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Write your **student number** in the boxes above.

Letter

Mathematical Methods 1/2

Examination 2 (Tech-Active)

Question and Answer Book

VCE Examination (Term 1 Mock) - April 2025

- Reading time is 15 minutes.
- Writing time is 2 hours.

Materials Supplied

- · Question and Answer Book of 21 pages.
- · Multiple-Choice Answer Sheet.

Instructions

- · Follow the instructions on your Multiple-Choice Answer Sheet.
- At the end of the examination, place your Multiple-Choice Answer Sheet inside the front cover of this book.

Students are **not** permitted to bring mobile phones and/or any unauthorised electronic devices into the examination room.

Contents	pages	
Section A (2 questions, 20 marks)	· -	
Section B (7 questions, 60 marks)		
Student's Full Name:		
Student's Email:		
Tutor's Name:		
Marks (Tutor Only):		

Section A

Instructions

- Answer all questions in pencil on the Multiple-Choice Answer Sheet.
- Choose the response that is **correct** or that **best answers** the question.
- A correct answer scores 1; an incorrect answer scores 0.
- Marks will not be deducted for incorrect answers.
- No marks will be given if more than one answer is completed for any question.
- Unless otherwise indicated, the diagrams in this book are not drawn to scale.

Question 1

The gradient of a line perpendicular to the line which passes through (-2,0) and (0,-4) is:

A.
$$\frac{1}{2}$$

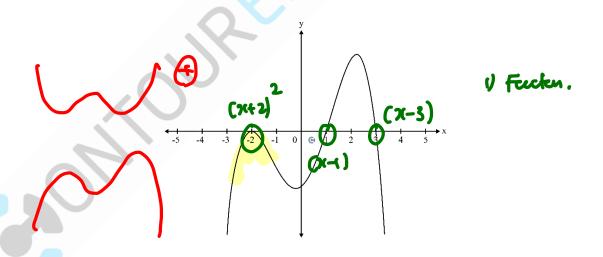
B.
$$-2$$

C.
$$-\frac{1}{2}$$

$$m = \frac{0 - -4}{-2 - 0} = \frac{4}{-2} = -2$$

Question 2

The diagram below shows part of the graph of a polynomial function.



A possible rule for this function is:

A.
$$y = (x+2)^2(x-1)(x-3)$$

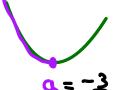
B.
$$y = (x+2)^2(x-1)(3-x)$$

C.
$$y = -(x-2)^2(x-1)(3-x)$$

D.
$$y = -(x+2)(x-1)(x-3)$$

$$(x+2)^{2}(x+1)(x-3)$$

step befor the typ The largest value of a such that the function $f: (-\infty a) \to R$, $f(x) = x^2 + 3x - 10$ is not many-to-one is equal to .: /:J



$$\int (x) = (x + \frac{3}{2})^2 - \frac{9}{4} - 10$$

Question 4

+ 4 has a horizontal asymptote with the equation: The graph of y =

A.
$$y = 4$$

B.
$$y = 3$$

B.
$$y = 3$$

C.
$$x = -2$$

D.
$$x = -3$$

$$y = \frac{\alpha}{(m+1)^2} +$$

Question 5

If $f(x - 1) = x^2 - 2x + 3$, then f(x) is equal to:

A.
$$x^2 - 2$$

B.
$$x^2 + 2$$

C.
$$x^2 - 2x + 2$$

D.
$$x^2 - 4x + 6$$

 $f(x-1) = x^2 - 2x + 3$

Question 6

The graph of a function f is obtained from the graph of the function g with the rule $g(x) = \sqrt{2x-5}$ via a reflection in the x-axis ollowed by a dilation from the y-axis by a factor of $\frac{1}{2}$.

Which one of the following is the rule for the function f?

A.
$$f(x) = \sqrt{5 - 4x}$$

B.
$$f(x) = -\sqrt{x-5}$$

C.
$$f(x) = \sqrt{x+5}$$

D.
$$f(x) = -\sqrt{4x - 5}$$

$$2x'=2$$

$$f: -y' = \int 2(2x') - 5$$

The point A(3,2) lies on the graph of the function f. A <u>transformation maps</u> the graph of f to the graph of g, where $g(x) = \frac{1}{2}f(x-1)$. The same transformation maps point A to point P.

f → 2

Dil I from x axis.

