travels 8 metres horizontally to drop down to that height again. Find this exact height.



Space for Personal Notes

Section F: Extension Exam 1 (16 Marks)**Question 15** (4 marks)

The parabola $y = ax^2 + bx + c$ passes through the points $(1, -\frac{1}{2})$, $(4, -5)$, and $(6, -3)$.

Determine the values of real numbers a , b , and c .

Space for Personal Notes

Question 16 (4 marks)

Let $f(x) = 2x^2 - 4x + 5$.

- a. Find the turning point of the parabola $y = f(x)$. (1 mark)

- b. Reflect this turning point in the line $x = 3$ and then in the line $y = 2$. (1 mark)

- c. The parabola $y = f(x)$ is reflected in the line $x = 3$ and then reflected in the line $y = 2$. Find the equation of the resulting parabola in the form $y = ax^2 + bx + c$, where a, b , and c are real numbers. (2 marks)

Space for Personal Notes

Question 17 (4 marks)

Solve $(x^2 + 1)^2 + 4 \geq 8x^2$ for all real x .

Space for Personal Notes

Let $f(x) = x^4 - 4kx^2 + 4 - k^2$, where k is a real constant.

[illegible]

MM12 [0.4] – Quadratics Exam Skills – Workshop Extension

Section G: Extension Exam 2 (16 Marks)

Question 19 (1 mark)

If $px^2 + 5x + q = 0$ has two roots $x = -2$ and $x = 1$, the value of $p - q$ is:

- A. -5
- B. 5
- C. 10
- D. 15

Question 20 (1 mark)

The equation of the parabola that passes through the points $(1, 2)$, $(3, 2)$ and $(4, 5)$ is:

- A. $y = x^2 - 4x - 5$
- B. $y = (x - 2)^2 + 1$
- C. $y = x^2 + 4x + 5$
- D. $y = (x - 1)^2 + 2$

Question 21 (1 mark)

Consider the graph of $y = x^2 - 2kx - 2$ where k is a real constant.

The values of k for which the distance between the two x -intercepts is less than 6 are:

- A. $-\sqrt{5} < k < \sqrt{5}$
- B. $-\sqrt{6} < k < \sqrt{6}$
- C. $-\sqrt{7} < k < \sqrt{7}$
- D. $-\sqrt{11} < k < \sqrt{11}$

Space for Personal Notes

Question 22 (1 mark)

Let $y = 2x^2 - 4x - 2$.

If $-2 < x < 3$, the possible values of y are:

- A. $-4 < y \leq 14$
- B. $-4 \leq y < 14$
- C. $4 < y < 14$
- D. $-4 < y < 14$

Question 23 (1 mark)

Find all values of k , such that $x^2 + kx + k^2 - 4$ has two real roots for x , where one is positive and one is negative.

- A. $k < 2$
- B. $k > -2$
- C. $-2 < k < 2$
- D. $-2 \leq k \leq 2$

Space for Personal Notes

Question 24 (11 marks)

Consider the function $f(x) = x^2 + (k - 2)x + \frac{k^2 - 4k - 4}{2}$, where k is a real constant.

a.

- i.** Find all values of k such that $f(x) = 0$ has one real root.. (1 mark)

- ii.** Find all values of k such that $f(x) = 0$ has two real roots. (1 mark)

- iii.** Find all values of k such that $f(x) = 0$ has two real roots, where one is positive and the other is negative. (2 marks)

- b.** Find all values of k for which the graph of $y = f(x)$ and the graph $y = kx + 2$ do not intersect. (2 marks)

c. Find all values of k such that $f(x) > 2$ for all real x . (2 marks)

d. Find all values of k such that the graph of $y = f(x)$ has two x -intercepts that have a distance between them that is less than 2. (3 marks)

Space for Personal Notes



Website: contoureducation.com.au | Phone: 1800 888 300 | Email: hello@contoureducation.com.au

VCE Mathematical Methods ½

Free 1-on-1 Consults

What Are 1-on-1 Consults?

- ▶ **Who Runs Them?** Experienced Contour tutors (45 + raw scores and 99 + ATARs).
- ▶ **Who Can Join?** Fully enrolled Contour students.
- ▶ **When Are They?** 30-minute 1-on-1 help sessions, after-school weekdays, and all-day weekends.
- ▶ **What To Do?** Join on time, ask questions, re-learn concepts, or extend yourself!
- ▶ **Price?** Completely free!
- ▶ **One Active Booking Per Subject:** Must attend your current consultation before scheduling the next :).

SAVE THE LINK, AND MAKE THE MOST OF THIS (FREE) SERVICE!

Booking Link

bit.ly/contour-methods-consult-2025