The coordinates of the point *P* are:

C.
$$(4,1)$$
D. $(4,2)$
 $y = \frac{1}{3} f(x-1)$

D.
$$(4,2)$$
 $y = \frac{1}{3} f(x-1)$

Question 8

2) Apply the same tradi-

Travelle | unt right
$$A:(3,2) \rightarrow (3,1)$$

The domain and the range for the relation with the equation $2 - y = \frac{3}{(x-1)^2}$ are given by:

A.
$$\{x: x \in R \setminus \{1\}\} \text{ and } \{y: y > 2\}.$$

B.
$$\{x: x \in R \setminus \{1\}\}\$$
and $\{y: y < 2\}.$

C.
$$\{x: x \in R \setminus \{1\}\}\$$
and $\{y: y < -2\}.$

D.
$$\{x: x \in R \setminus \{1\}\} \text{ and } \{y: y \in R \setminus \{2\}\}.$$





Question 9

The graph of a cubic function of the form $y = a(x + h)^3 + k$ has a stationary point of inflection at (-2, 2)and intercepts the *y*-axis at 10. The equation of the function is: $a(x-(-2))^3+2$ a(x+2)3+2

A.
$$\frac{y-(x-2)^3+2}{x^2+2}$$

$$B_{-} y - 2(x+2)^3 + 10$$

$$C. - \frac{y - (x + 2)^3 + 10}{2}$$

D.
$$y = (x+2)^3 + 2$$

A function has the rule, $f(x) = 2x^{\frac{1}{3}} + 8$, $x \in R$. The rule for the inverse function is:

A.
$$f^{-1}(x) = \frac{2}{x} - 8$$

B.
$$f^{-1}(x) = \frac{1}{2x^3 - 8}$$

C.
$$f^{-1}(x) = \left(\frac{x-8}{2}\right)^3$$

D.
$$f^{-1}(x) = 2x^3 - 8$$

$$\frac{2-8}{2} = \sqrt{3}$$

$$\left(\frac{x-R}{2}\right)^3 = \left(y^{(1)}\right)^3$$

$$\left(\frac{2x-8}{2}\right)^3 = y'$$

Which of the following functions is not one-to-one?

A.
$$f(x) = 25 - x^2 x < 0$$

B. $f(x) = \frac{1}{x^2} + 25$

$$\mathbf{C.} \ \ f(x) = 4\sqrt{x}$$

D. $f(x) = -\frac{5}{x}$



Question 12

If $f(x) = \begin{cases} -3x + 5 & x \ge -2 \\ x + 5 & x < -2 \end{cases}$ then the range of f is:

A.
$$(-\infty, 1]$$

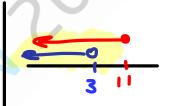
B.
$$(-\infty, 11)$$

C.
$$(-\infty, 11]$$

D.
$$(-5,\infty) \cup (-\infty,5]$$



< 3



Page: 6-00,11

Question 13

If $4(x-1)^2 = a(x+1)^2 + bx$ for all real values of x, the values of a and b are:

A.
$$a = 4$$
, $b = 16$ 4 $x^2 - 8x + 4 = ax^2 + 2ax + a + b > 4$

B.
$$a = 4$$
, $b = -16$

C.
$$a = 4$$
, $b = 4$ $(4x^2) - 3x + 4 = (ax^2) + (2a+b) + a$

D.
$$a = 4$$
, $b = -6$

Question 14

The angle, in degrees, between the lines $y = 2x + \frac{5}{3}$ and $y = \frac{3x}{27} - \frac{10}{27}$ is closest to:

B.
$$0.20$$
 $\theta = ton$

C. 8.13

D.
$$0.14$$
 = $tan^{-1} \left(\frac{2-3}{(+2\times3)} \right)$

Question 15

Let $p(x) = x^3 - ax + 1$ where $a \in \mathbb{R}$. If the remainder of p(x) when divided by ax + 8 is 1, hen the value of a is:

$$p(x) \div (ax+8)$$

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Three-letter words are to be made by arranging the letters of the word NETHODS. What is the probability that a randomly chosen arrangement begins with a vowel?

A.
$$\frac{2}{7}$$
B. $\frac{3}{10}$
C. $\frac{1}{3}$
D. $\frac{4}{11}$
Prob = # arranged ve want = $\frac{2 \times 6 \times 5}{7 \times 6 \times 5}$
 $\frac{3}{7 \times 6 \times 5}$
 $\frac{7}{7 \times 6 \times 5}$

Question 17

Suppose that for three events A, B and C, $Pr(A \mid B) = 1$ and $Pr(C \mid B) = Pr(C)$. Which of the following is true? **HINT:** $X \subseteq Y$ means X is part of Y.

A. Pr(A) = 1.

B. $C \subseteq B$. Pr(ANB) = Pr(B)

C. B and C are independent events and $B \subseteq A$.

The following information applies to the two questions that follow:

The probability that Zoe bakes cookies on Friday is 0.55. If she bakes on Friday, the probability that she bakes again on Saturday is 0.75. If she does not bake on Friday, the probability that she bakes on Saturday is 0.25.

Question 18

The probability that Zoe bakes on **both** Friday and Saturday is closest to

A. 0.41

A (BF (Bs)

B. 0.20 **C.** 0.15

25.0 × 22.0 =

D. 0.55

Question 19

The probability that Zoe bakes on **Saturday** is closest to

A. 0.57 **B.** 0.48 Pr(Bs) = Pr(BF(Bs) + Pr(BF'(Bs))

C. 0.53

D. 0.34

=0.55 x0.75 + 0.45 x 0.25

Question 20 Factor 45.

If the solutions of $x^2 + bx + 6 = 0$ are integers, the possible values of b are:

A. 5 and 7.

B.
$$-5$$
 and -7 .

C.
$$\pm 5$$
 and ± 7 .

D.
$$-5$$
 and 7 .

Section B

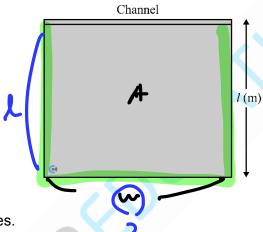
Instructions

- Answer **all** questions in the spaces provided.
- Write your responses in English.

Question 1 (5 marks)

A piece of fencing 960 m ong will be used to enclose three sides of a rectangular field. The fourth side has a straight channel along it.

Let *l* be the length of the field as shown. Let *A* be the area of the field.



All measurements are in metres.

a. Express A as a function q l.

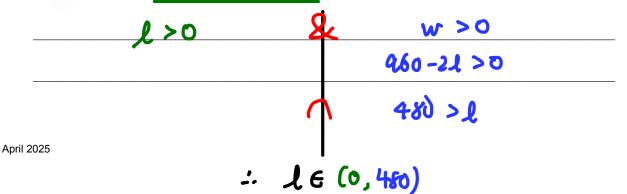
2 marks

$$A = w \cdot 1$$

$$= (960-21)1$$

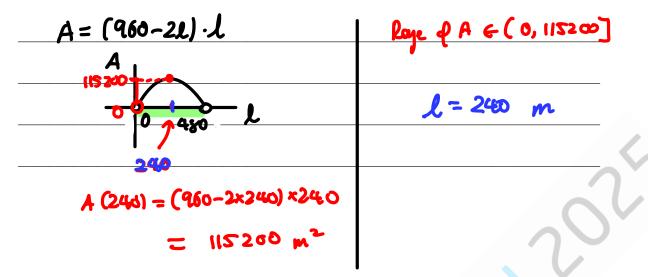
$$= (960-21)1$$

b. What is a suitable domain of the function *A*? 1 mark



c. Determine the range of A. Also state the value of l for which the maximum area occurs.

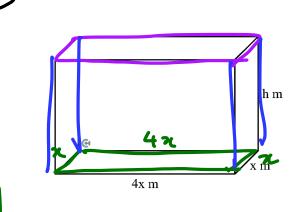
2 marks



Question 2 (11 marks)

A cuboid (rectangular prism) has dimensions x metres, h metres and 4x metres as shown on the diagram.

The cuboid is made of 240 m of wire.

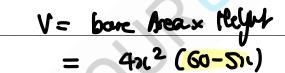


a. Find h in terms of x.

2 marks

$$\rho = 2(4x + 4x + x + x) + 4h = 240$$

b. Find the volume, $V m^3$, of the cuboid in terms of x.



1 mark

c. Find V when x = 11.

$$V(1) = 2420 m^3$$
.

d. Find the possible values of x for the cuboid to exist.

2 marks

60-5x70

26 20 12>2 **)** 0

ne (0,12)

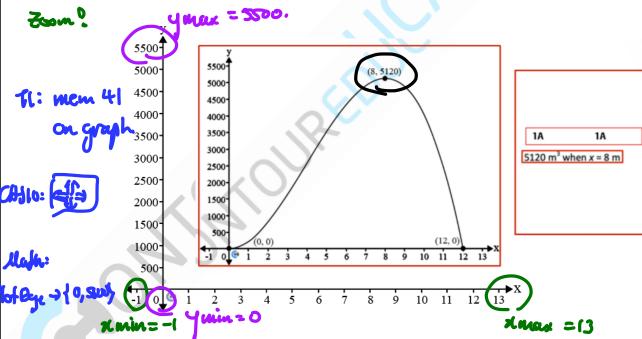
Find the possible values of x when V = 1620, correct to two decimal places.

1 mark

11.37. oc ≈ 3.00

Sketch the graph for the volume of the cuboid on the axes below. Label the endpoints with coordinates.

2 marks



2 marks

g. Hence, state the maximum volume of the cuboid and the value of x for which it occurs.

V= 5120

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Question 3 (8 marks)

The table shows the results of an experiment in which the air resistance (R) of a new car was measured for different speeds (S).

Speed (km/hr)	Resistance (kN)
0	(0)
5	1/
10	5
15	10
20	18
25	28
30	41
35	55
40	72
45	91
50	113
55	136
60	162
65	190
70	221
75	253

a. Using a linear model, R = aS + b (where a and b are constants) and the results for speeds $0 \, km/hr$ and $50 \, km/hr$, find appropriate values for a and b.

2 marks

0 = a.0+b	113 = ax 50 +b,
Q = P	113= 500
	$a = \frac{113}{50}$

b. Using a quadratic model, $R = cS^2 + d$ (where c and d are constants) and the results for speeds $0 \ km/hr$ and $50 \ km/hr$, find appropriate values for c and d.

2 marks

0= c·0²+d	$113 = c \cdot 50^2 + d.$
0 = d	(13
	2500 = C

c. Using a cubic model, $R = eS^3 + f$ (where e and f are constants) and the results for speeds $0 \ km/hr$ and $50 \ km/hr$, find appropriate values for e and f.

2 marks

$$0 = e \cdot 0^{3} + f$$

$$0 = f \cdot \frac{113}{125000} = e \cdot .$$

d. Using points (25 28) and (75 253), evaluate each of the three models. Which of the 2 marks models fits the data best?

Model 1: $R = \frac{1/3}{50}$ S	Sub in "s" valu-
	Makel 1: 12(25) = 113 x 25 = 36.5
Model 2: $R = \frac{113}{2500} s^2$	Chor = 56.5 -28 = 28.5
2,00	P(75)= 113 × 75 = 169.5
Model 3: $R = \frac{1(3)}{125000} 5^3$	om = 253 - 169.5 = 83-5
	Malel 2: P(251 = 28.25.
	Em = 28 -28. 25 = - 2. 24
	Q(75) = 254.25
	Fm = 253-254.25=1.25

Model 8: R(25) = 14.125

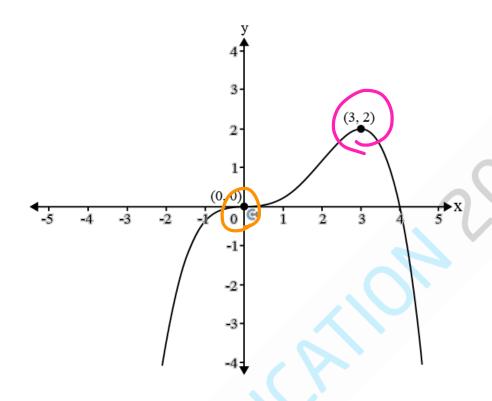
P(75)= 381.375

$$6mr = 253 - 381.335$$

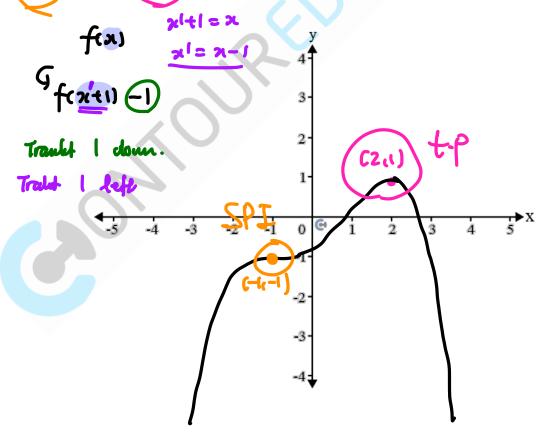
$$= -128.375$$

Question 4 (9 marks)

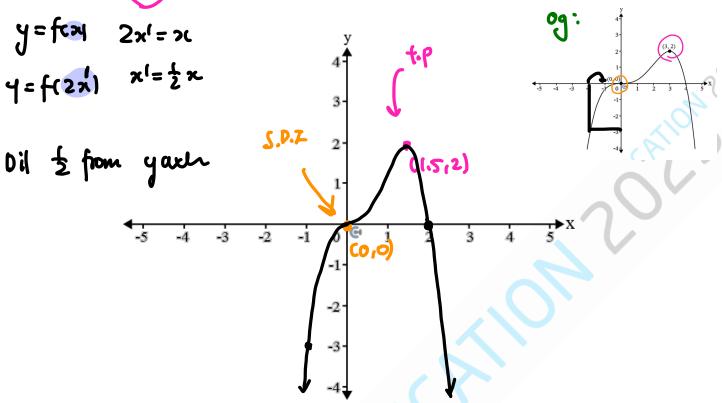
The diagram shows the graph of y = f(x) which passes through (0,0).



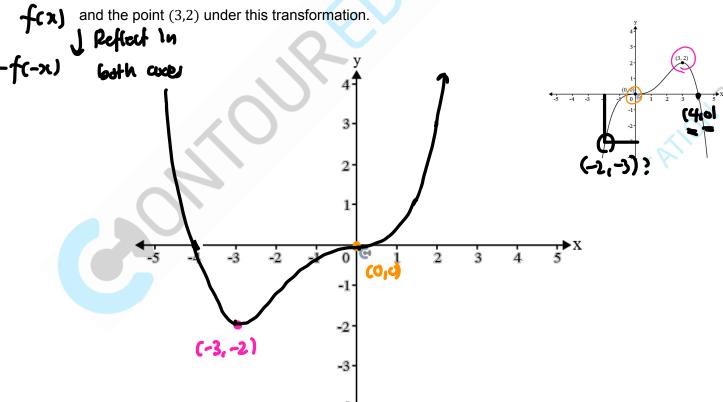
a. Sketch the graph of y = f(x + 1) - 1, Label the coordinates of the image of the point 3 marks (0,0) and the point (3,2) under this transformation.



b. Sketch the graph of y = f(2x), Label the coordinates of the image of the point (0,0) and 3 marks the point (3,2) under this transformation.



c. Sketch the graph of y = -f(-x). Label the coordinates of the image of the point (0,0) 3 marks



Question 5 (10 marks)

The revenue (in thousands of dollars) from the sale of x thousand items is given by $R(x) = 6(2x^2 + 10x + 3)$ and the manufacturing cost (in thousands of dollars) of x thousand items is $C(x) = x(6x^2 - x + 1)$.

a. State the degree of R(x) and C(x).

1 mark

Highet pour

& Always expus

Degree of C = 3,

b. Calculate the revenue and the cost of 1000 items sold and explain whether a profit is made.

2 marks

$$R(i) = 90$$
 4 90,000 $P(i) - C(i)$
 $C(i) = 6$ 4 6,000 $= 90 - 6 = 84$

c. Show that the profit (in thousand dollars) from the sale of x thousand items is given by $P(x) = -6x^3 + 13x^2 + 59x + 18$.

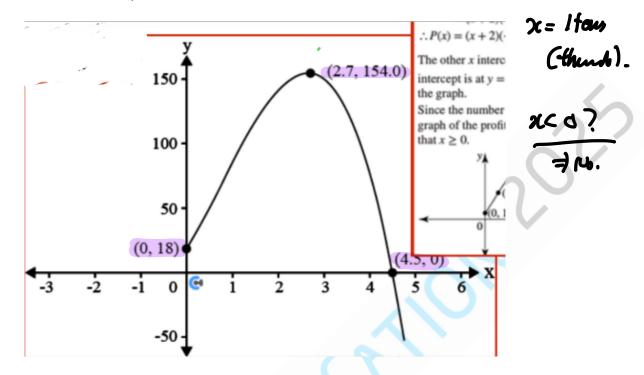
2 marks

$$P(x) = R(x) - C(x)$$

$$= 6(2x^{2} + 10x + 3) - x(6x^{2} - x + 1)$$

$$= 12x^{2} + 60x + 18 - 6x^{3} + x^{2} - x$$

d. Given the graph of $y = -6x^3 + 13x^2 + 59x + 18$ cuts the *x*-axis at x = -2, sketch the graph of y = P(x) for appropriate values of *x*. Label all axial intercepts and turning points correct to one decimal place.



e. If a loss occurs when the number of items manufactured is d, state the smallest value of d. 2 marks d.

Profit < 0.	: Itemy > 4500
	be ne is in
$\rho(x) < \rho$	thounds
	iden
x>4.5	
	Min I fem = d = 450

Question 6 (11 marks)

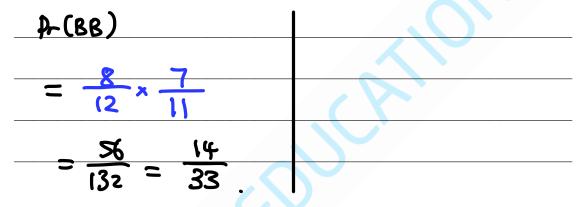
Ravi has two jars, each containing blue marbles and red marbles.

- **a.** The first jar contains 8 blue marbles and 4 red marbles.
 - i. If Ravi picks one marble at random from this jar, what is the probability it is blue?

1 mark

ii. If he picks two marbles from this jar without replacement, what is the probability they are both blue?

2 marks



iii. If he picks two marbles from this jar without replacement, what is the probability that2 marksthe second marble is blue?

1 1st can be red or ble

$$= \frac{14}{33} + \frac{4}{12} \times \frac{8}{11} = \frac{2}{3}$$

iv. What is the probability that the first marble was red given that the second marble is 2 marks blue?

$$Pr(1^{s+}=\text{Red} \mid 2^{nd} \text{ is blue}) = \frac{Pr(1^{s+}\text{ Red} \land 2^{nd}\text{ Blue})}{Pr(2^{nd} \text{ is blue})}$$

$$=\frac{\text{Pr}(RB)}{2/3} = \frac{\frac{4}{12} \times \frac{8}{11}}{2/3} = \frac{4}{11}$$
From (i)

- **b.** The second jar also contains 8 blue marbles, but Ravi does not know how many red marbles it holds. Suppose the second jar contains a total of m marbles.
 - i. Ravi picks two marbles at random from the second jar without replacement. Write an 2 marks expression in terms of m for the probability that both marbles are blue.

$$Pr(BB) = \frac{8}{m} \times \frac{7}{m-1}$$

$$= \frac{56}{m(m-1)}$$

ii. If the probability of selecting two blue marbles from the second jar is $\frac{4}{15}$, how many red 2 marks marbles are in the second jar?

$$Pr(BB) = \frac{56}{m(m-1)} = \frac{4}{15}$$
 $= 15 - 8$
 $= 7$
 $m = 15, -14$
 $= 7$
 $= 7$

Question 7 (6 marks)

A music festival organiser needs to assemble a four-member performance panel from a pool of n male performers and m female performers.

You may leave your answers in terms of ${}^{n}C_{r}$ or ${}^{n}P_{r}$.

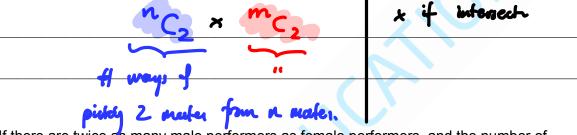
a. How many different panels can be formed? Give your answers in terms of m and n.

1 mark



b. How many panels consist of exactly two male performers and two female performers? 1 r Give your answers in terms of m and n.

1 mark



c. If there are twice as many male performers as female performers, and the number of gender-balanced panels is less than 720, what are the possible values of n?

gerraer balarreed partele is less than 720, what	are the pecchile values of n.
n = 2m	$2m! = 2m \times (2m-1) \times (2m-2)$
	$\frac{2m!}{(2m-2)!} = 2m \cdot (2m-1)$
find # panels with 2 natu	$m! = m \times (m-1) \times (m-2)!$
d 2 feul	
	(m-2)1.
= nC2 × mC2 from b)	2m(2m-1) $m(m-1)$
2m m	= 2! 2! 2720
	-4.82 / m. < 5.5 >
$=\frac{2m!}{2m!} \times \frac{m!}{2m!}$	
2!(2m-2)! $2!(m-2)!$	-9-64 < 2m < 11.14
$= \frac{n_{C_2} \times m_{C_2} \text{ fun b}}{2m_{C_2} \times m_{C_2}}$ $= \frac{2m!}{2!(2m-2)!} \times \frac{m!}{2!(m-2)!}$	$\frac{m!}{(m-2)!} = m(m-1)$ $= \frac{2m(2m-1)}{2!} \times \frac{m(m-1)}{2!} < 720$ $\frac{-4.82 < m < S.S.}{-9.64} < 2m < 11.14$

-9.14 < n < 11.64